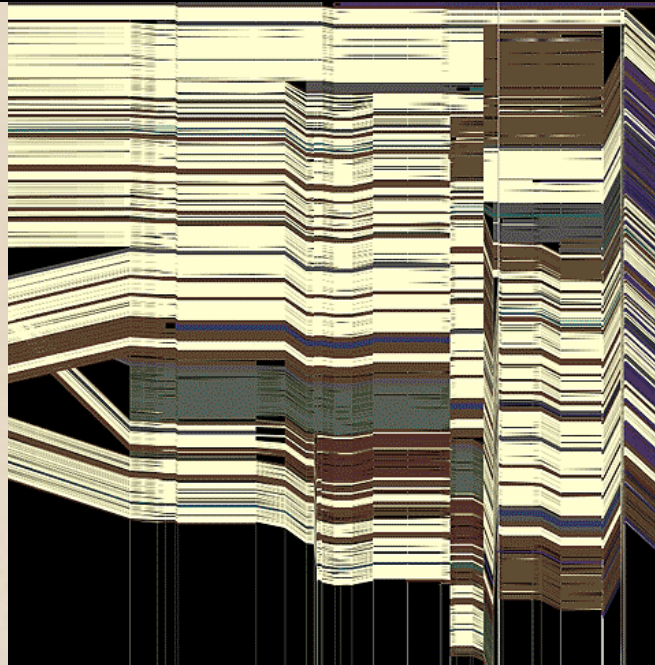
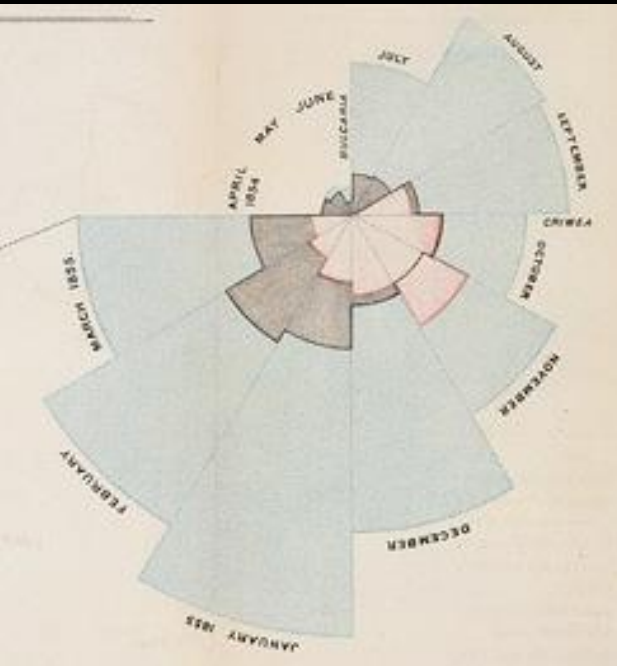


CSE 442 - Data Visualization

Color



Leilani Battle University of Washington

Purpose of Color

To label

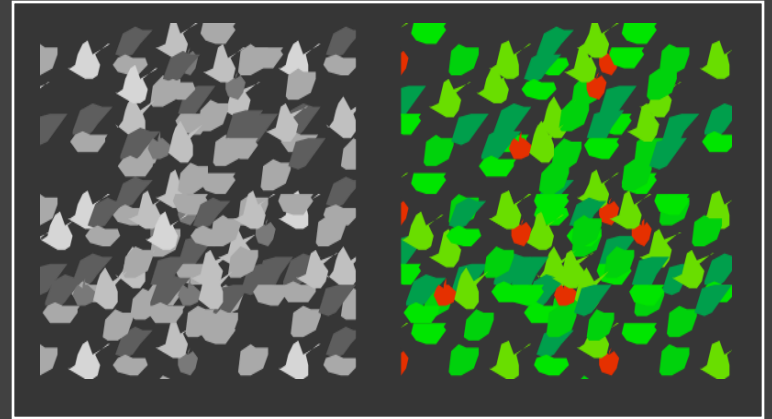
To measure

To represent and imitate

To enliven and decorate

“Above all, do no harm.”

- Edward Tufte



Learning Goals

How is color defined in visualization?

How do we reason about color:
as rendered within media?
as perceived by the human eye?

What are useful rules of thumb for applying color in visualizations?

Topics

Perception of Color

Light

Visual system – Cone Response, Opponent Signals

Mental models – Perception, Appearance, Cognition

Color in Information Visualization

Categorical & Quantitative encoding

Guidelines for color palette design

Perception of Color

What color is this?

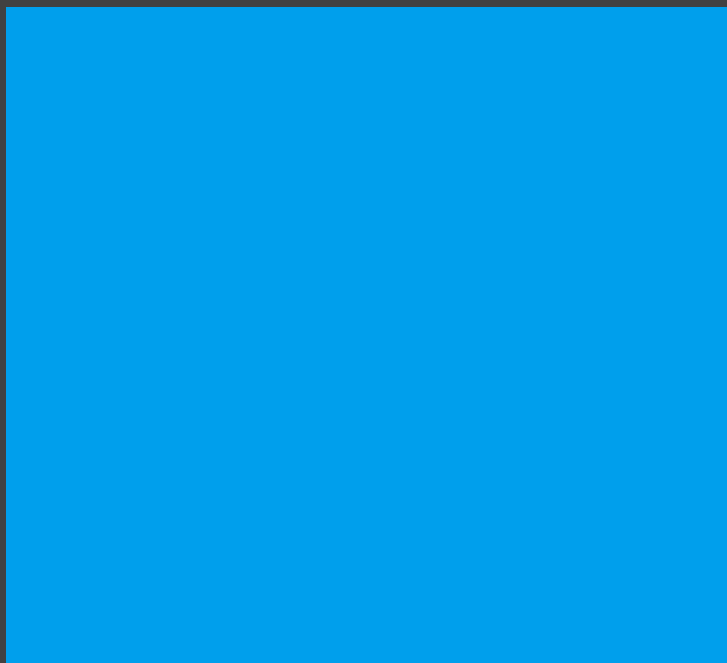


What color is this?



“Yellow”

What color is this?



What color is this?



“Blue”

What color is this?

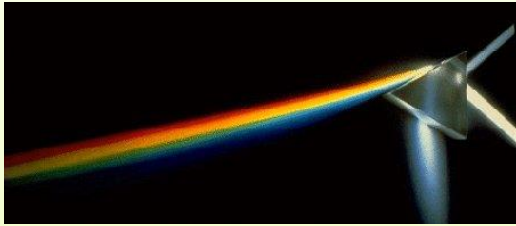


What color is this?

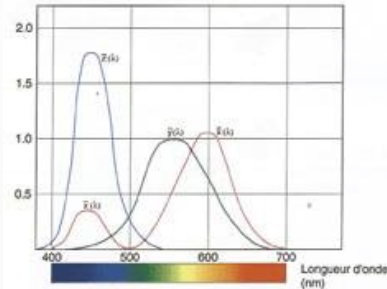


“Teal” ?

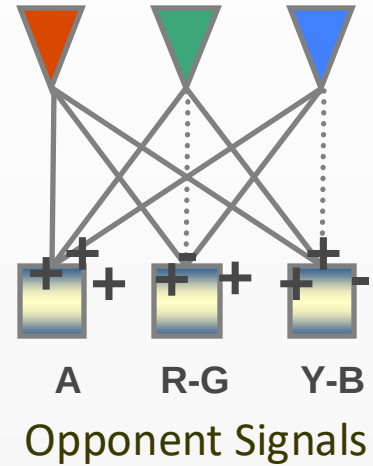
Perception of Color



Light



Cone Response



Opponent Signals

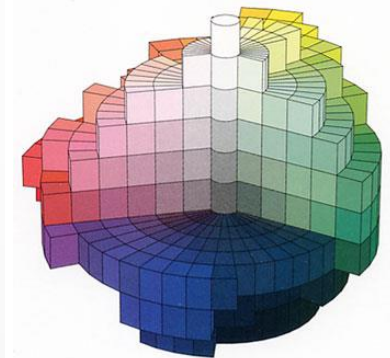
“Yellow”

Color Cognition



Mark D. Fairchild
**COLOR APPEARANCE
MODELS**

Color Appearance



Color Perception

Physicist's View

Light as electromagnetic waves

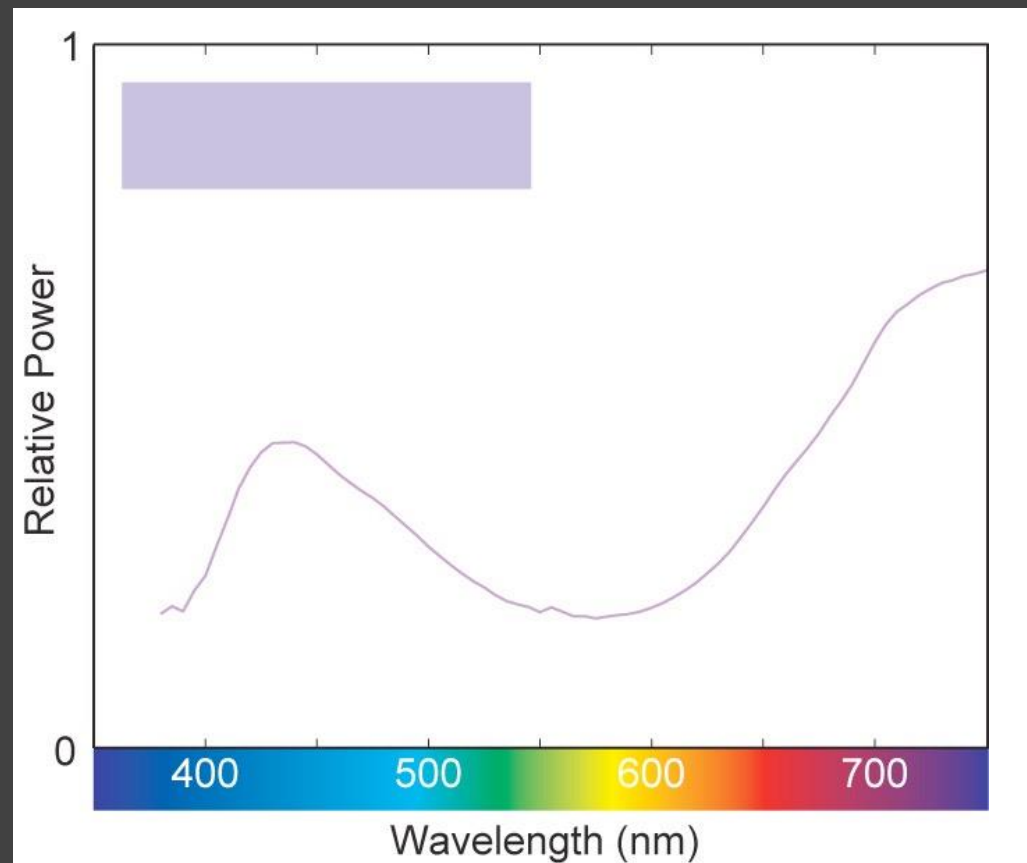
Wavelength

Visible spectrum is

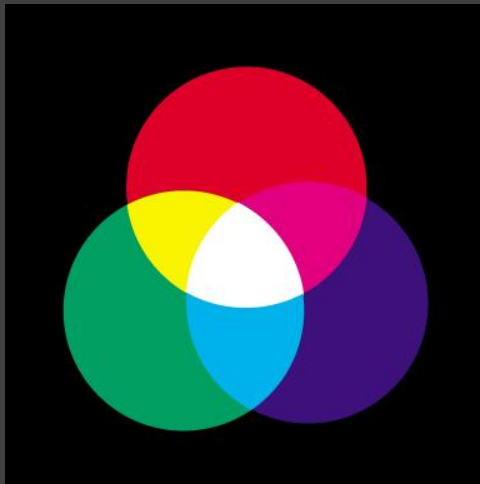
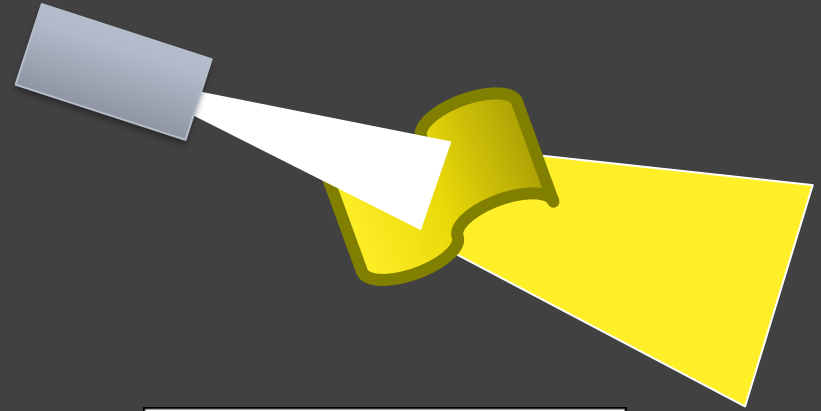
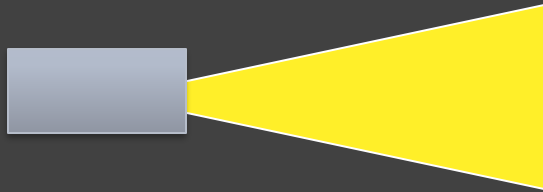
370-730 nm

Power or

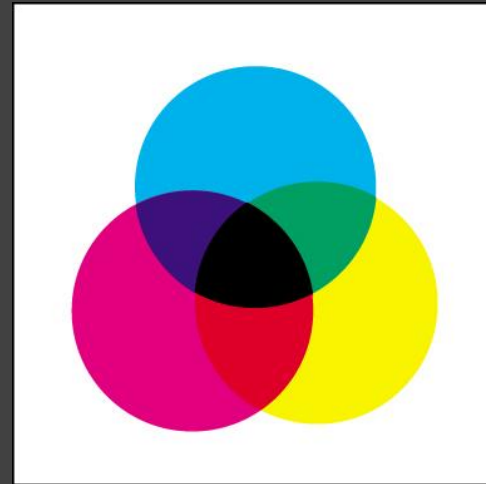
“Relative luminance”



Emissive vs. Reflective Light

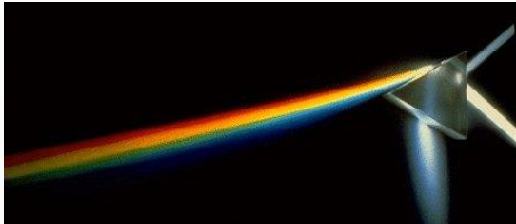


Additive
(digital displays)

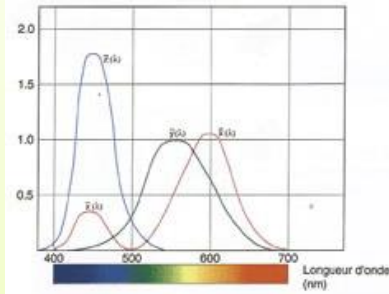


Subtractive
(print, e-paper)

