

Lectures 8 and 9: Database Design

Wednesday&Friday, April 10&12

Announcements/Reminders

- Homework 1: solutions are posted
- Homework 2: posted (due Friday, April 20)
- Project Phase 1 due Friday, April 12

Outline

- The relational data model: 3.1
- Functional dependencies: 3.4

Schema Refinements = Normal Forms

- 1st Normal Form = all tables are flat
- 2nd Normal Form = obsolete
- Boyce Codd Normal Form = will study
- 3rd Normal Form = see book

First Normal Form (1NF)

- A database schema is in First Normal Form if all tables are flat

Student

Name	GPA	Courses			
Alice	3.8	<table border="1"><tr><td>Math</td></tr><tr><td>DB</td></tr><tr><td>OS</td></tr></table>	Math	DB	OS
Math					
DB					
OS					
Bob	3.7	<table border="1"><tr><td>DB</td></tr><tr><td>OS</td></tr></table>	DB	OS	
DB					
OS					
Carol	3.9	<table border="1"><tr><td>Math</td></tr><tr><td>OS</td></tr></table>	Math	OS	
Math					
OS					

Student

Name	GPA
Alice	3.8
Bob	3.7
Carol	3.9

Takes

Student	Course
Alice	Math
Carol	Math
Alice	DB
Bob	DB
Alice	OS
Carol	OS

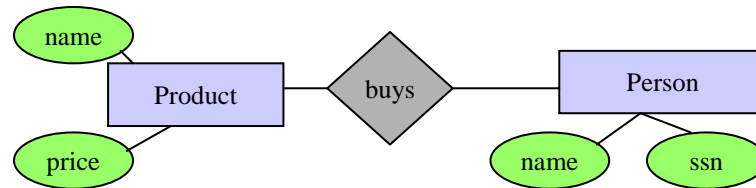
Course

Course
Math
DB
OS

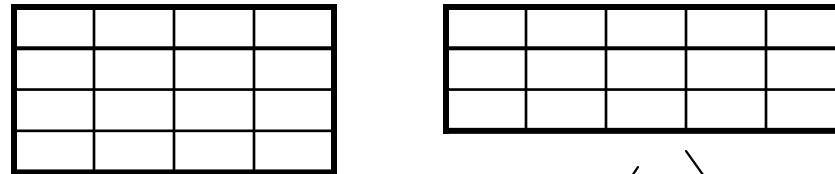
→
May need to add keys

Relational Schema Design

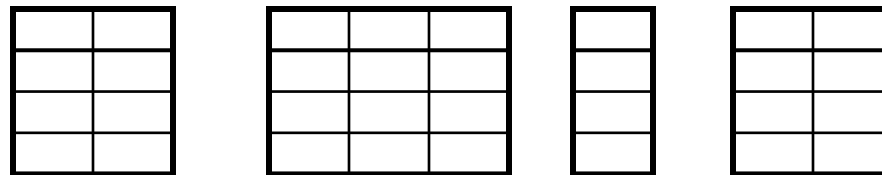
Conceptual Model:



Relational Model:
plus FD's



Normalization:
Eliminates anomalies



Data Anomalies

When a database is poorly designed we get anomalies:

Redundancy: data is repeated

Updated anomalies: need to change in several places

Delete anomalies: may lose data when we don't want

Relational Schema Design

Recall set attributes (persons with several phones):

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

One person may have multiple phones, but lives in only one city

Anomalies:

- Redundancy = repeat data
- Update anomalies = Fred moves to “Bellevue”
- Deletion anomalies = Joe deletes his phone number:
what is his city ?

Relation Decomposition

Break the relation into two:

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

Name	<u>SSN</u>	City
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield

<u>SSN</u>	<u>PhoneNumber</u>
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121

Anomalies have gone:

- No more repeated data
- Easy to move Fred to “Bellevue” (how ?)
- Easy to delete all Joe’s phone number (how ?)

