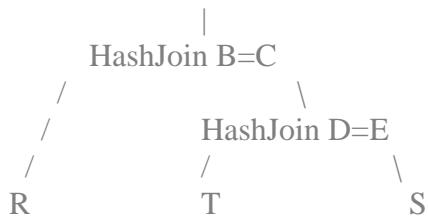


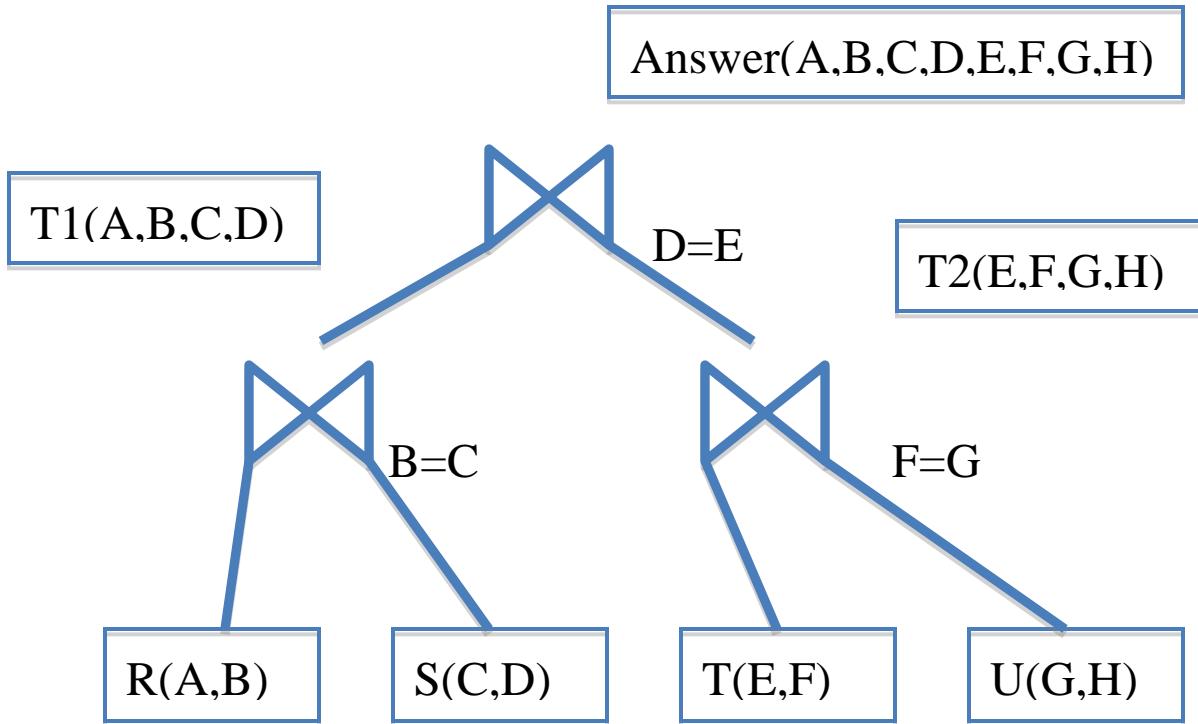
Section 9

1. Consider the query $R(A,B)$ join $S(C,D)$ join $T(E,F)$ (the join condition is $B=C$ and $D=E$). Suppose $M=100$, and $B(R)=30$, $B(S)=200$, $B(T)=60$, $B(R \text{ join } S)=80$, $B(S \text{ join } T)=50$. Design an optimal query plan that uses only main-memory hash join algorithms. Your plan may store intermediate results to disk if necessary.

Load R & T into memory and create hash tables of them. Then read blocks of S one at a time, performing the joins in the following graph. All intermediate results are pipelined.



2. Consider the algebra plan below. Each of the joint operators is a main memory hash join algorithm, using the Open(), GetNext(), Close() interface. Assuming that all joins are pipelining, show the execution steps for computing the entire join.



Where R, S, T, U have the following content:

R	
A1	B
A2	B

S	
B	D1
B	D2

T	
D1	F
D2	F

U	
F	H1
F	H2

```

T0.open
    T2.open
        U.open
        U.getNext
        U.getNext
        U.getNext // got NULL
        U.close
        T.open
    T2.getNext
        T.getNext
    T2.getNext
    T2.getNext
        T.getNext
    T2.getNext
    T2.getNext // got NULL
    T2.close
        T.close
    T1.open
        S.open
        S.getNext
        S.getNext
        S.getNext // got NULL
        S.close
        R.open
    T0.getNext
        T1.getNext
            R.getNext
    T0.getNext
    T0.getNext
        T1.getNext
    T0.getNext
    T0.getNext
        T1.getNext
            R.getNext
    T0.getNext
    T0.getNext
        T1.getNext
    T0.getNext
    T0.getNext
        T1.getNext
            R.getNext // got NULL

    T0.close
        T1.close
            R.close

```

- (b) [10 points] Consider the following query, where \bowtie denotes the natural join:

$$R(A, B) \bowtie S(B, C) \bowtie T(C, D) \bowtie U(D, E)$$

Here we only consider left linear plans

- i. How many different left linear plans exist for this query ?

$$n !$$

- ii. Show two different left linear plans without cartesian products.

$$\begin{aligned} & (((R \text{ join } S) \text{ join } T) \text{ join } U) \\ & (((T \text{ join } S) \text{ join } U) \text{ join } R) \end{aligned}$$

- iii. How many different plans without cartesian product exists for this query ?

$$2^{\wedge}(n-1)$$