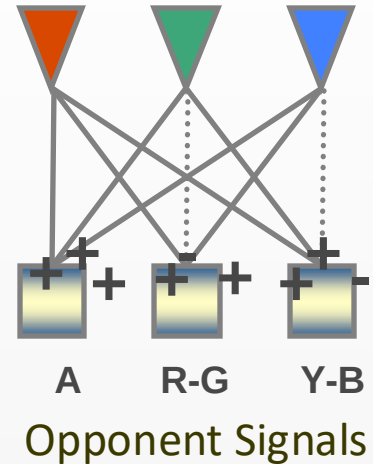
Perception of Color



Light



Cone Response



Opponent Signals

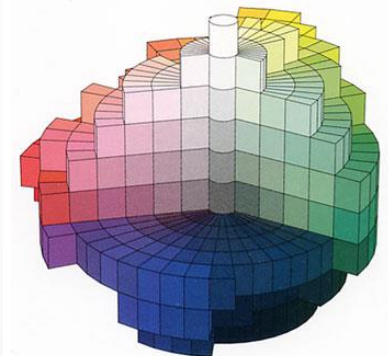
“Yellow”

Color Cognition



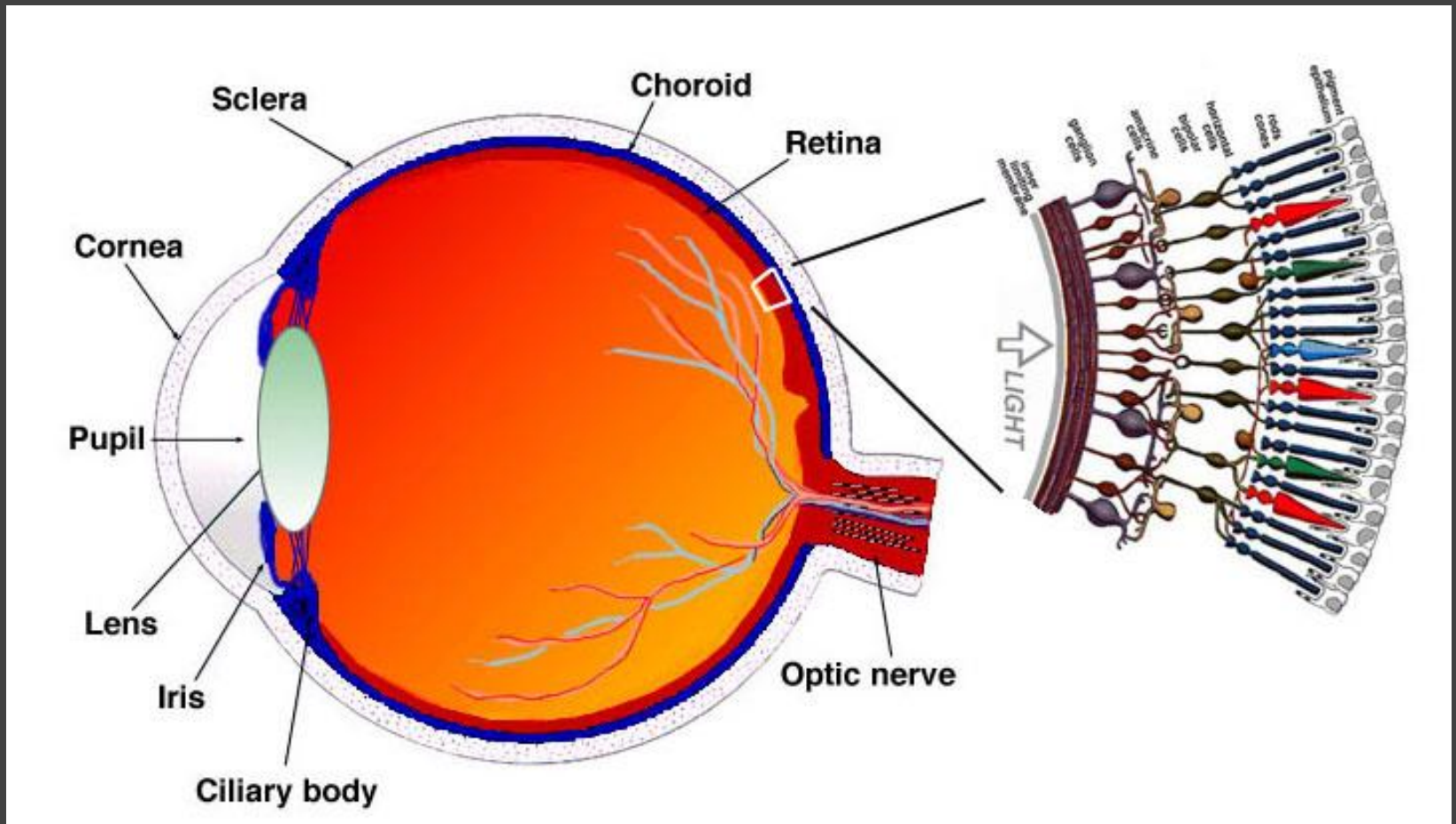
Mark D. Fairchild
**COLOR APPEARANCE
MODELS**

Color Appearance



Color Perception

Retina

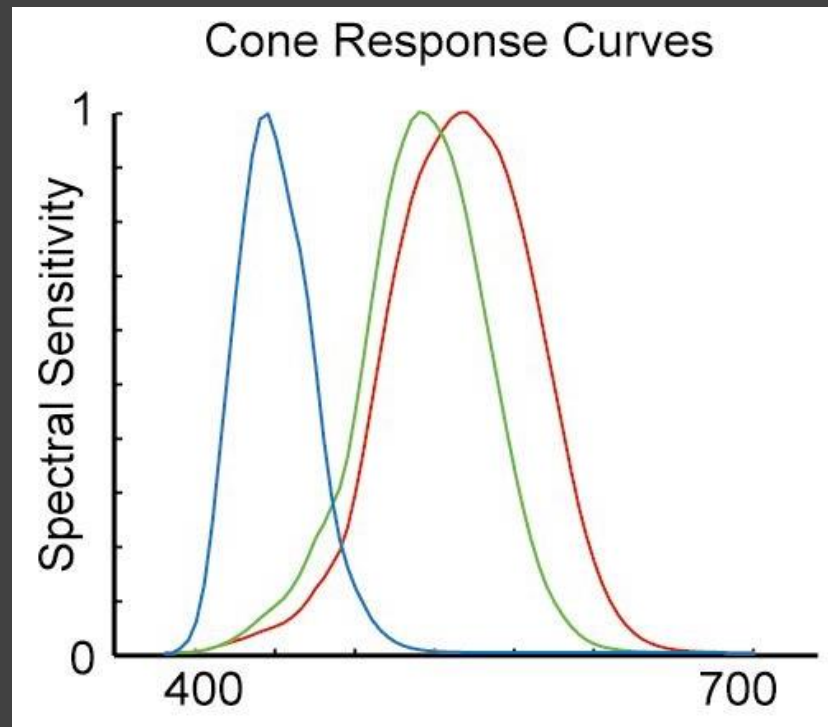


Simple Anatomy of the Retina, Helga Kolb

As light enters our retina...

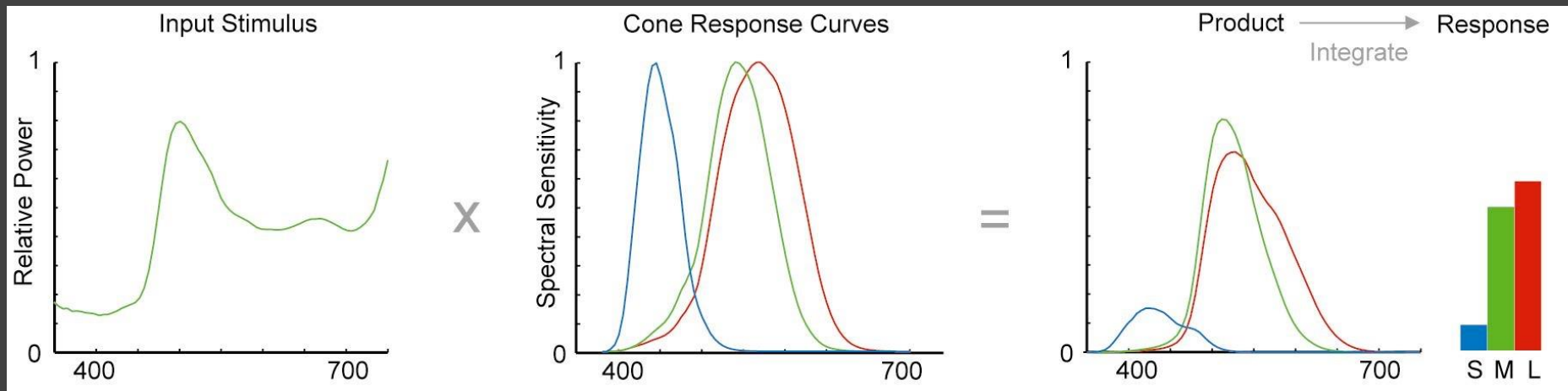
LMS (Long, Middle, Short) Cones

Sensitive to different wavelengths



As light enters our retina...

LMS (Long, Middle, Short) Cones
Sensitive to different wavelengths
Integration with input stimulus



Effects of Retina Encoding

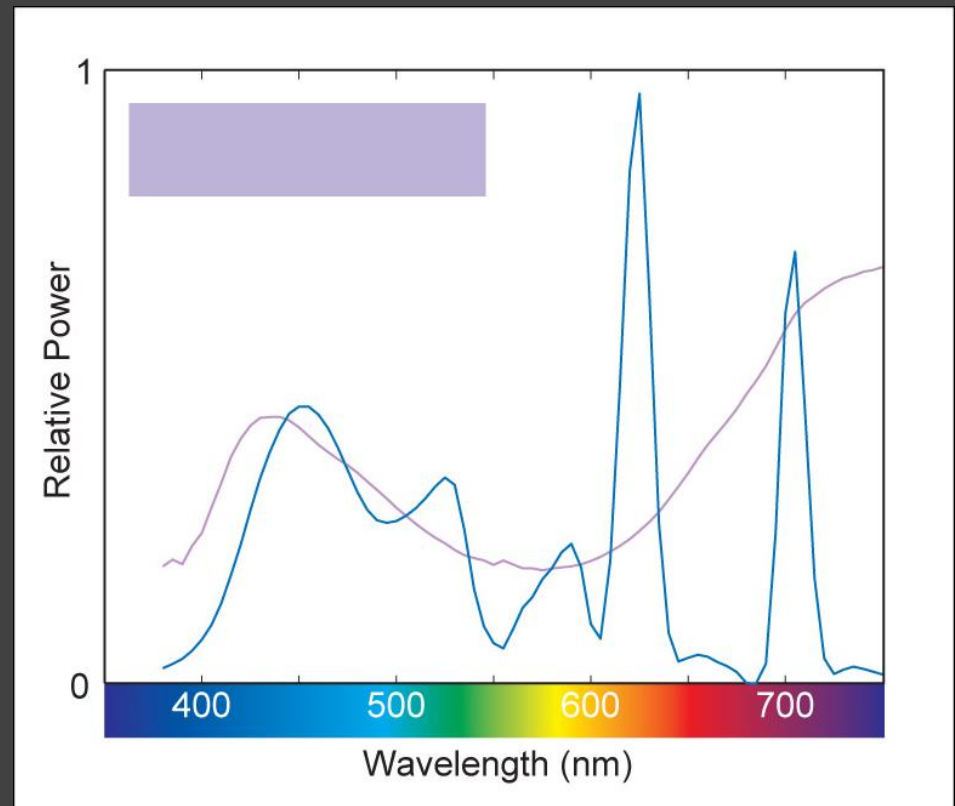
Spectra that stimulate the same LMS response are indistinguishable (a.k.a. “metamers”).

“Tri-stimulus”

Computer displays

Digital scanners

Digital cameras



We Use Color Spaces to Express Color Ranges

Color spaces allow us to capture, index, and enumerate colors perceived by the human eye.

Given a set of input parameters, we can extract the corresponding color from the color space

We can also plot the color space to see its organization and relationships between colors

Color Spaces of Interest

CIE XYZ

HSL / RGB

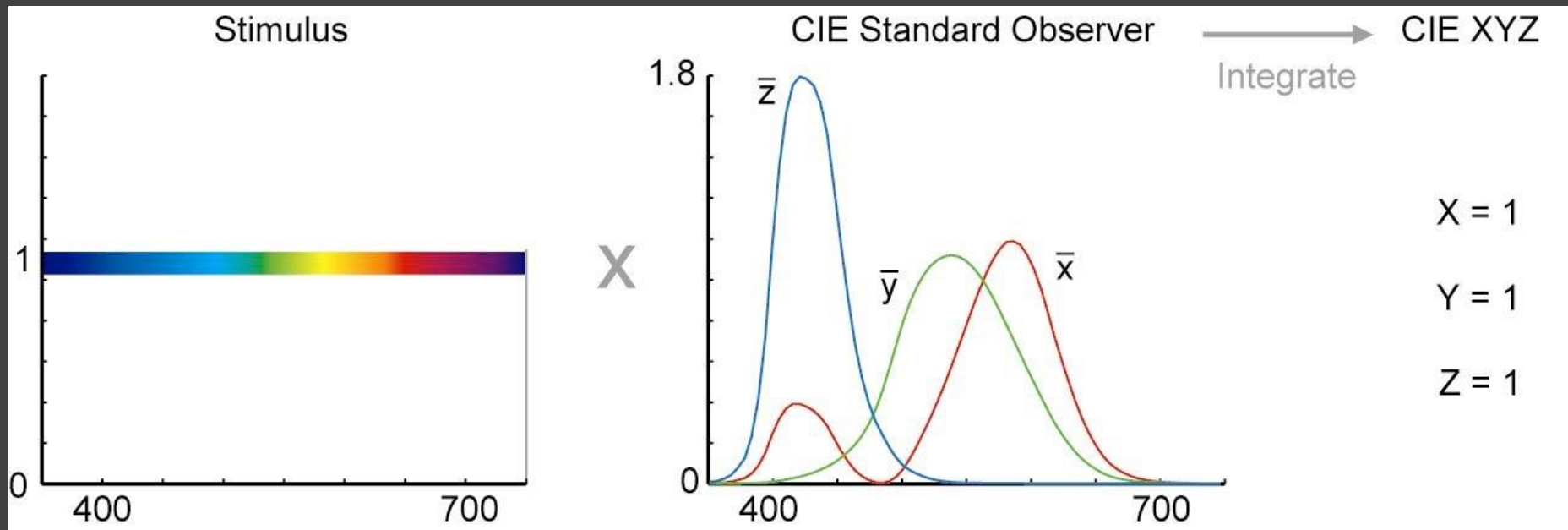
CIE LAB / CIE LUV

Munsell Color System

CIE XYZ Color Space

Standardized in 1931 to mathematically represent tri-stimulus response from cones on the retina.