Relational Schema Design (or Logical Design)

Main idea:

- Start with some relational schema
- Find out its *functional dependencies*
- Use them to design a better relational schema

Functional Dependencies

- A form of constraint
 - hence, part of the schema
- Finding them is part of the database design
- Also used in normalizing the relations

Functional Dependencies

Definition:

If two tuples agree on the attributes

$$A_1, A_2, \dots, A_n$$

then they must also agree on the attributes

$$B_1, B_2, \dots, B_m$$

Formally:

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$$

When Does an FD Hold

Definition: $A_1, \dots, A_m \rightarrow B_1, \dots, B_n$ holds in R if:

$$\forall t, t' \in R, (t.A_1=t'.A_1 \wedge \dots \wedge t.A_m=t'.A_m \Rightarrow t.B_1=t'.B_1 \wedge \dots \wedge t.B_n=t'.B_n)$$

R

	A_1	...	A_m		B_1	...	B_m		
t									
t'									

if t, t' agree here then t, t' agree here

Examples

An FD holds, or does not hold on an instance:

EmpID	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234	Lawyer

EmpID \rightarrow Name, Phone, Position

Position \rightarrow Phone

but not Phone \rightarrow Position

Example

EmpID	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876 ←	Salesrep
E1111	Smith	9876 ←	Salesrep
E9999	Mary	1234	Lawyer

Position → Phone

Example

EmpID	Name	Phone	Position
E0045	Smith	1234 →	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234 →	Lawyer

but not Phone → Position

Example

FD's are constraints:

- On some instances they hold
- On others they don't

name \rightarrow color
category \rightarrow department
color, category \rightarrow price

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Green	Toys	99

Does this instance satisfy all the FDs ?

Example

name → color
category → department
color, category → price

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Black	Toys	99
Gizmo	Stationary	Green	Office-supp.	59

What about this one ?

An Interesting Observation

If all these FDs are true:

name \rightarrow color
category \rightarrow department
color, category \rightarrow price

Then this FD also holds:

name, category \rightarrow price

Why ??

Goal: Find ALL Functional Dependencies

- Anomalies occur when certain “bad” FDs hold
- We know some of the FDs
- Need to find *all* FDs, then look for the bad ones

Armstrong's Rules (1/3)

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$$

Is equivalent to

$$\begin{aligned} A_1, A_2, \dots, A_n &\rightarrow B_1 \\ A_1, A_2, \dots, A_n &\rightarrow B_2 \\ &\dots \\ A_1, A_2, \dots, A_n &\rightarrow B_m \end{aligned}$$

**Splitting rule
and
Combing rule**

	A1	...	Am		B1	...	Bm	

Armstrong's Rules (1/3)

$$A_1, A_2, \dots, A_n \rightarrow A_i$$

Trivial Rule

where $i = 1, 2, \dots, n$

Why ?

	A_1	...	A_m	

Armstrong's Rules (1/3)

Transitive Closure Rule

If

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$$

and

$$B_1, B_2, \dots, B_m \rightarrow C_1, C_2, \dots, C_p$$

then

$$A_1, A_2, \dots, A_n \rightarrow C_1, C_2, \dots, C_p$$

Why ?

	A_1	...	A_m		B_1	...	B_m		C_1	...	C_p	

Example (continued)

Start from the following FDs:

1. name \rightarrow color
2. category \rightarrow department
3. color, category \rightarrow price

Infer the following FDs:

Inferred FD	Which Rule did we apply ?
4. name, category \rightarrow name	
5. name, category \rightarrow color	
6. name, category \rightarrow category	
7. name, category \rightarrow color, category	
8. name, category \rightarrow price	

Example (continued)

Answers:

1. name \rightarrow color
2. category \rightarrow department
3. color, category \rightarrow price

Inferred FD	Which Rule did we apply ?
4. name, category \rightarrow name	Trivial rule
5. name, category \rightarrow color	Transitivity on 4, 1
6. name, category \rightarrow category	Trivial rule
7. name, category \rightarrow color, category	Split/combine on 5, 6
8. name, category \rightarrow price	Transitivity on 3, 7

THIS IS TOO HARD ! Let's see an easier way.

Closure of a set of Attributes

Given a set of attributes A_1, \dots, A_n

The **closure**, $\{A_1, \dots, A_n\}^+$ = the set of attributes B
s.t. $A_1, \dots, A_n \rightarrow B$

Example:

name \rightarrow color
category \rightarrow department
color, category \rightarrow price

Closures:

name⁺ = {name, color}

{name, category}⁺ = {name, category, color, department, price}

color⁺ = {color}

Closure Algorithm

$X = \{A_1, \dots, A_n\}$.

Repeat until X doesn't change **do:**

if $B_1, \dots, B_n \rightarrow C$ is a FD **and**
 B_1, \dots, B_n are all in X
then add C to X .

