

# Lecture 23: Query Optimization (3)

Monday, November 22, 2010

## Outline

- Search space
- Algorithms for enumerating query plans
- Estimating the cost of a query plan

## Computing the Cost of a Plan

- Collect statistical summaries of stored data
- Estimate size in a bottom-up fashion
- Estimate cost by using the estimated size

## Statistics on Base Data

- Collected information for each relation
  - Number of tuples (cardinality)
  - Indexes, number of keys in the index
  - Number of physical pages, clustering info
  - Statistical information on attributes
    - Min value, max value, number distinct values
    - Histograms
  - Correlations between columns (hard)
- Collection approach: periodic, using sampling

## Size Estimation Problem

```
S = SELECT list
FROM R1, ..., Rn
WHERE cond1 AND cond2 AND ... AND condk
```

Given  $T(R_1), T(R_2), \dots, T(R_n)$   
Estimate  $T(S)$

How can we do this ? Note: doesn't have to be exact.

## Size Estimation Problem

```
S = SELECT list
FROM R1, ..., Rn
WHERE cond1 AND cond2 AND ... AND condk
```

Remark:  $T(S) \leq T(R_1) \times T(R_2) \times \dots \times T(R_n)$

## Selectivity Factor

- Each condition *cond* reduces the size by some factor called selectivity factor
- Assuming independence, multiply the selectivity factors

## Example

R(A,B)  
S(B,C)  
T(C,D)

```
SELECT *
FROM R, S, T
WHERE R.B=S.B and S.C=T.C and R.A<40
```

T(R) = 30k, T(S) = 200k, T(T) = 10k

Selectivity of R.B = S.B is 1/3  
Selectivity of S.C = T.C is 1/10  
Selectivity of R.A < 40 is 1/2

What is the estimated size of the query output ?

## Rule of Thumb

- If selectivities are unknown, then:  
selectivity factor = 1/10  
[System R, 1979]

## Selectivities from Statistics

- Condition is A = c /\* value selection on R \*/  
– Selectivity = 1/V(R,A)
- Condition is A < c /\* range selection on R \*/  
– Selectivity = (c - Low(R, A))/(High(R,A) - Low(R,A))T(R)
- Condition is A = B /\* R ⋈<sub>A=B</sub> S \*/  
– Selectivity = 1 / max(V(R,A), V(S,A))  
– (will explain next)

## Assumptions

- Containment of values: if  $V(R,A) \leq V(S,B)$ , then the set of A values of R is included in the set of B values of S  
– Note: this indeed holds when A is a foreign key in R, and B is a key in S
- Preservation of values: for any other attribute C,  $V(R \bowtie_{A=B} S, C) = V(R, C)$  (or  $V(S, C)$ )

## Selectivity of $R \bowtie_{A=B} S$

Assume  $V(R,A) \leq V(S,B)$

- mmmmmmmhkh,mmmbknmmmmmmmmmmmmktt
- Each tuple t in R joins with T(S)/V(S,B) tuple(s) in S

- Hence  $T(R \bowtie_{A=B} S) = T(R) T(S) / V(S,B)$

In general:  $T(R \bowtie_{A=B} S) = T(R) T(S) / \max(V(R,A), V(S,B))$

## Size Estimation for Join

Example:

- $T(R) = 10000$ ,  $T(S) = 20000$
- $V(R,A) = 100$ ,  $V(S,B) = 200$
- How large is  $R \bowtie_{A=B} S$  ?

## Histograms

- Statistics on data maintained by the RDBMS
- Makes size estimation much more accurate (hence, cost estimations are more accurate)

## Histograms

Employee(ssn, name, age)

$T(\text{Employee}) = 25000$ ,  $V(\text{Employee, age}) = 50$   
 $\min(\text{age}) = 19$ ,  $\max(\text{age}) = 68$

$\sigma_{\text{age}=48}(\text{Employee}) = ?$      $\sigma_{\text{age}>28 \text{ and age}<35}(\text{Employee}) = ?$

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Estimate =  $25000 / 50 = 500$     Estimate =  $25000 * 6 / 60 = 2500$

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Age:	0..20	20..29	30-39	40-49	50-59	> 60
Tuples	200	800	5000	12000	6500	500

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Tuples	200	800	5000	12000	6500	500

Estimate = 1200

Estimate =  $2 * 80 + 5 * 500 = 2660$

## Types of Histograms

- How should we determine the bucket boundaries in a histogram ?

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- How should we determine the bucket boundaries in a histogram ?
- Eq-Width
- Eq-Depth
- Compressed

Employee(ssn, name, age)

## Histograms

**Eq-width:**

Age:	0..20	20..29	30-39	40-49	50-59	> 60
Tuples	200	800	5000	12000	6500	500

**Eq-depth:**

Age:	0..20	20..29	30-39	40-49	50-59	> 60
Tuples	1800	2000	2100	2200	1900	1800

**Compressed:** store separately some highly frequent values: (48,1900)

## Difficult Questions on Histograms

- Small number of buckets
  - Hundreds, or thousands, but not more
  - WHY ?
- *Not* updated during database update, but recomputed periodically
  - WHY ?
- Multidimensional histograms rarely used
  - WHY ?

## Summary of Query Optimization

- Three parts:
  - search space, algorithms, size/cost estimation
- Ideal goal: find optimal plan. But
  - Impossible to estimate accurately
  - Impossible to search the entire space
- Goal of today's optimizers:
  - Avoid very bad plans