“Standard observer” response curves

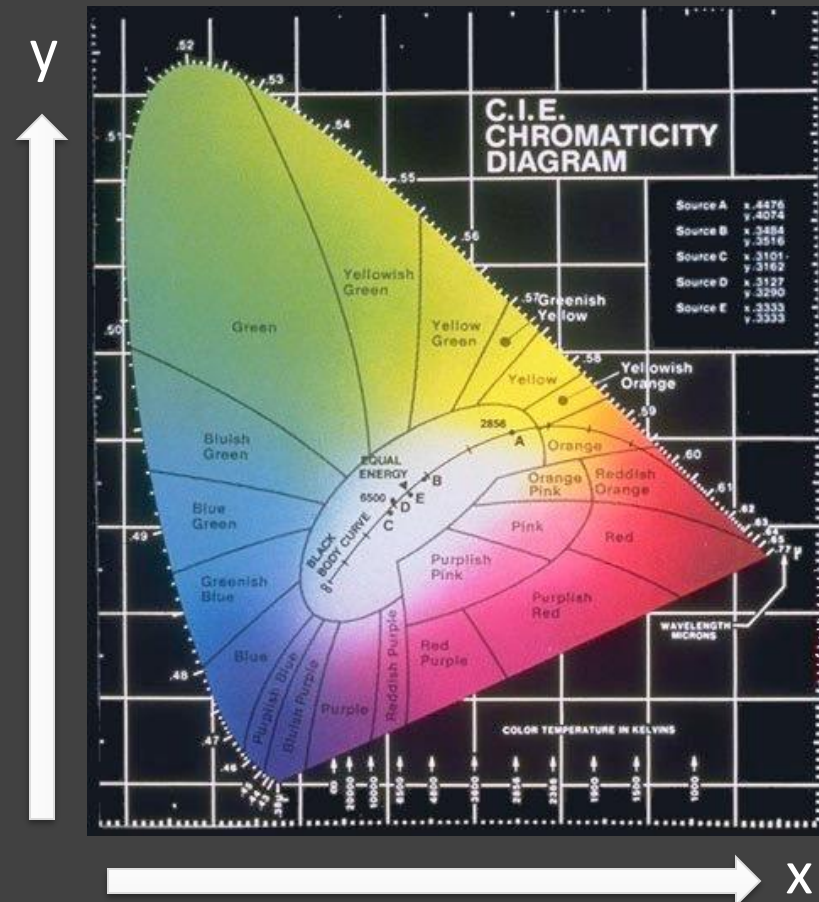


CIE Chromaticity Diagram

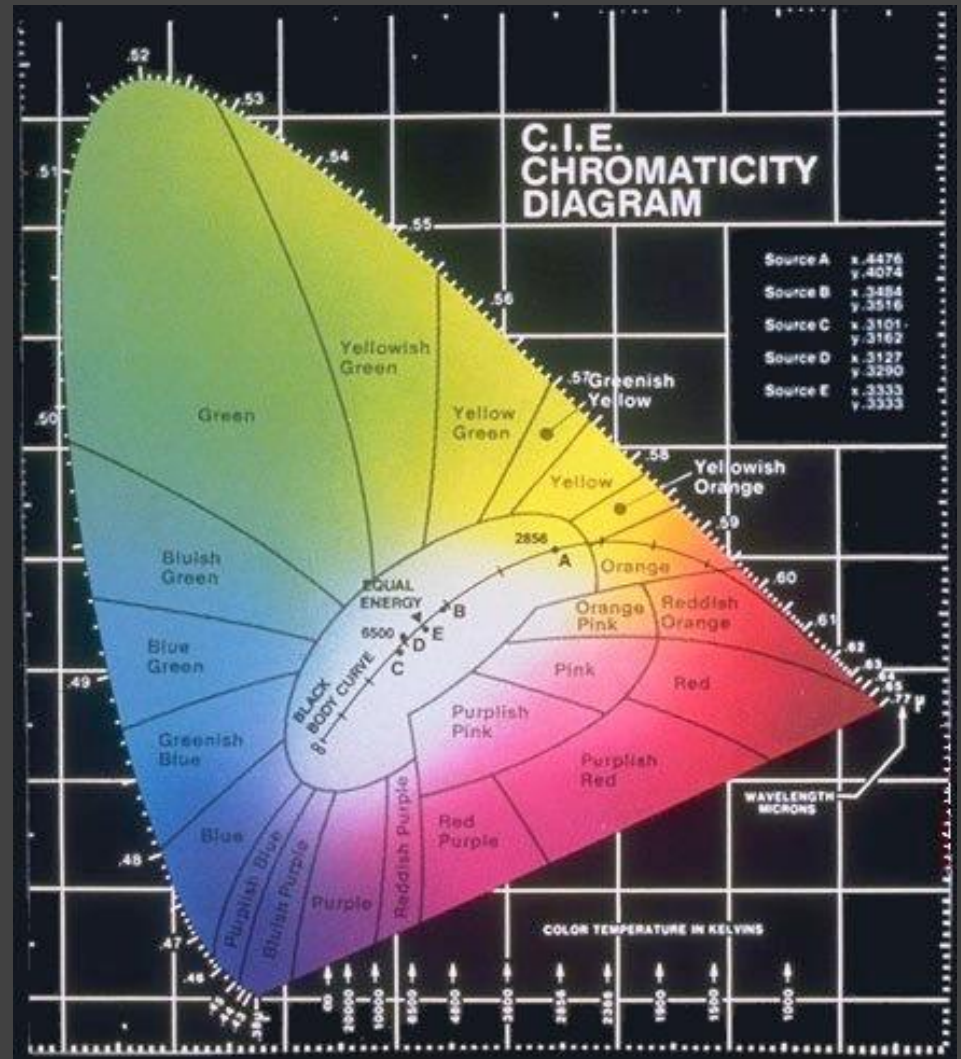
Colorfulness vs. Brightness

$$x = X / (X+Y+Z)$$

$$y = Y / (X+Y+Z)$$

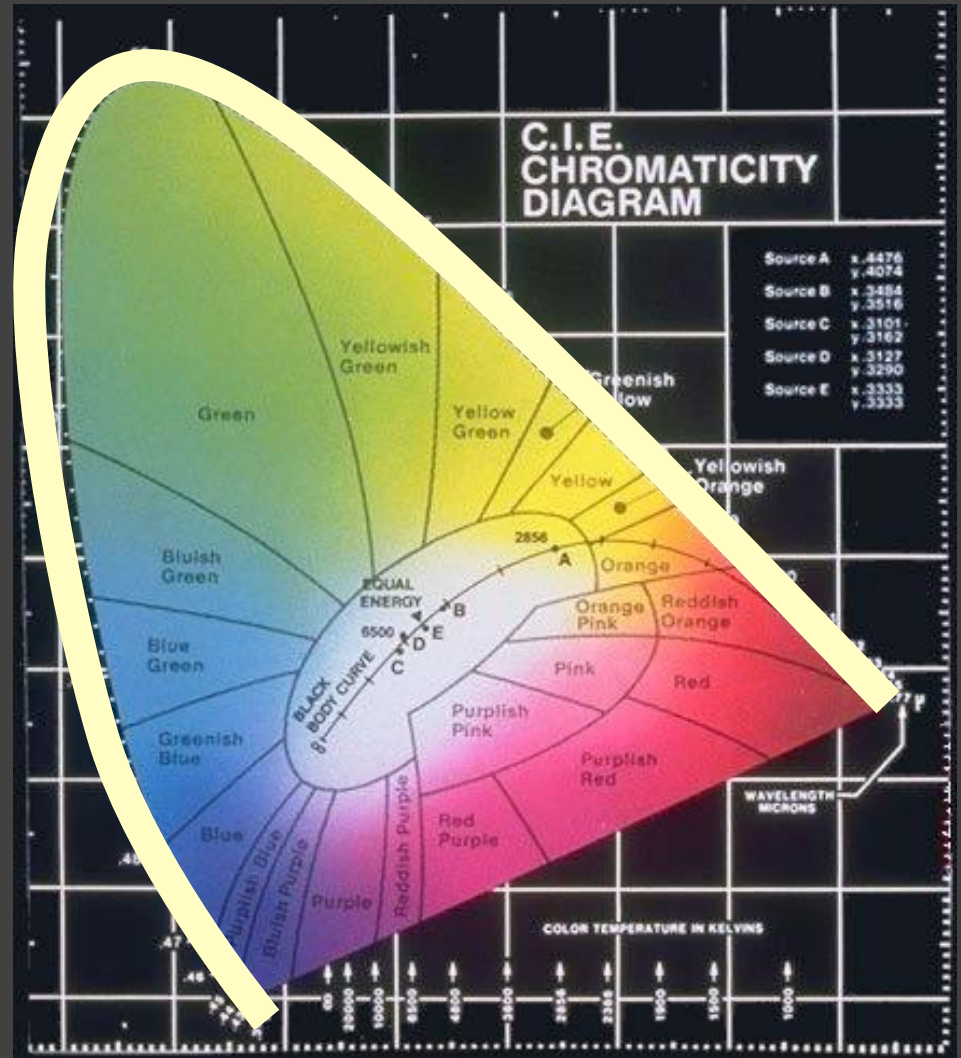


CIE Chromaticity Diagram



CIE Chromaticity Diagram

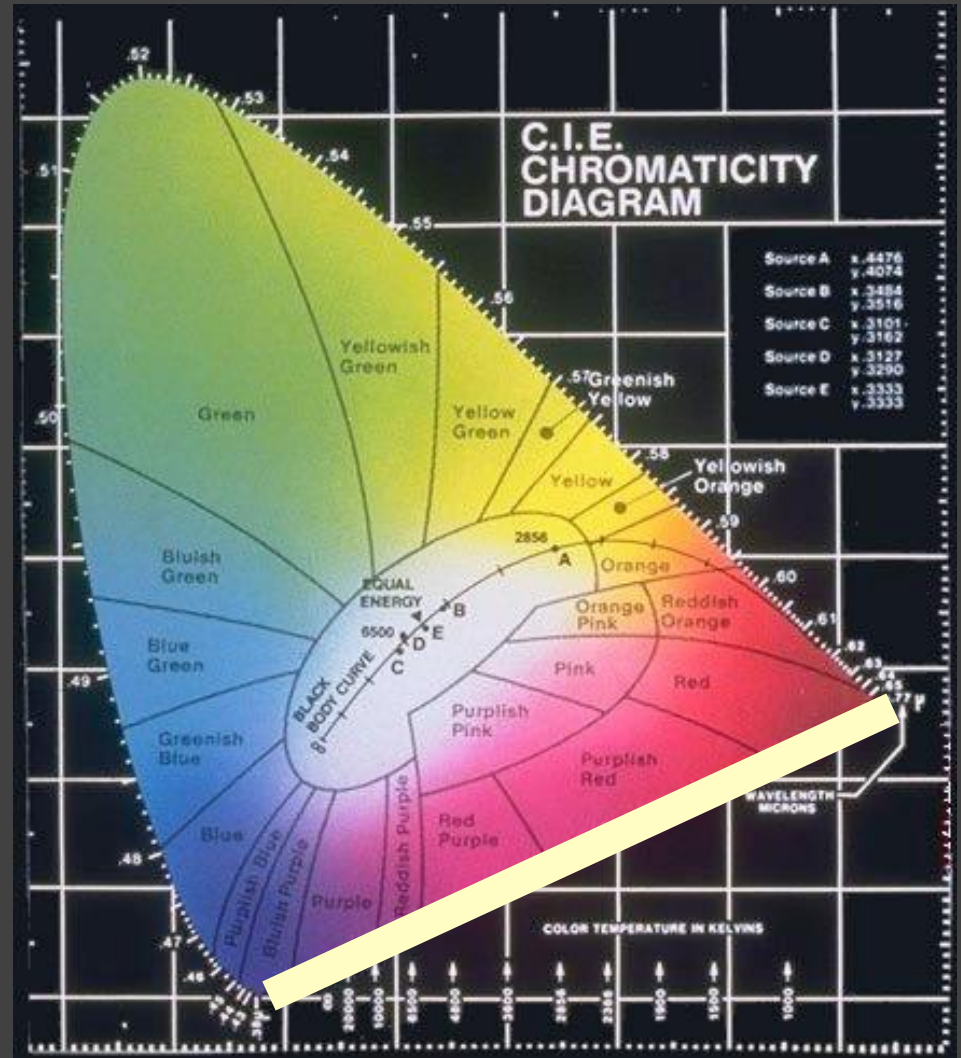
Spectrum locus



CIE Chromaticity Diagram

Spectrum locus

Purple line

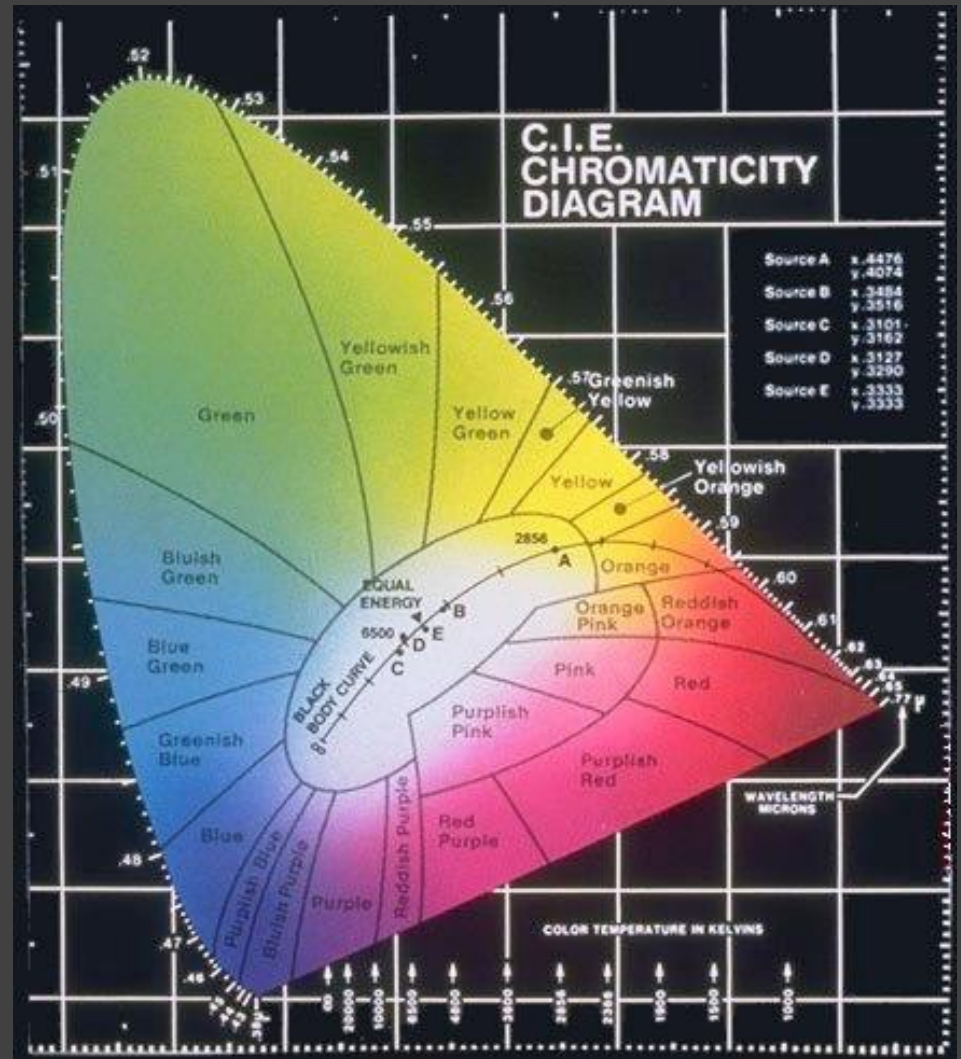


CIE Chromaticity Diagram

Spectrum locus

Purple line

Mixture of two
lights appears as a
straight line.