Example:

$\text{name} \rightarrow \text{color}$
 $\text{category} \rightarrow \text{department}$
 $\text{color, category} \rightarrow \text{price}$

$\{\text{name, category}\}^+ =$
 $\{\text{name, category, color, department, price}\}$

Hence: $\text{name, category} \rightarrow \text{color, department, price}$

Example

In class:

$R(A,B,C,D,E,F)$

A, B	\rightarrow	C
A, D	\rightarrow	E
B	\rightarrow	D
A, F	\rightarrow	B

Compute $\{A,B\}^+$ $X = \{A, B, \quad \}$

Compute $\{A, F\}^+$ $X = \{A, F, \quad \}$

Why Do We Need Closure

- With closure we can find all FD's easily
- To check if $X \rightarrow A$
 - Compute X^+
 - Check if $A \in X^+$

Using Closure to Infer ALL FDs

Example:

$$\begin{array}{l} A, B \rightarrow C \\ A, D \rightarrow B \\ B \rightarrow D \end{array}$$

Step 1: Compute X^+ , for every X :

$$A^+ = A, \quad B^+ = BD, \quad C^+ = C, \quad D^+ = D$$
$$AB^+ = ABCD, \quad AC^+ = AC, \quad AD^+ = ABCD,$$
$$BC^+ = BCD, \quad BD^+ = BD, \quad CD^+ = CD$$
$$ABC^+ = ABD^+ = ACD^+ = ABCD \text{ (no need to compute— why ?)}$$
$$BCD^+ = BCD, \quad ABCD^+ = ABCD$$

Step 2: Enumerate all FD's $X \rightarrow Y$, s.t. $Y \subseteq X^+$ and $X \cap Y = \emptyset$:

$$AB \rightarrow CD, \quad AD \rightarrow BC, \quad ABC \rightarrow D, \quad ABD \rightarrow C, \quad ACD \rightarrow B$$

Another Example

- Enrollment(student, major, course, room, time)
student \rightarrow major
major, course \rightarrow room
course \rightarrow time

What else can we infer ? [in class, or at home]

Keys

- A **superkey** is a set of attributes A_1, \dots, A_n s.t. for any other attribute B , we have $A_1, \dots, A_n \rightarrow B$
- A **key** is a minimal superkey
 - I.e. set of attributes which is a superkey and for which no subset is a superkey

Computing (Super)Keys

- Compute X^+ for all sets X
- If $X^+ = \text{all attributes}$, then X is a key
- List only the minimal X 's

Example

Product(name, price, category, color)

name, category \rightarrow price
category \rightarrow color

What is the key ?

Example

Product(name, price, category, color)

name, category \rightarrow price
category \rightarrow color

What is the key ?

(name, category) + = name, category, price, color

Hence (name, category) is a key

Examples of Keys

Enrollment(student, address, course, room, time)

student \rightarrow address

room, time \rightarrow course

student, course \rightarrow room, time

(find keys at home)

Eliminating Anomalies

Main idea:

- $X \rightarrow A$ is OK if X is a (super)key
- $X \rightarrow A$ is not OK otherwise

Example

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

SSN \rightarrow Name, City

What the key?

{SSN, PhoneNumber}

Hence SSN \rightarrow Name, City
is a “bad” dependency

Key or Keys ?

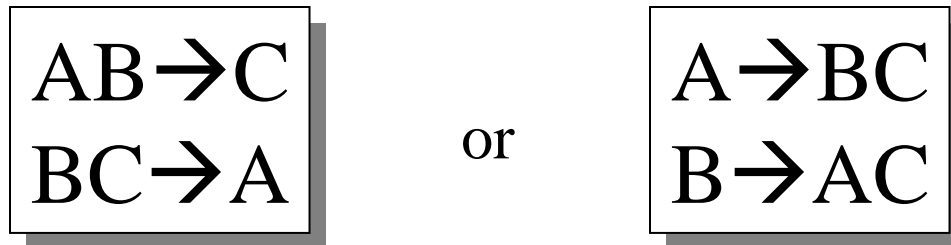
Can we have more than one key ?

Given $R(A,B,C)$ define FD's s.t. there are two or more keys

Key or Keys ?

Can we have more than one key ?

Given $R(A,B,C)$ define FD's s.t. there are two or more keys



what are the keys here ?

Can you design FDs such that there are *three* keys ?