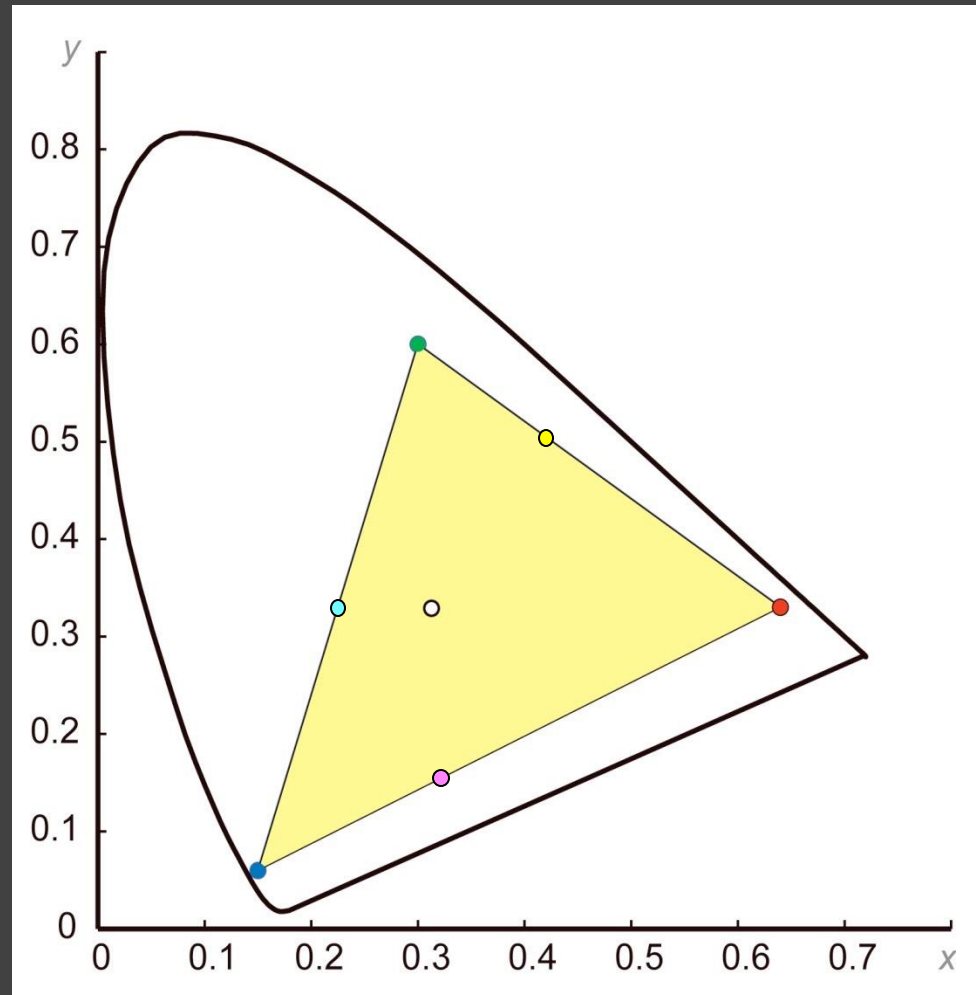


Display Gamuts

Typically defined by:

3 Colorants

Convex region



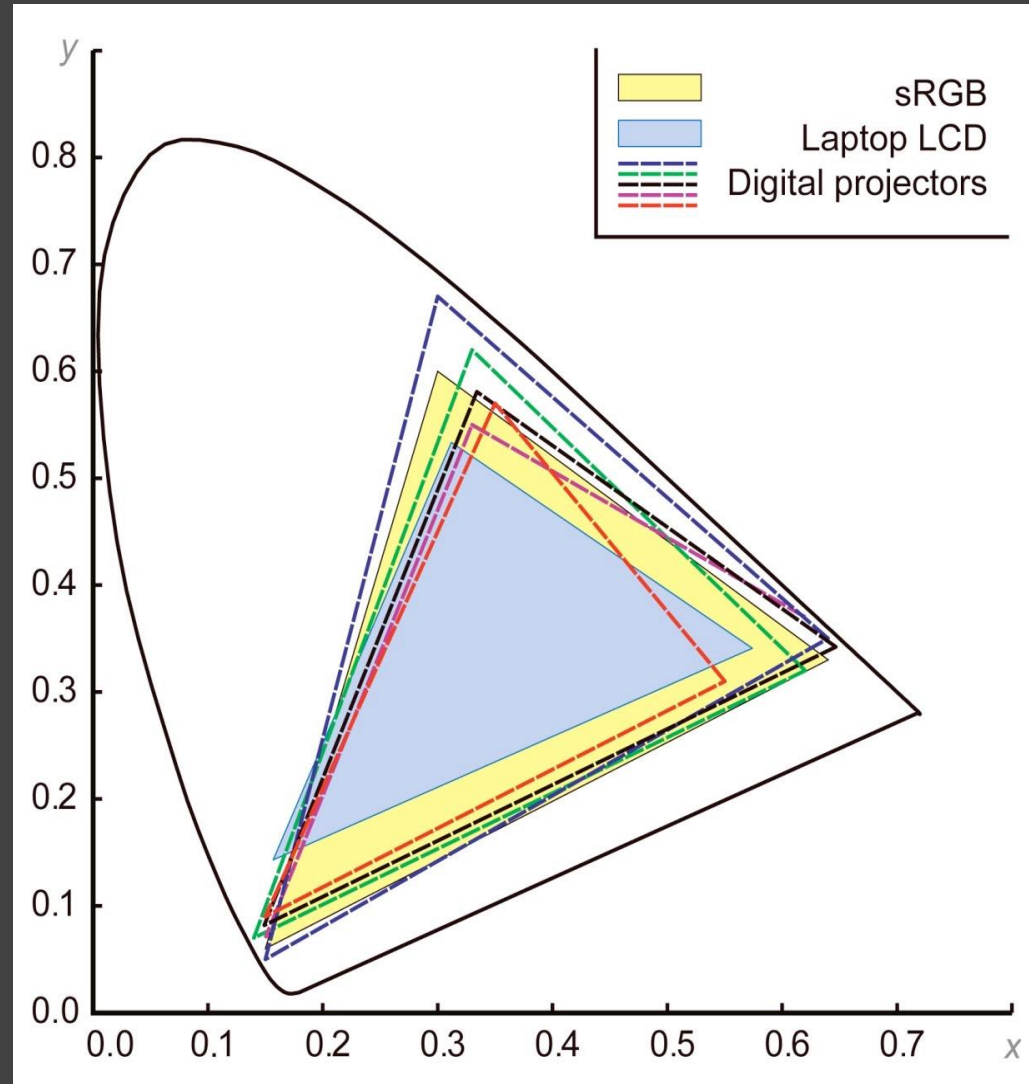
Display Gamuts

Deviations from sRGB specification

Example:

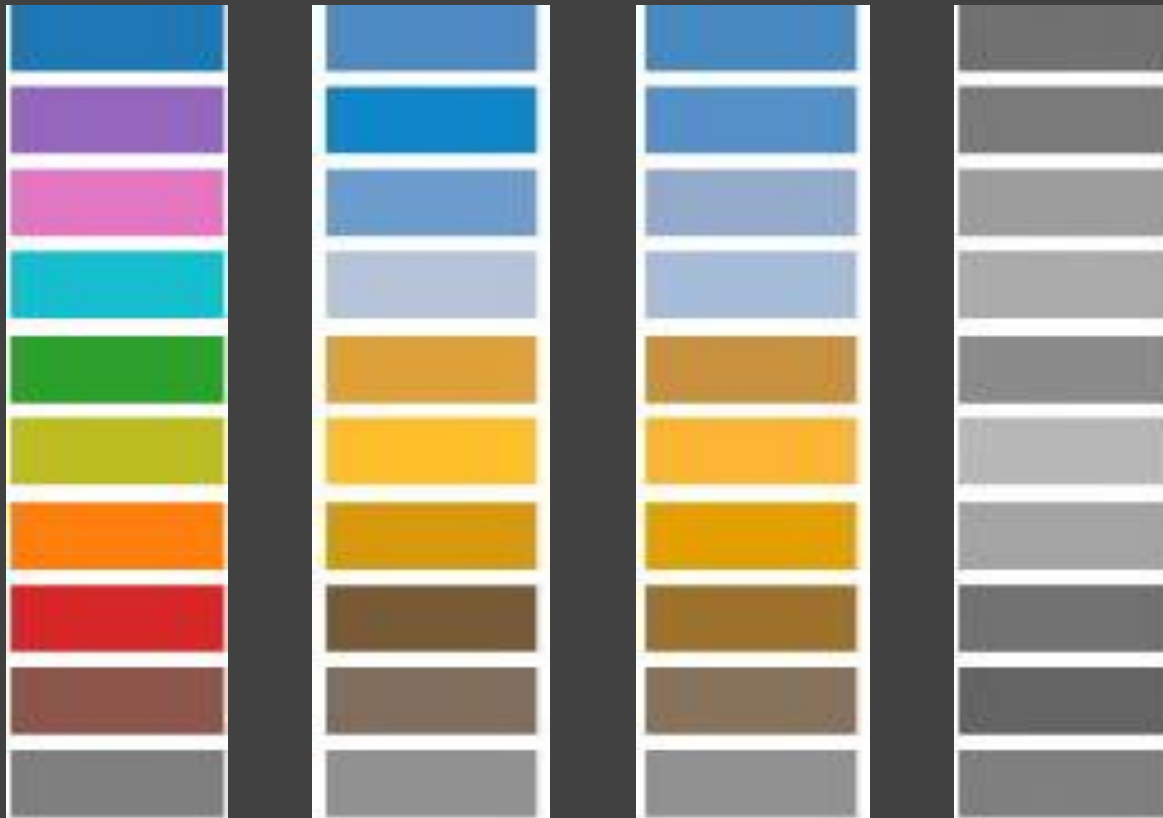
(R, G, B) coordinates ranging from 0-255.

Displays may produce different colors for a coord!



Color Vision Deficiency (CVD)

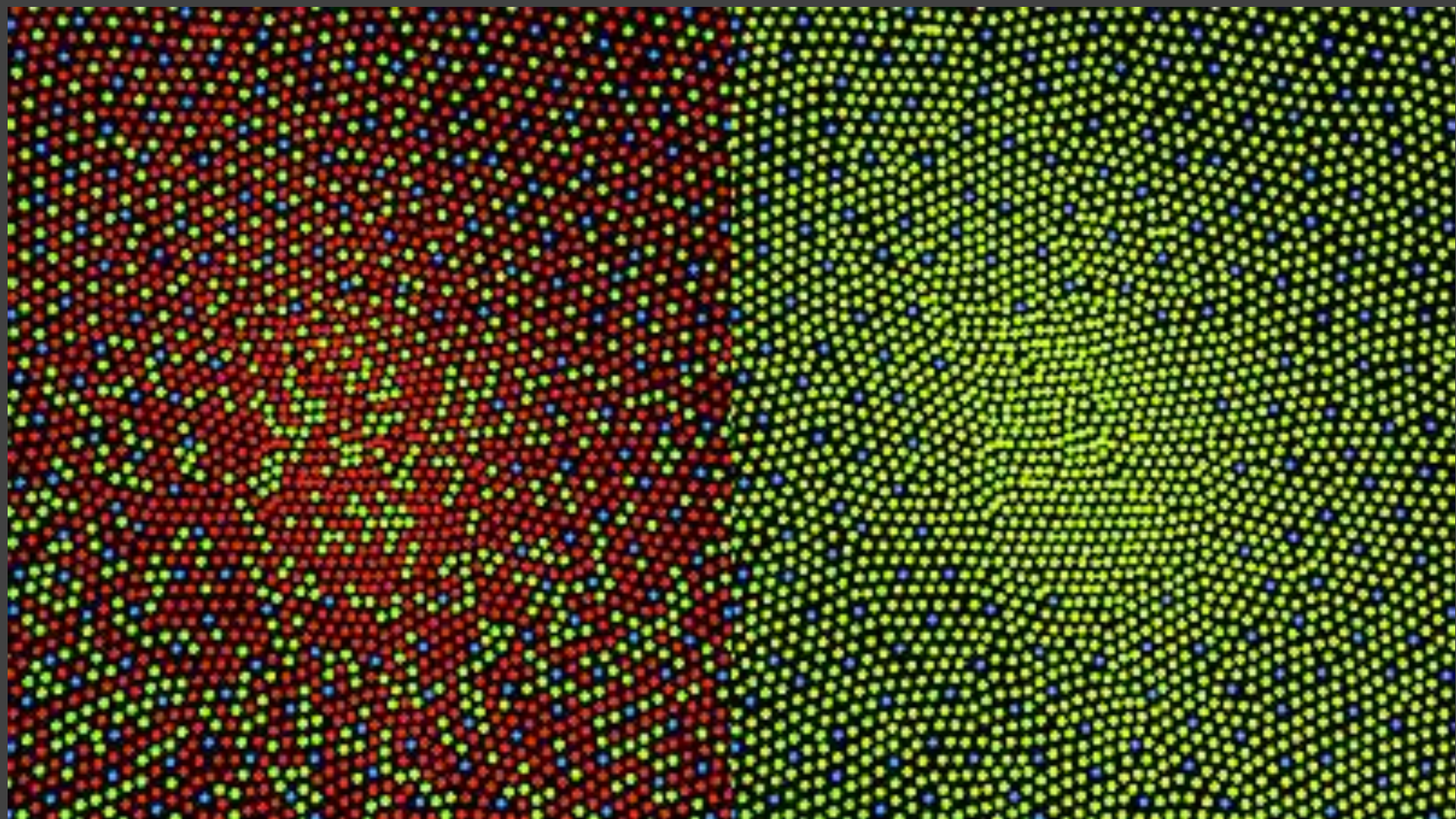
Missing one or more cones or rods in retina.



Protanope

Deuteranope

Luminance



Normal Retina

Protanopia

Color Vision Simulators

Simulate color vision deficiencies

Browser plug-ins

Photoshop plug-ins, etc.



Deuteranope

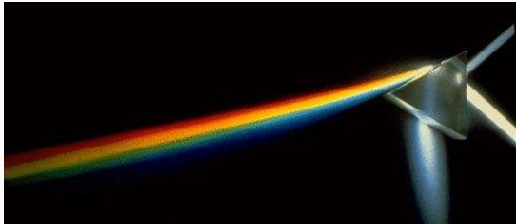


Protanope

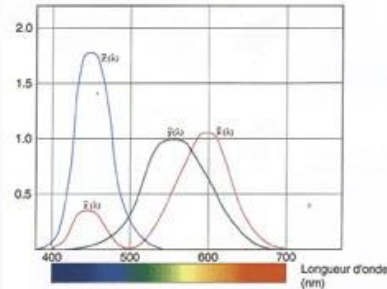


Tritanope

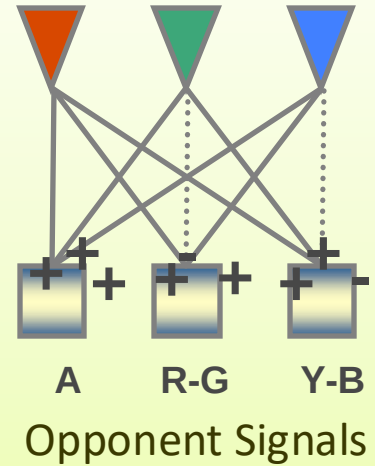
Perception of Color



Light



Cone Response



Opponent Signals

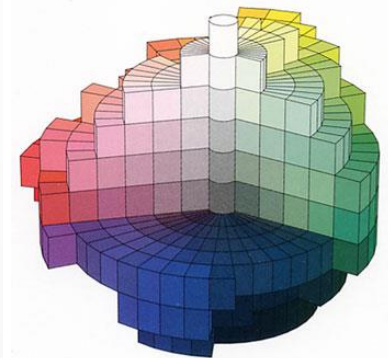
“Yellow”

Color Cognition



Mark D. Fairchild
**COLOR APPEARANCE
MODELS**

Color Appearance



Color Perception

Primary Colors

To paint “all colors”:

Leonardo da Vinci, circa 1500 described in his notebooks
a list of simple colors...

Yellow

Blue

Green

Red

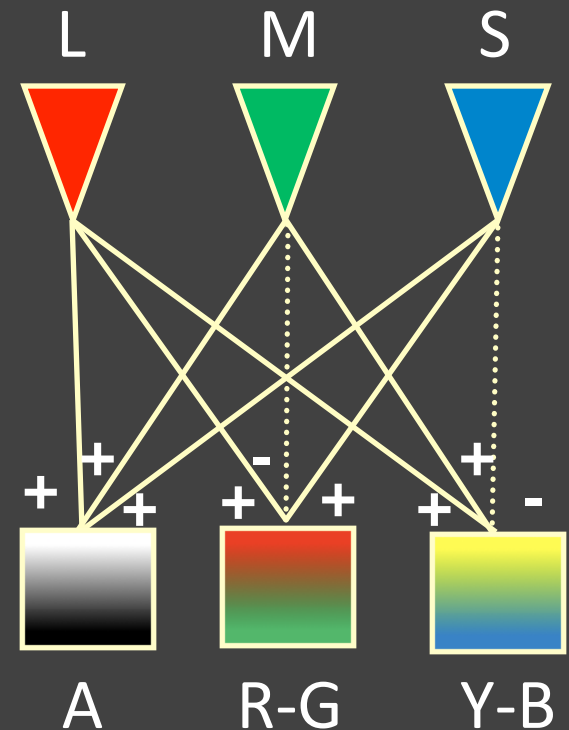
Opponent Processing

LMS are combined to create:

Lightness

Red-green contrast

Yellow-blue contrast



[Fairchild]

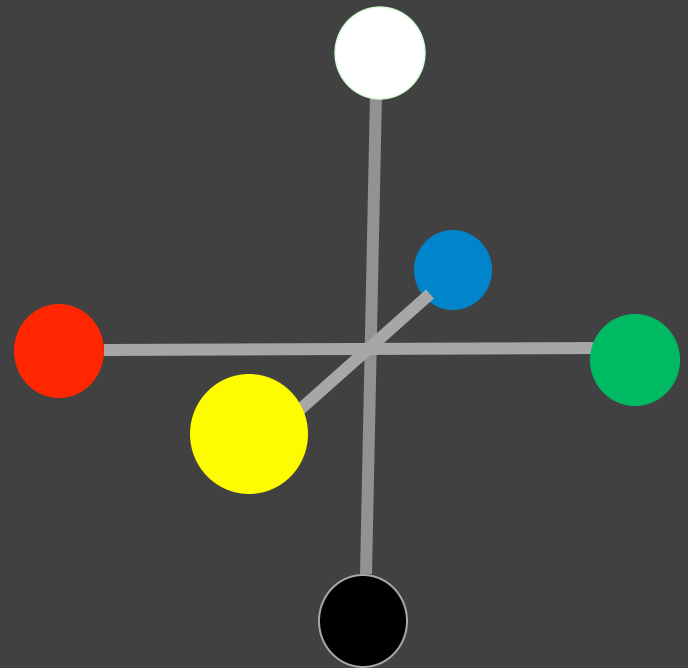
Opponent Processing

LMS are combined to create:

Lightness

Red-green contrast

Yellow-blue contrast



Opponent Processing

LMS are combined to create:

Lightness

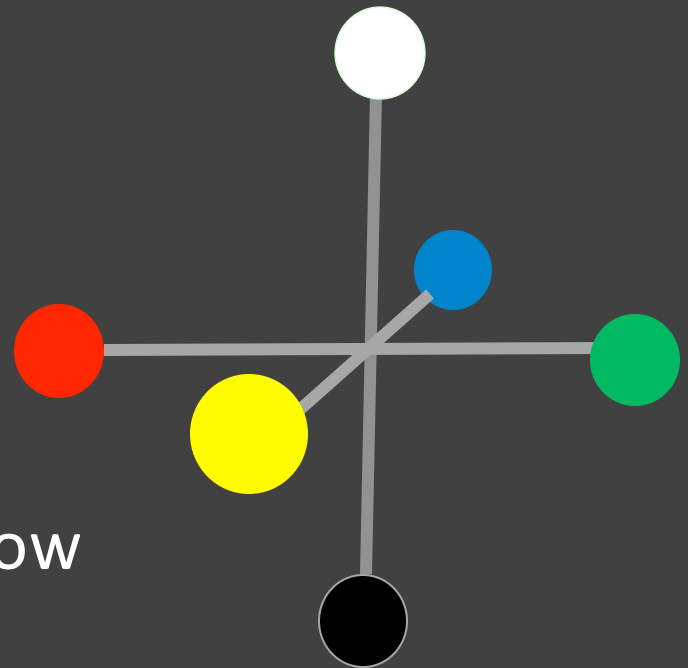
Red-green contrast

Yellow-blue contrast

Experiments:

No reddish-green, no blueish-yellow

Color after images







CIE LAB Color Space

Axes correspond to opponent signals

L^* = Luminance

a^* = Red-green contrast

b^* = Yellow-blue contrast

Much more perceptually uniform than RGB!

Scaling of axes to represent “color distance”

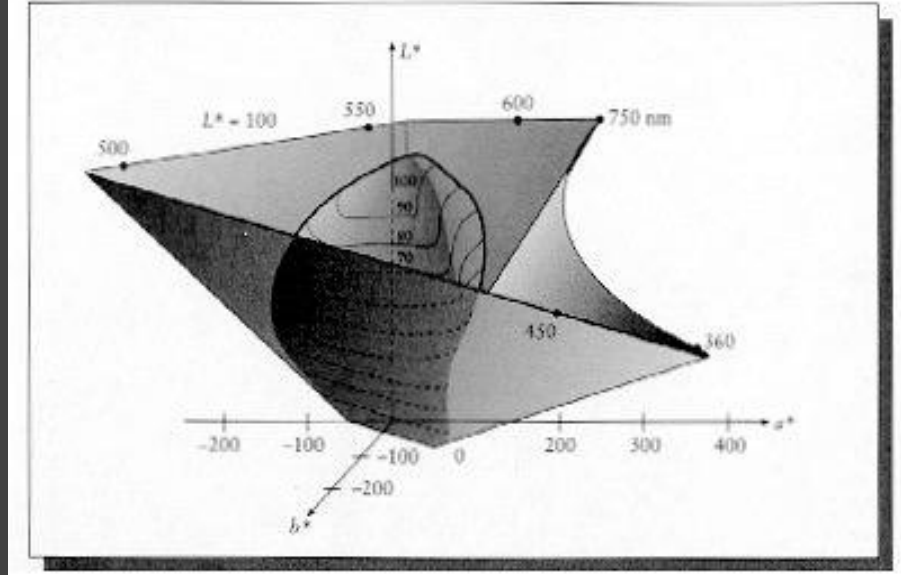
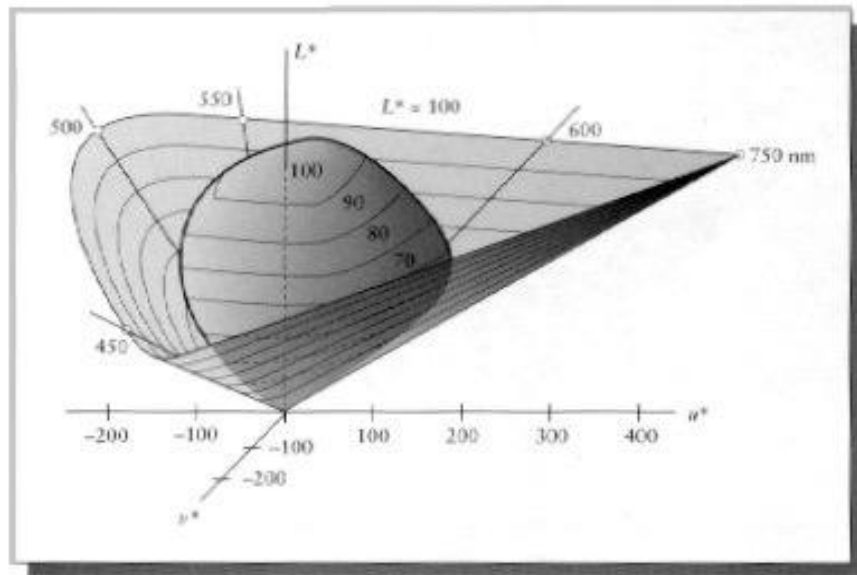
JND = Just noticeable difference (~2.3 units)

D3 + Vega include LAB color space support

CIE LAB and LUV Color Spaces

Standardized in 1976 to mathematically represent opponent processing theory.

Non-linear transformation of CIE XYZ



CIE LAB Color Space

Axes correspond to opponent signals

L^* = Luminance

a^* = Red-green contrast

b^* = Yellow-blue contrast

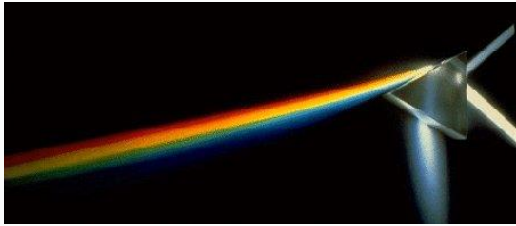
Much more perceptually uniform than sRGB!

Scaling of axes to represent “color distance”

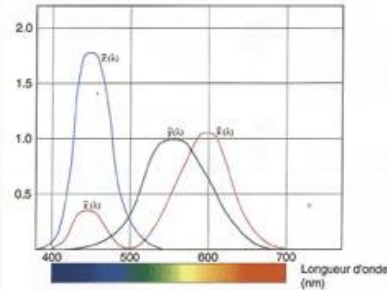
JND = Just noticeable difference (~2.3 units)

D3 + Vega include LAB color space support!

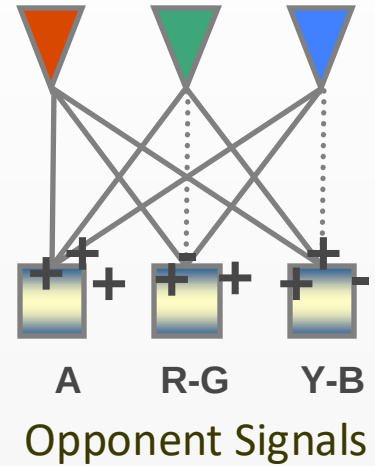
Perception of Color



Light



Cone Response



Opponent Signals

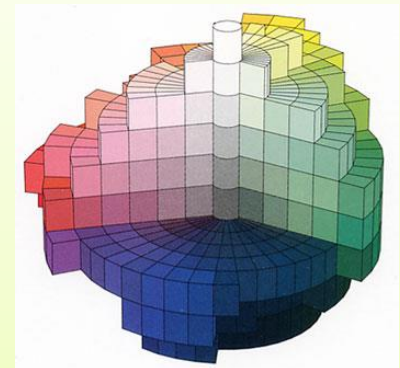
“Yellow”