Boyce-Codd Normal Form

A simple condition for removing anomalies from relations:

A relation R is in BCNF if:

If $A_1, \dots, A_n \rightarrow B$ is a non-trivial dependency in R , then $\{A_1, \dots, A_n\}$ is a superkey for R

In other words: there are no “bad” FDs

Equivalently:

$\forall X$, either $(X^+ = X)$ or $(X^+ = \text{all attributes})$

BCNF Decomposition Algorithm

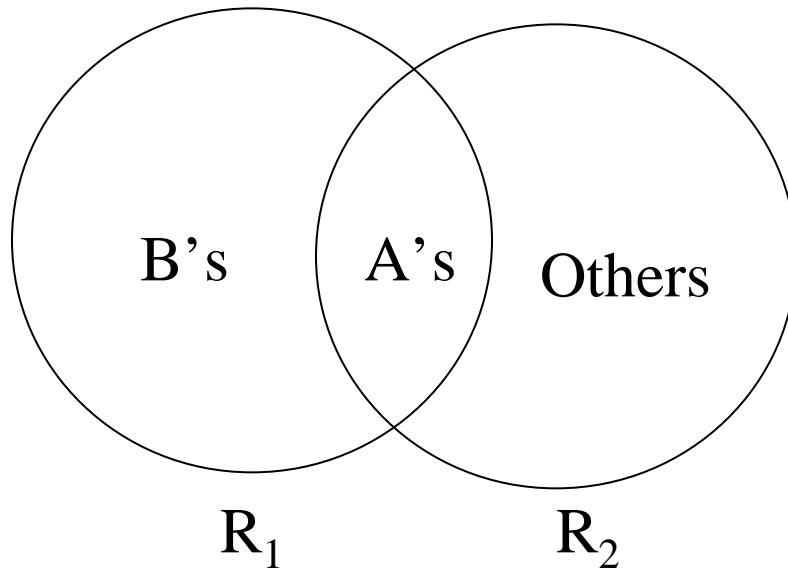
repeat

choose $A_1, \dots, A_m \rightarrow B_1, \dots, B_n$ that violates BCNF

split R into $R_1(A_1, \dots, A_m, B_1, \dots, B_n)$ and $R_2(A_1, \dots, A_m, [\text{others}])$

continue with both R_1 and R_2

until no more violations



Is there a
2-attribute
relation that is
not in BCNF ?

In practice, we have
a better algorithm (coming⁴³ up)

Example

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

SSN → Name, City

What the key?

{SSN, PhoneNumber}

use SSN → Name, City
to split

Example

<u>Name</u>	<u>SSN</u>	<u>City</u>
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield

SSN → Name, City

<u>SSN</u>	<u>PhoneNumber</u>
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121
987-65-4321	908-555-1234

Let's check anomalies:

- Redundancy ?
- Update ?
- Delete ?

Example Decomposition

Person(name, SSN, age, hairColor, phoneNumber)

SSN \rightarrow name, age

age \rightarrow hairColor

Decompose in BCNF (in class):

BCNF Decomposition Algorithm

BCNF_Decompose(R)

find X s.t.: $X \neq X^+ \neq$ [all attributes]

if (not found) **then** “R is in BCNF”

let $Y = X^+ - X$

let $Z =$ [all attributes] $- X^+$

decompose R into $R_1(X \cup Y)$ and $R_2(X \cup Z)$

continue to decompose recursively R_1 and R_2

Find X s.t.: $X \neq X^+ \neq$ [all attributes]

Example BCNF Decomposition

Person(name, SSN, age, hairColor, phoneNumber)

SSN \rightarrow name, age

age \rightarrow hairColor

Iteration 1: Person

SSN⁺ = SSN, name, age, hairColor

Decompose into: P(SSN, name, age, hairColor)

Phone(SSN, phoneNumber)

Iteration 2: P

age⁺ = age, hairColor

Decompose: People(SSN, name, age)

Hair(age, hairColor)