Color Cognition



Mark D. Fairchild
**COLOR APPEARANCE
MODELS**

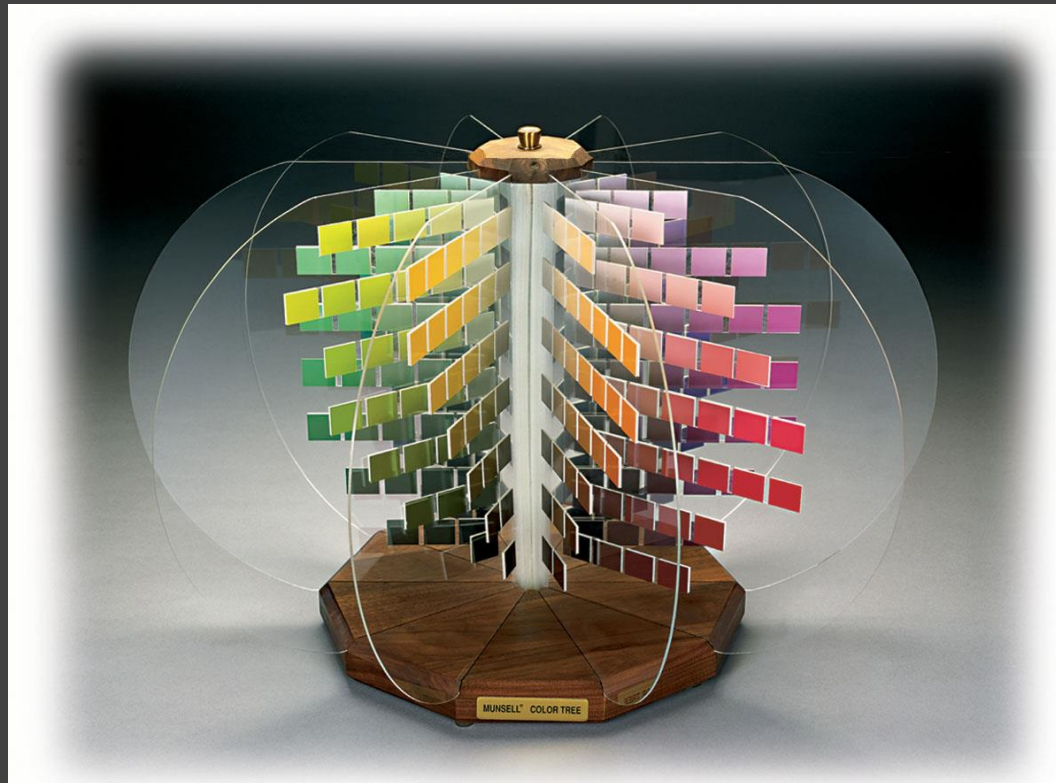
Color Appearance



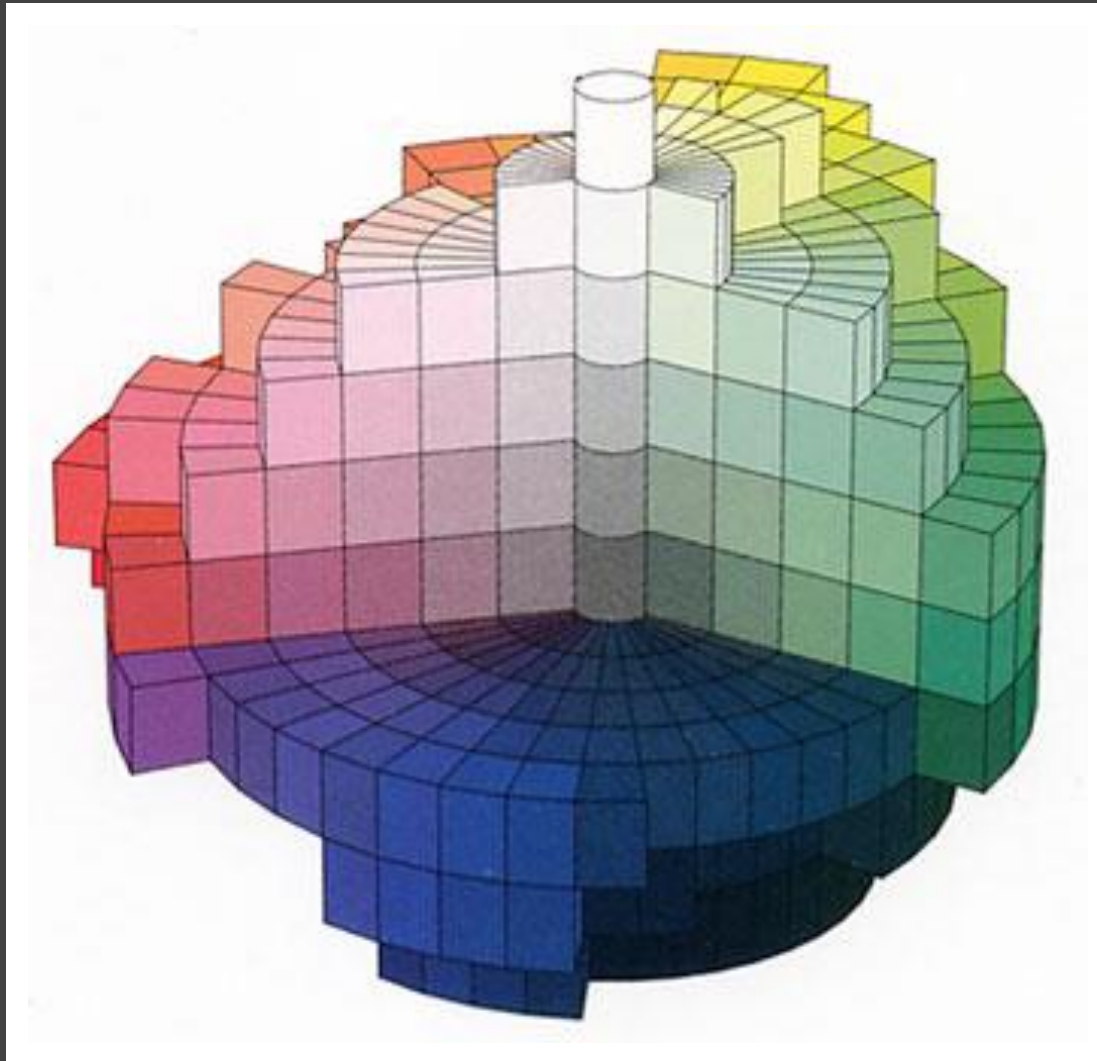
Color Perception

Albert Munsell

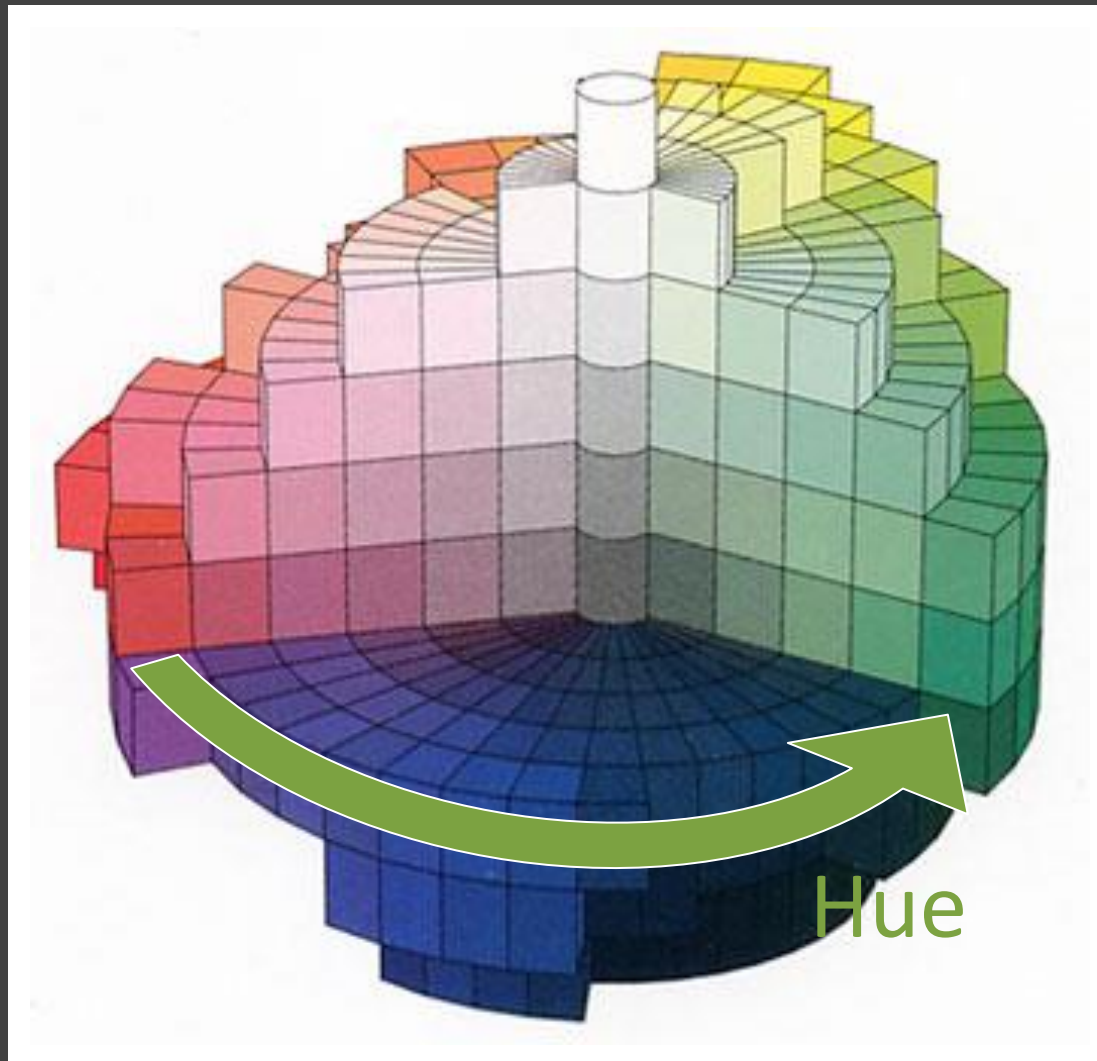
Developed the first perceptual color system based on his experience as an artist (1905).



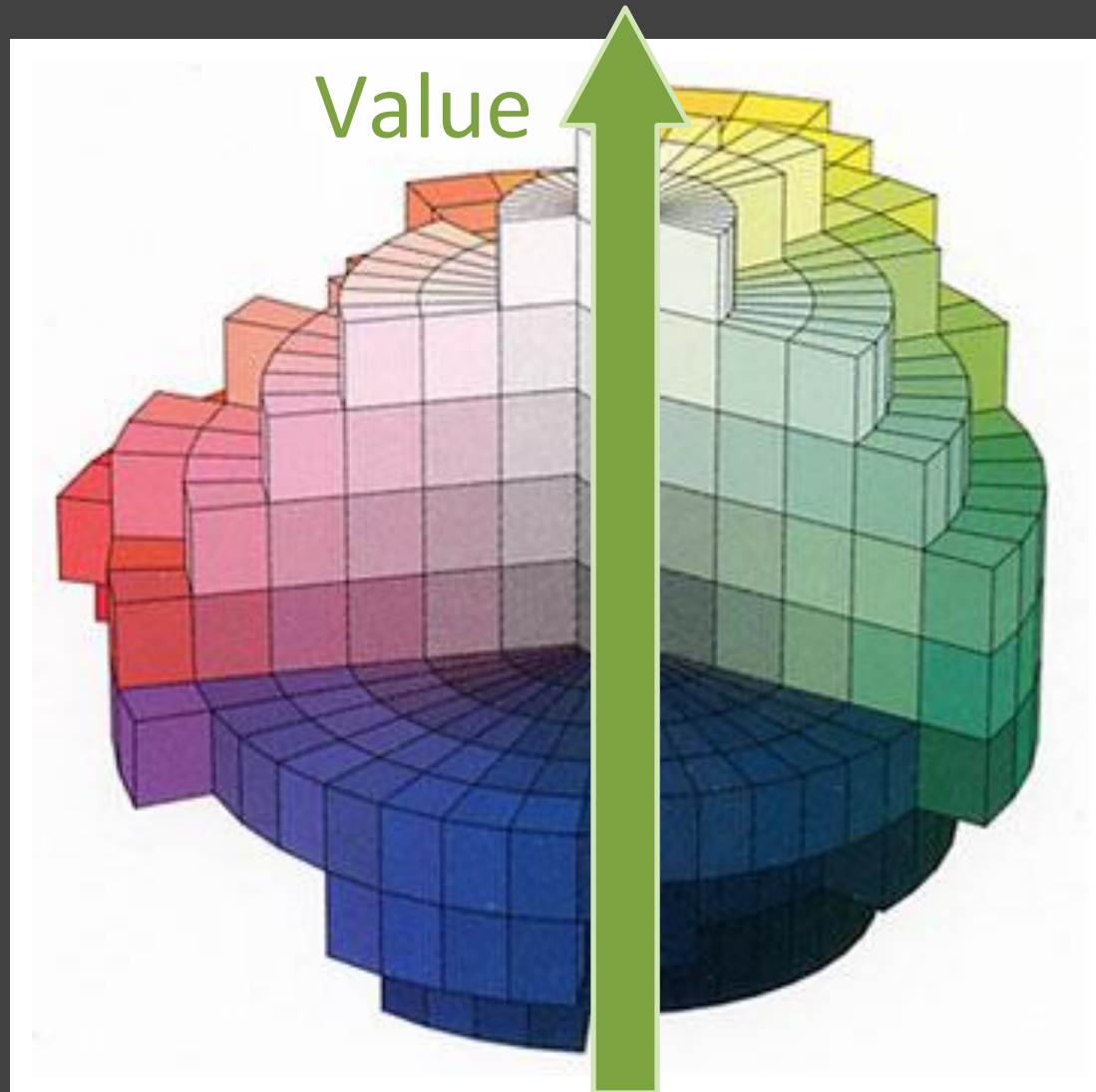
Hue, Value, and Chroma



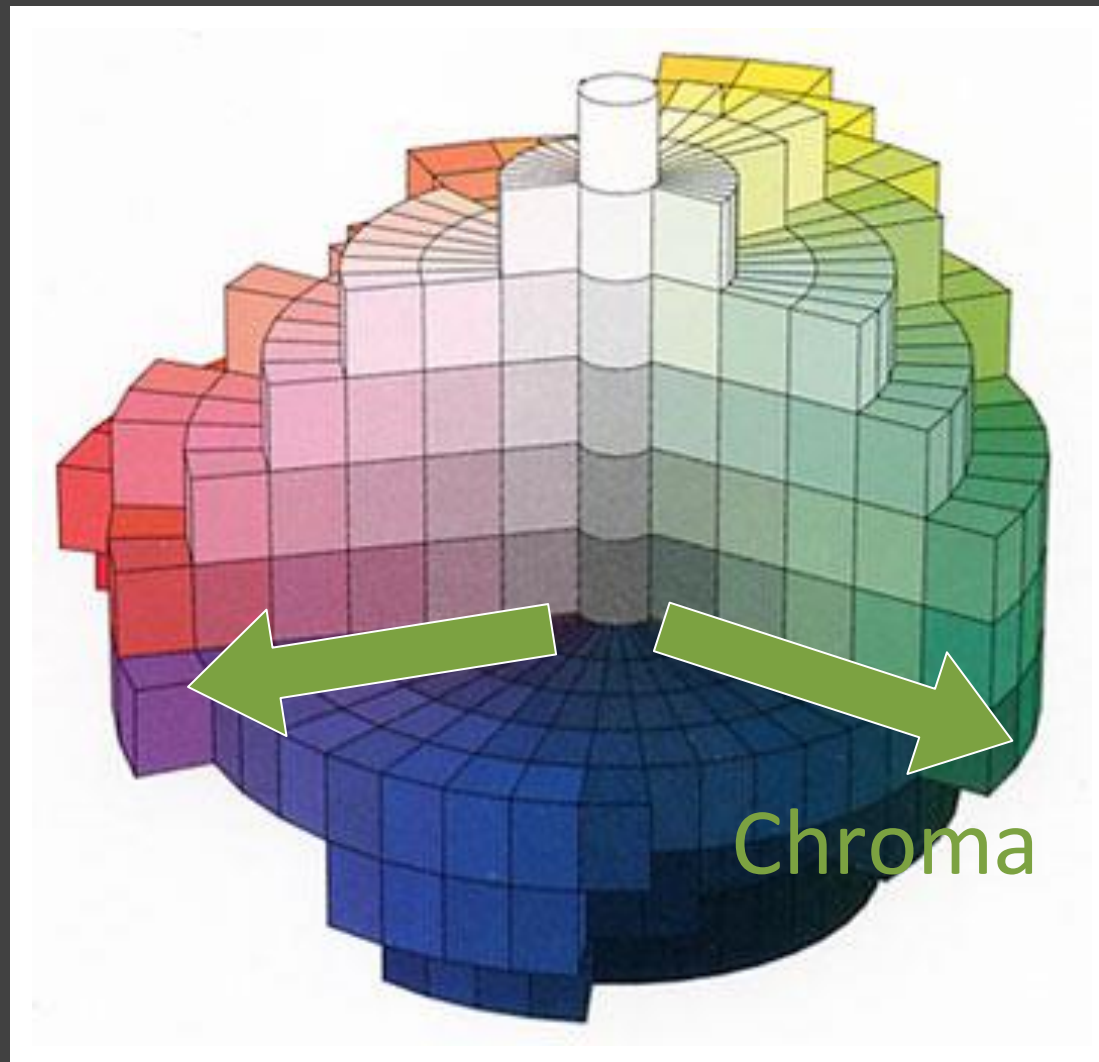
Hue, Value and Chroma



Hue, Value and Chroma



Hue, Value and Chroma



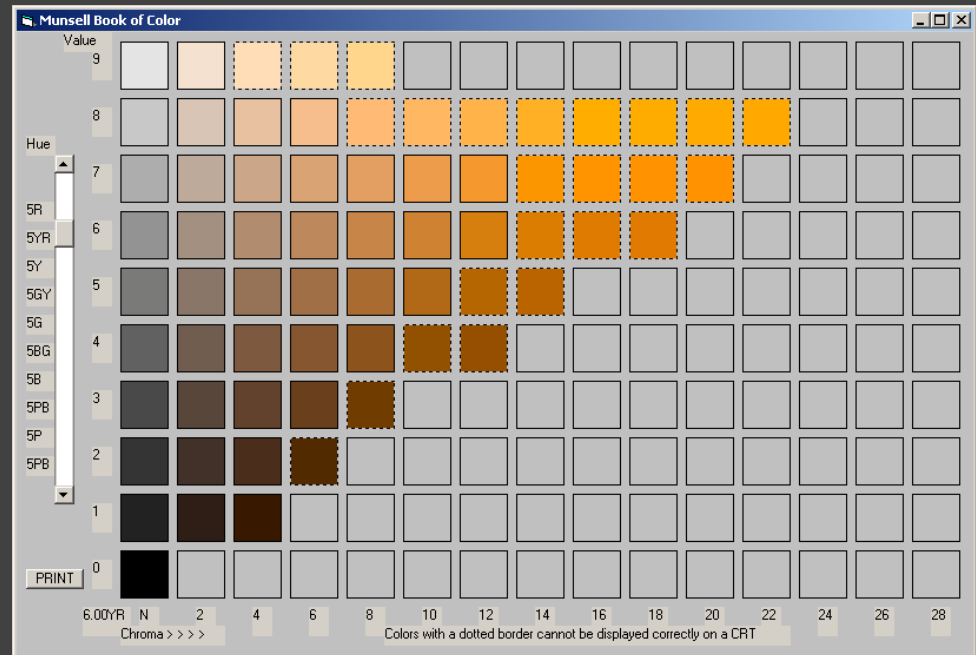
Munsell Color System

Perceptually-based

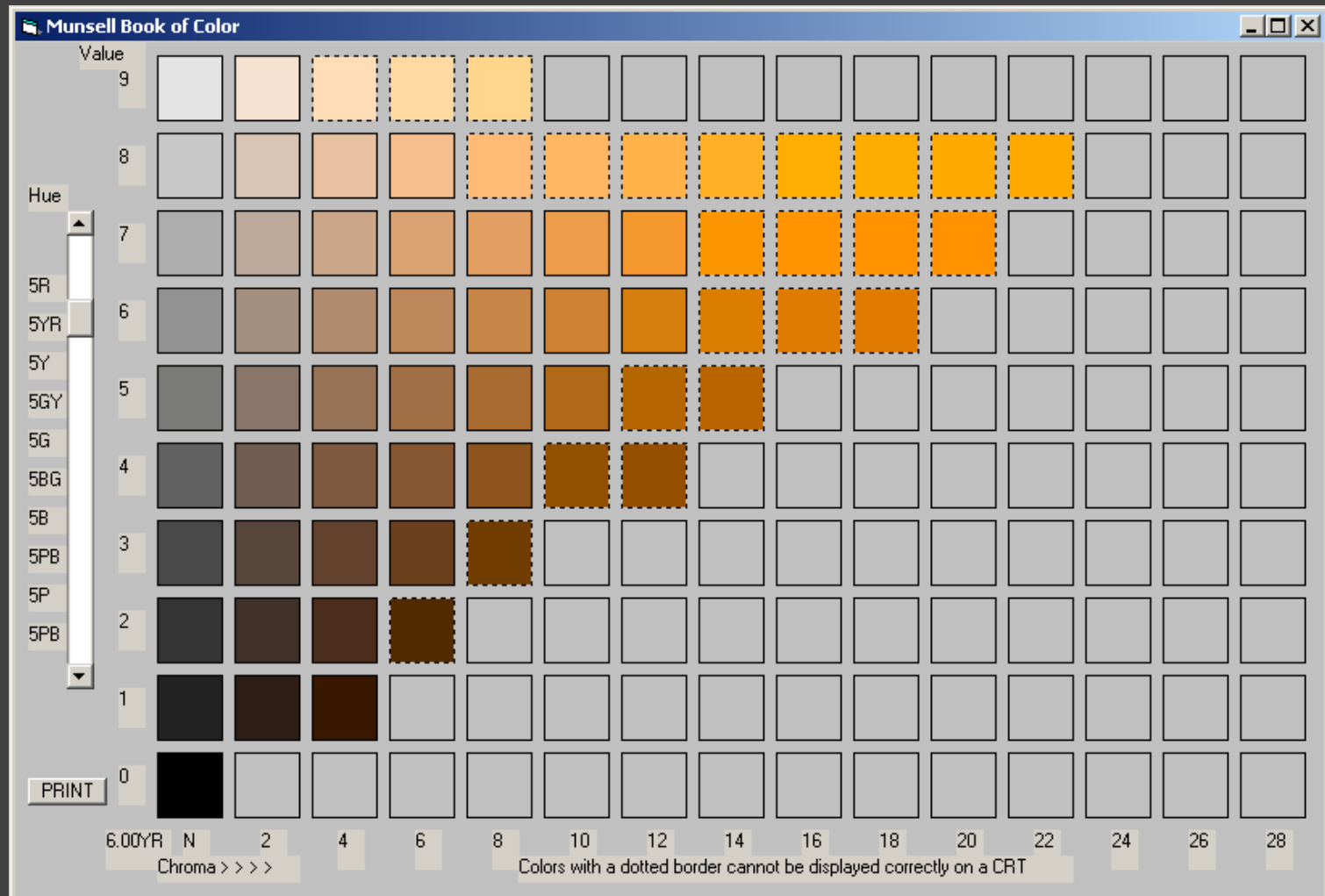
Precisely reference a color

Intuitive dimensions

Look-up table (LUT)

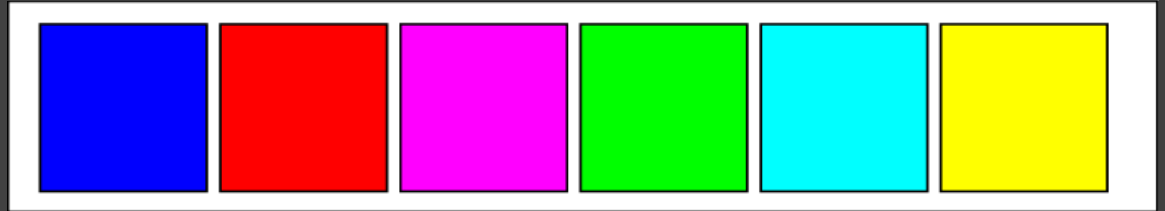


Munsell Color System



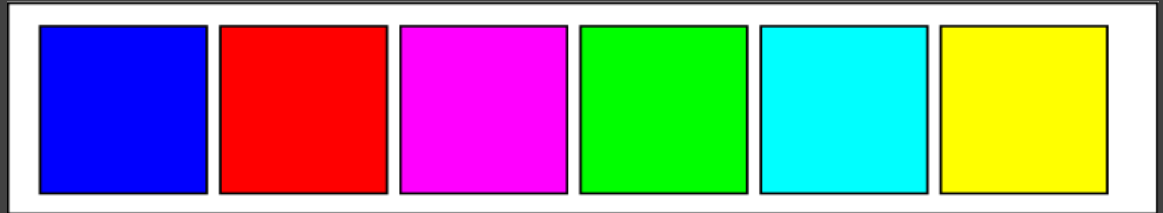
Perceptual Brightness

Color palette



Perceptual Brightness

Color palette

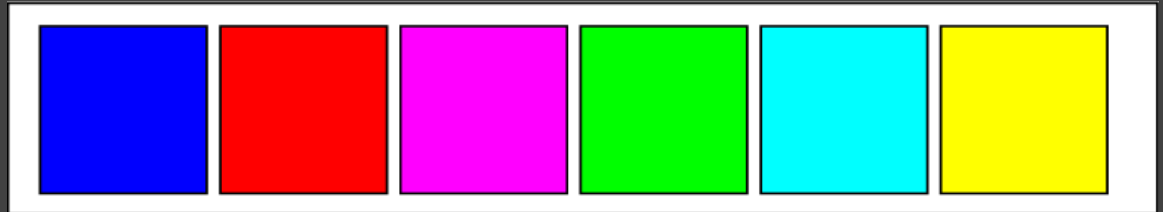


HSL Lightness
(Photoshop)



Perceptual Brightness

Color palette

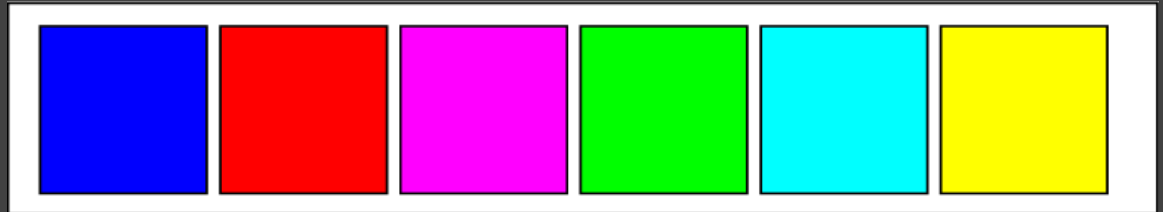


Luminance Y
(*CIE XYZ*)



Perceptual Brightness

Color palette

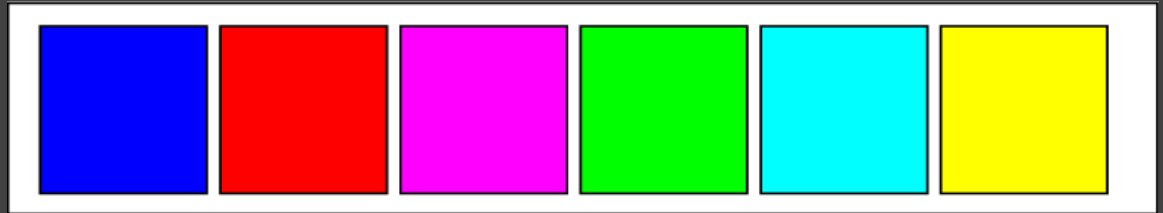


Munsell Value



Perceptual Brightness

Color palette

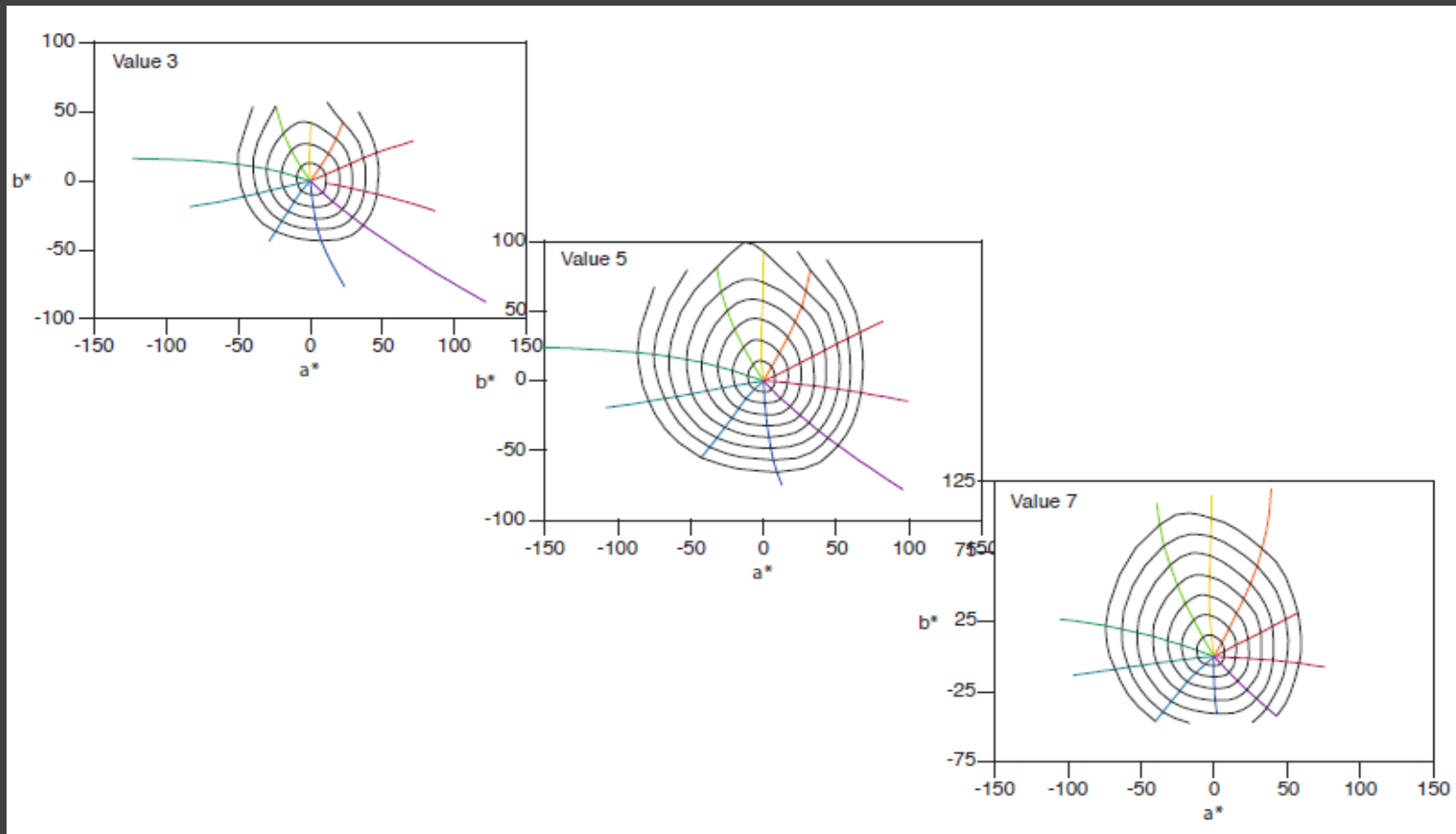


Munsell Value
 L^* (CIE LAB)



Perceptually-Uniform Color Space

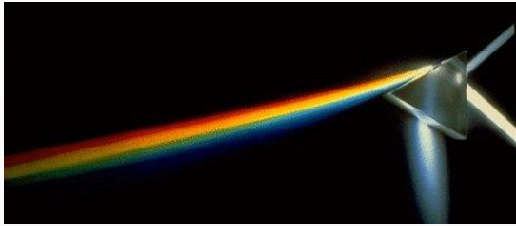
Munsell colors in CIE LAB coordinates



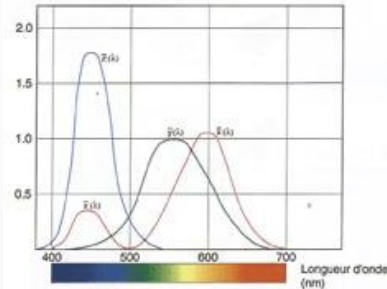
Summarizing the Color Spaces

Color Space	Emphasis
CIE XYZ	Physics/Anatomy
RGB / HSL	Hardware Capabilities
CIE LAB / CIE LUV	Psychology/Perception
Munsell Color System	Psychology/Perception

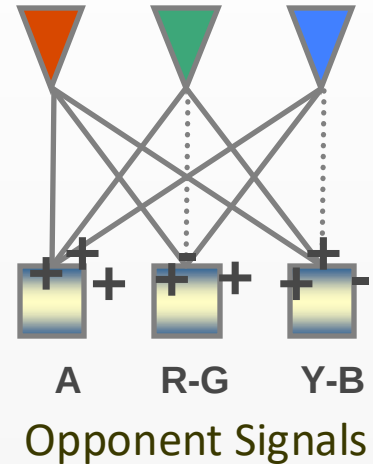
Perception of Color



Light



Cone Response



Opponent Signals

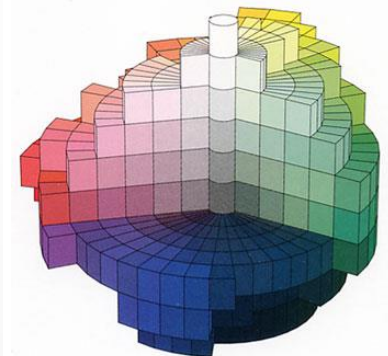
“Yellow”