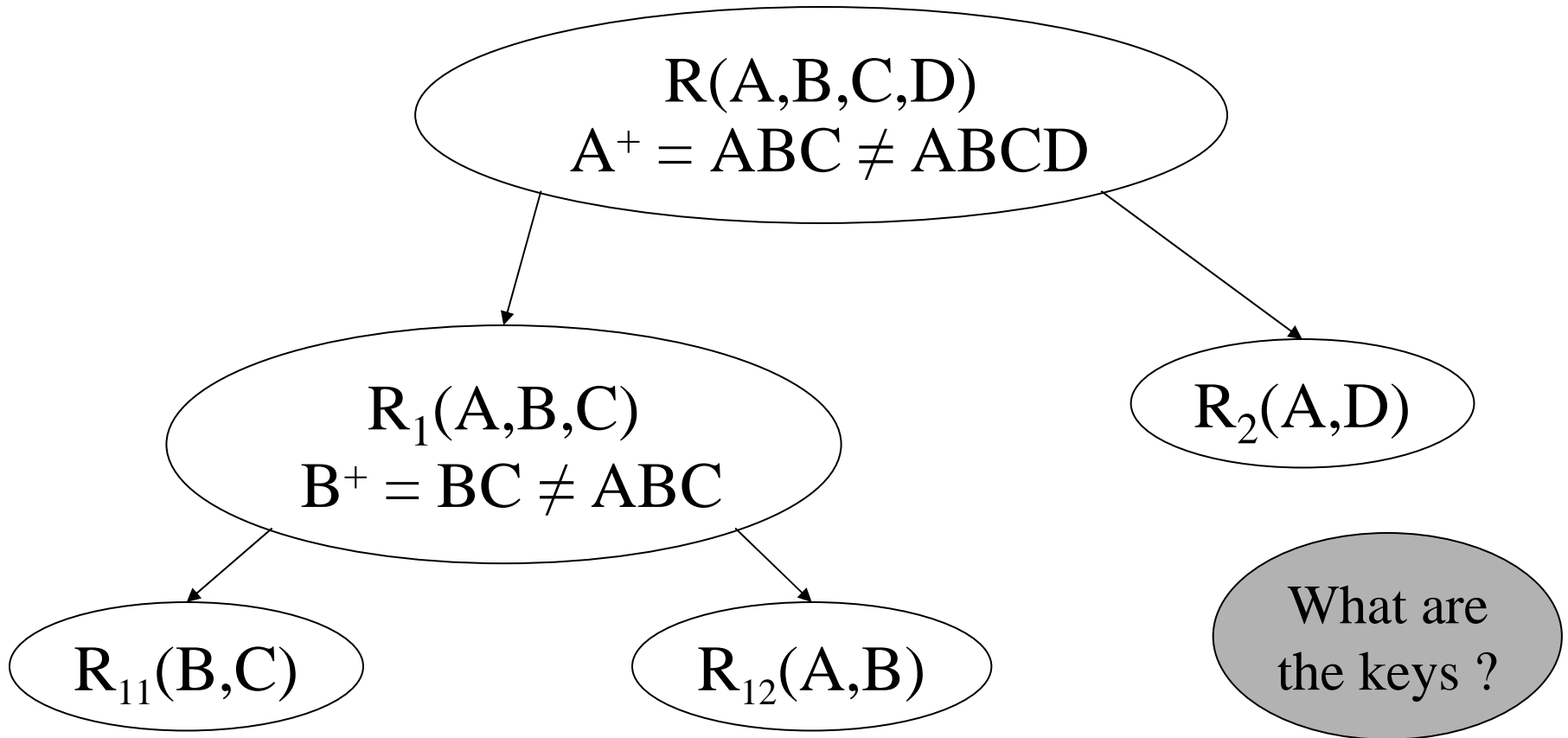
Phone(SSN, phoneNumber)

What are
the keys ?

R(A,B,C,D)

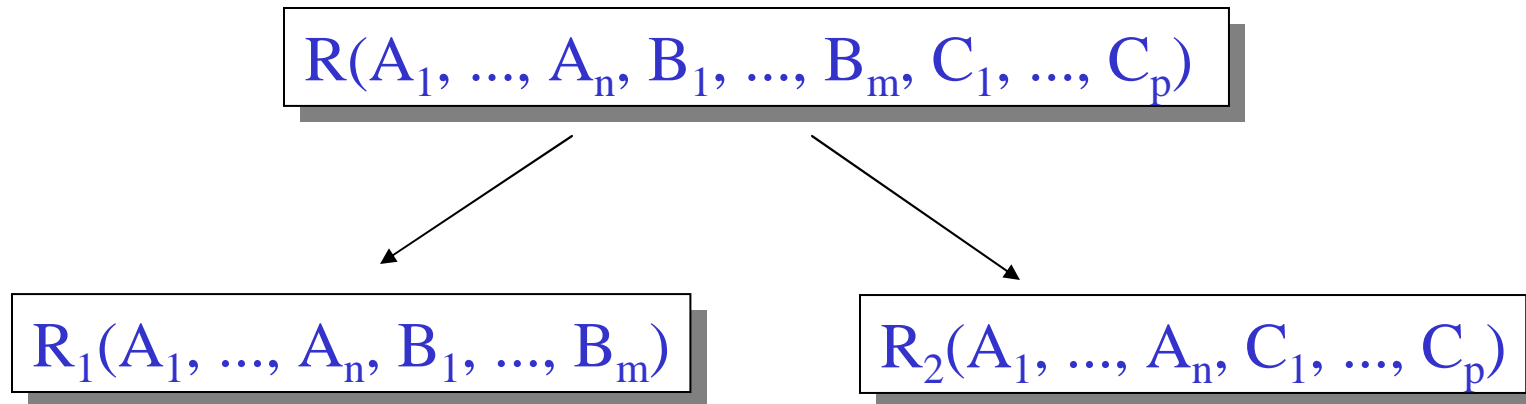
A → B
B → C

Example



What happens if in R we first pick B^+ ? Or AB^+ ?

Decompositions in General




R_1 = projection of R on $A_1, \dots, A_n, B_1, \dots, B_m$

R_2 = projection of R on $A_1, \dots, A_n, C_1, \dots, C_p$

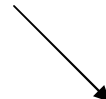
Theory of Decomposition

- Sometimes it is correct:

Name	Price	Category
Gizmo	19.99	Gadget
OneClick	24.99	Camera
Gizmo	19.99	Camera



Name	Price
Gizmo	19.99
OneClick	24.99
Gizmo	19.99



Name	Category
Gizmo	Gadget
OneClick	Camera
Gizmo	Camera

Lossless decomposition

Incorrect Decomposition

- Sometimes it is not:

Name	Price	Category
Gizmo	19.99	Gadget
OneClick	24.99	Camera
Gizmo	19.99	Camera

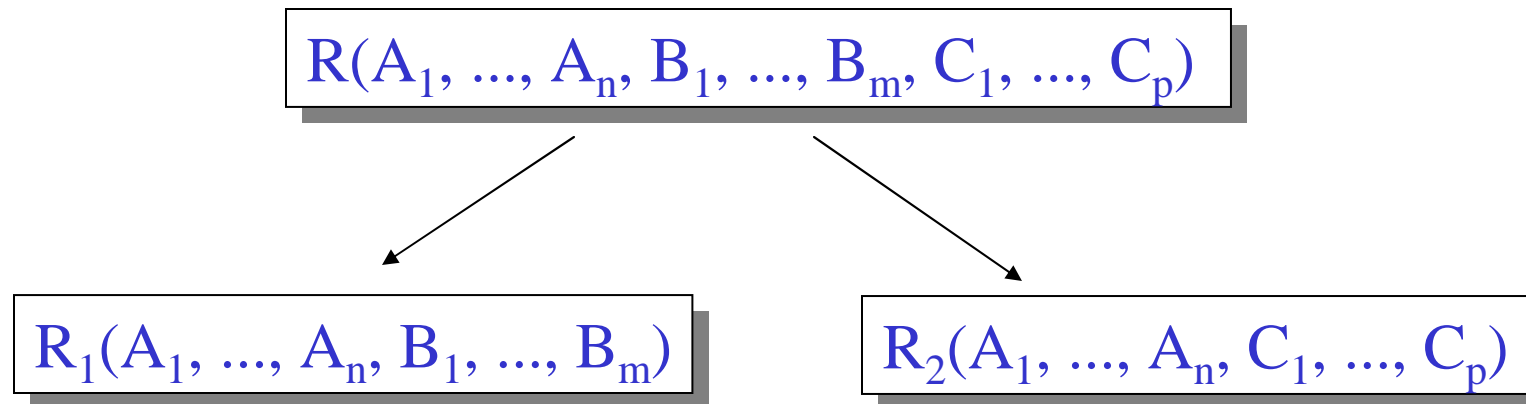
What's incorrect ??

Name	Category
Gizmo	Gadget
OneClick	Camera
Gizmo	Camera

Price	Category
19.99	Gadget
24.99	Camera
19.99	Camera

Lossy decomposition

Decompositions in General



If $A_1, \dots, A_n \rightarrow B_1, \dots, B_m$
Then the decomposition is lossless

Note: don't need $A_1, \dots, A_n \rightarrow C_1, \dots, C_p$

BCNF decomposition is always lossless. WHY ?