Color Cognition



Mark D. Fairchild
**COLOR APPEARANCE
MODELS**

Color Appearance

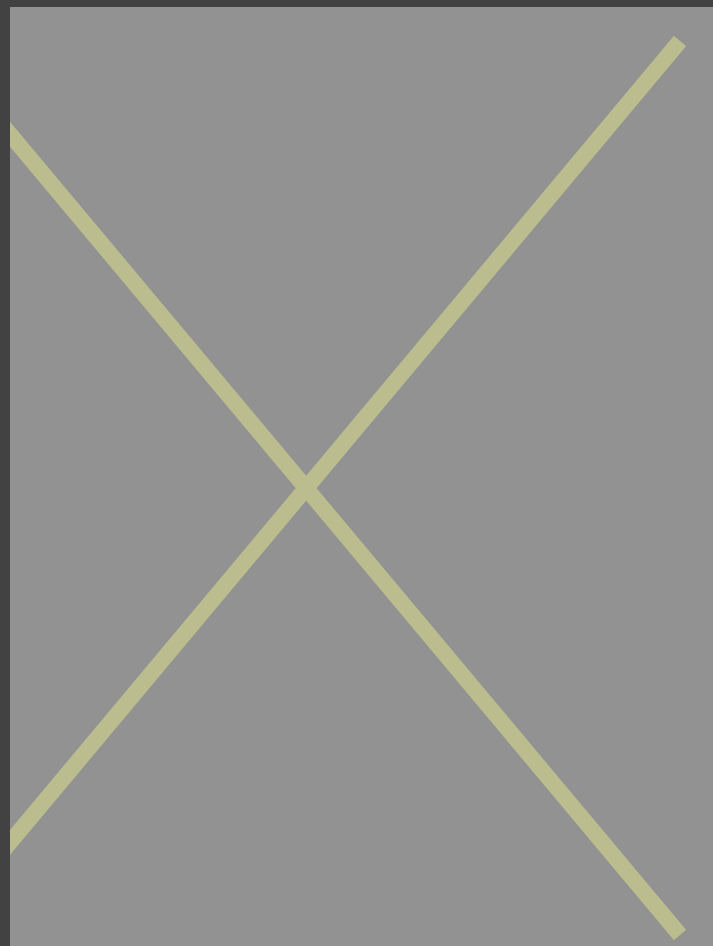
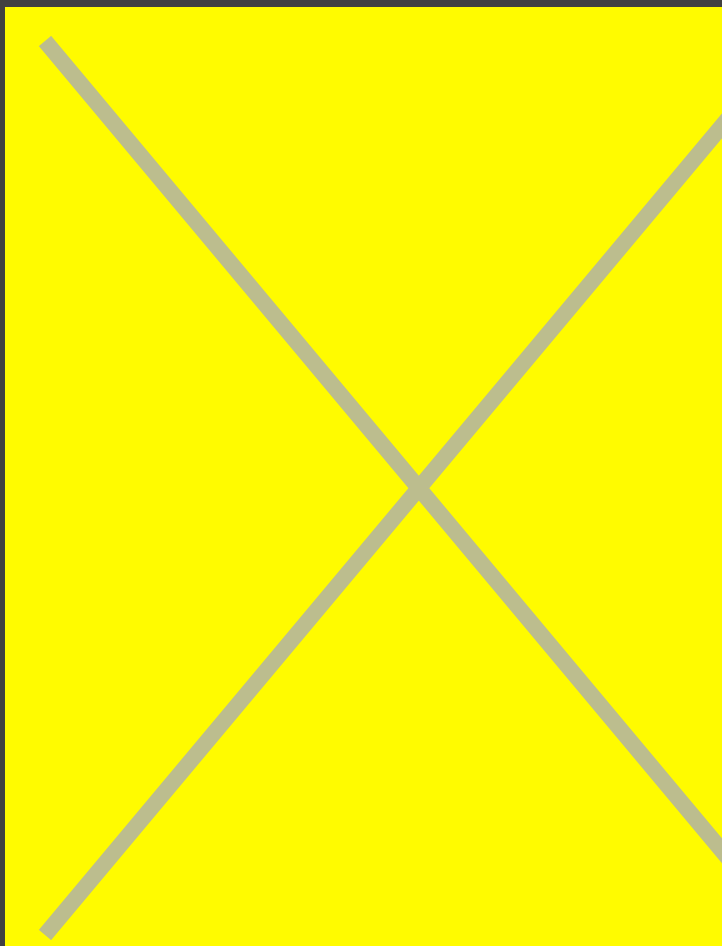


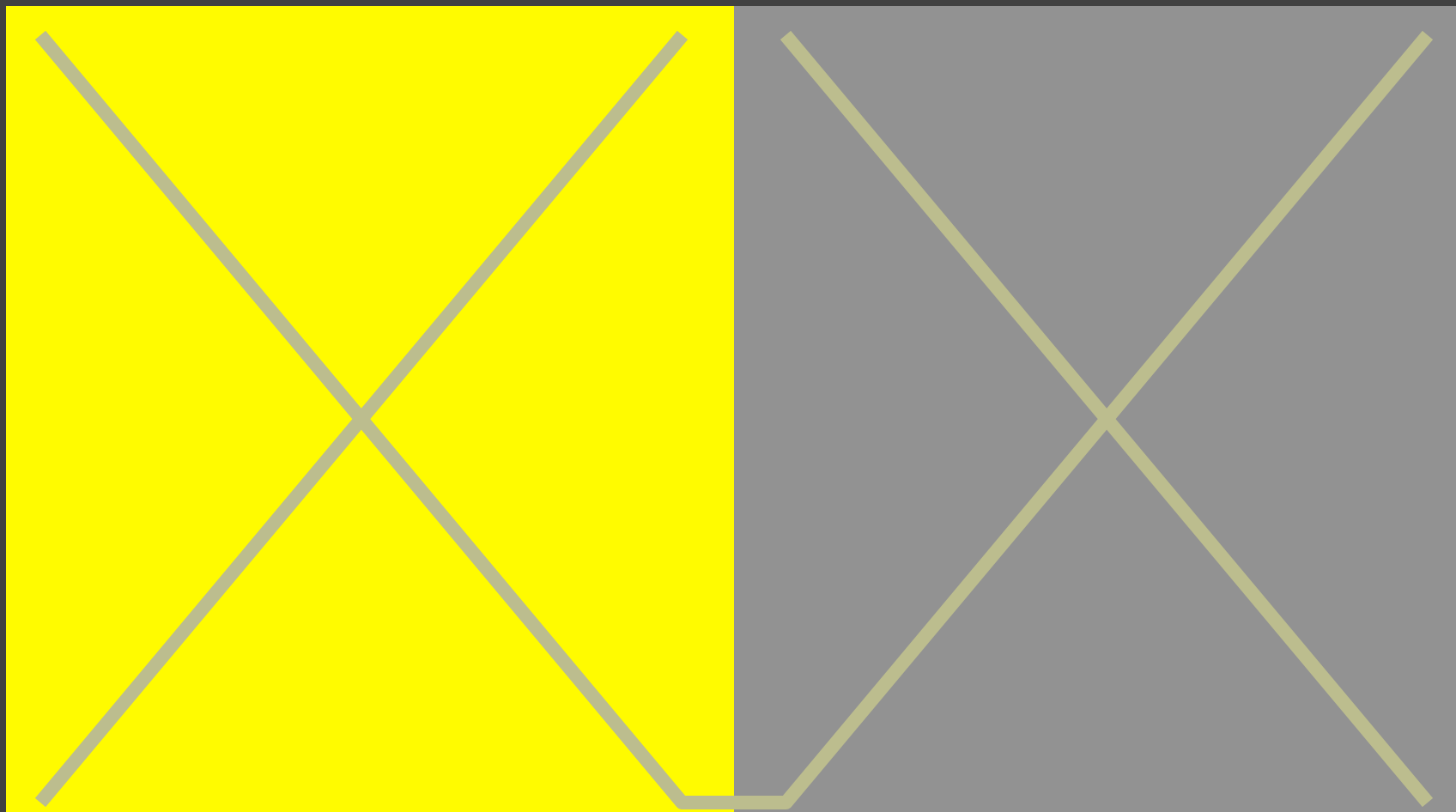
Color Perception

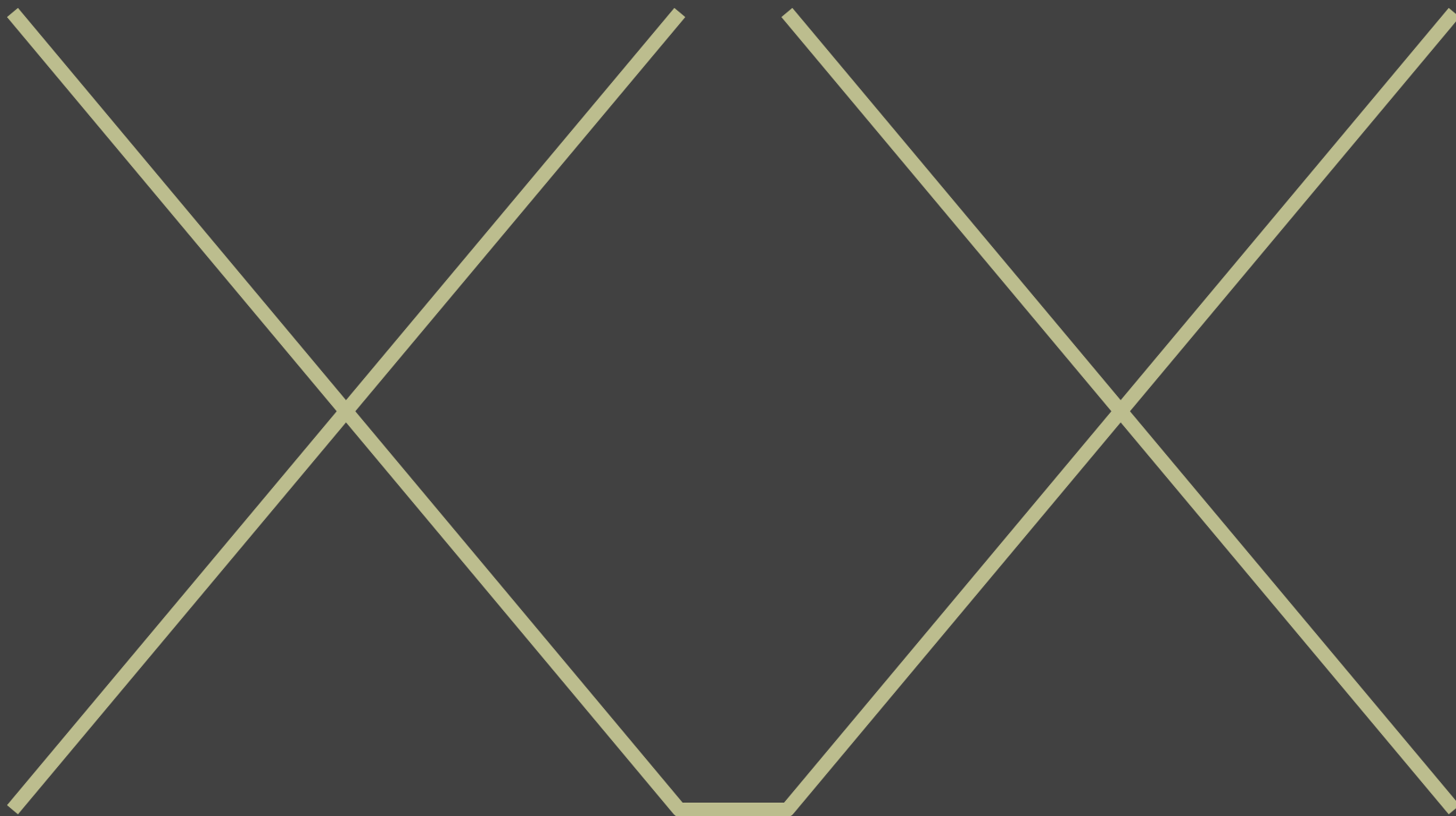
Color Appearance

If we have a perceptually-uniform color space, can we predict how we perceive colors?

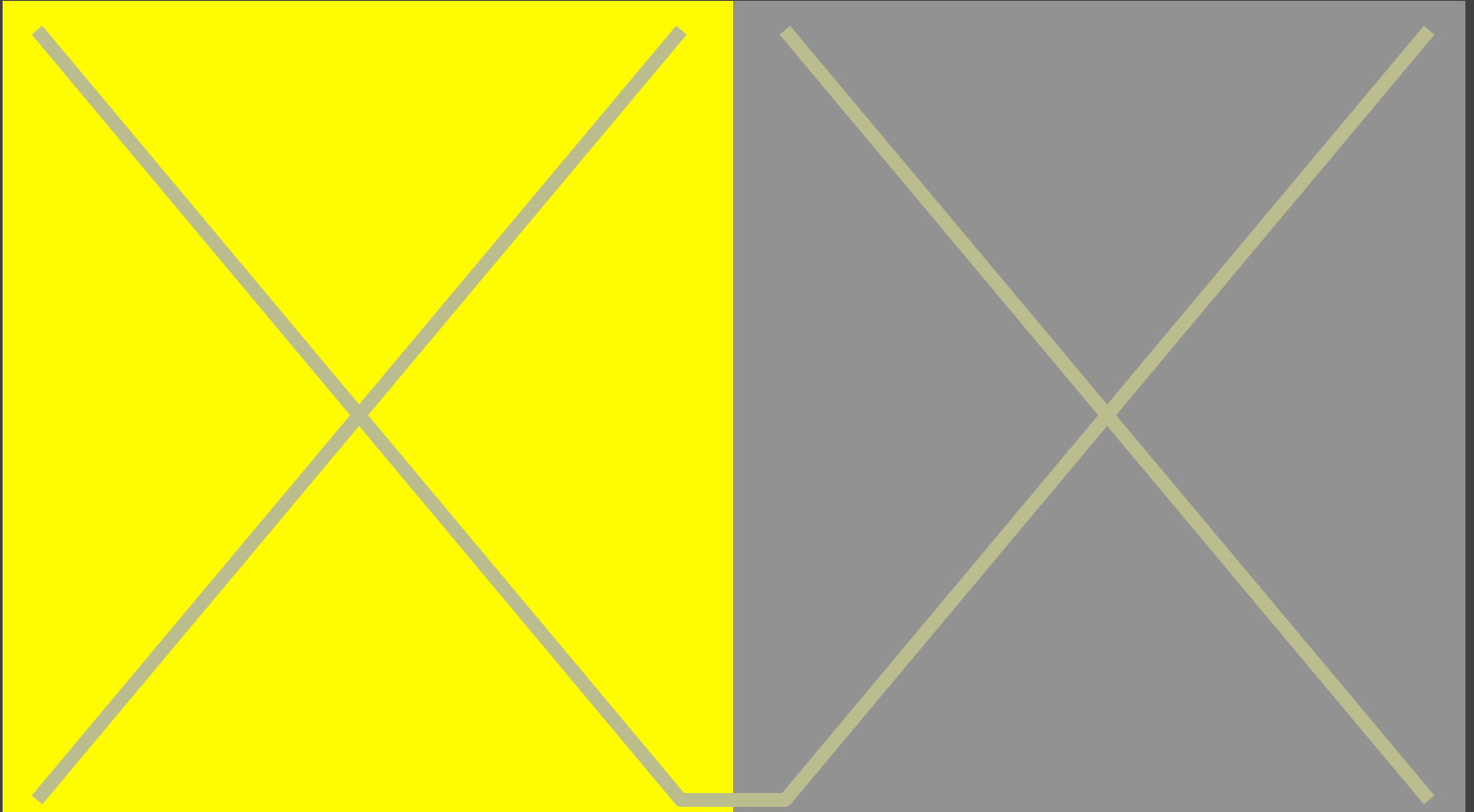
“In order to use color effectively it is necessary to recognize that it deceives continually.”
- Josef Albers, *Interaction of Color*







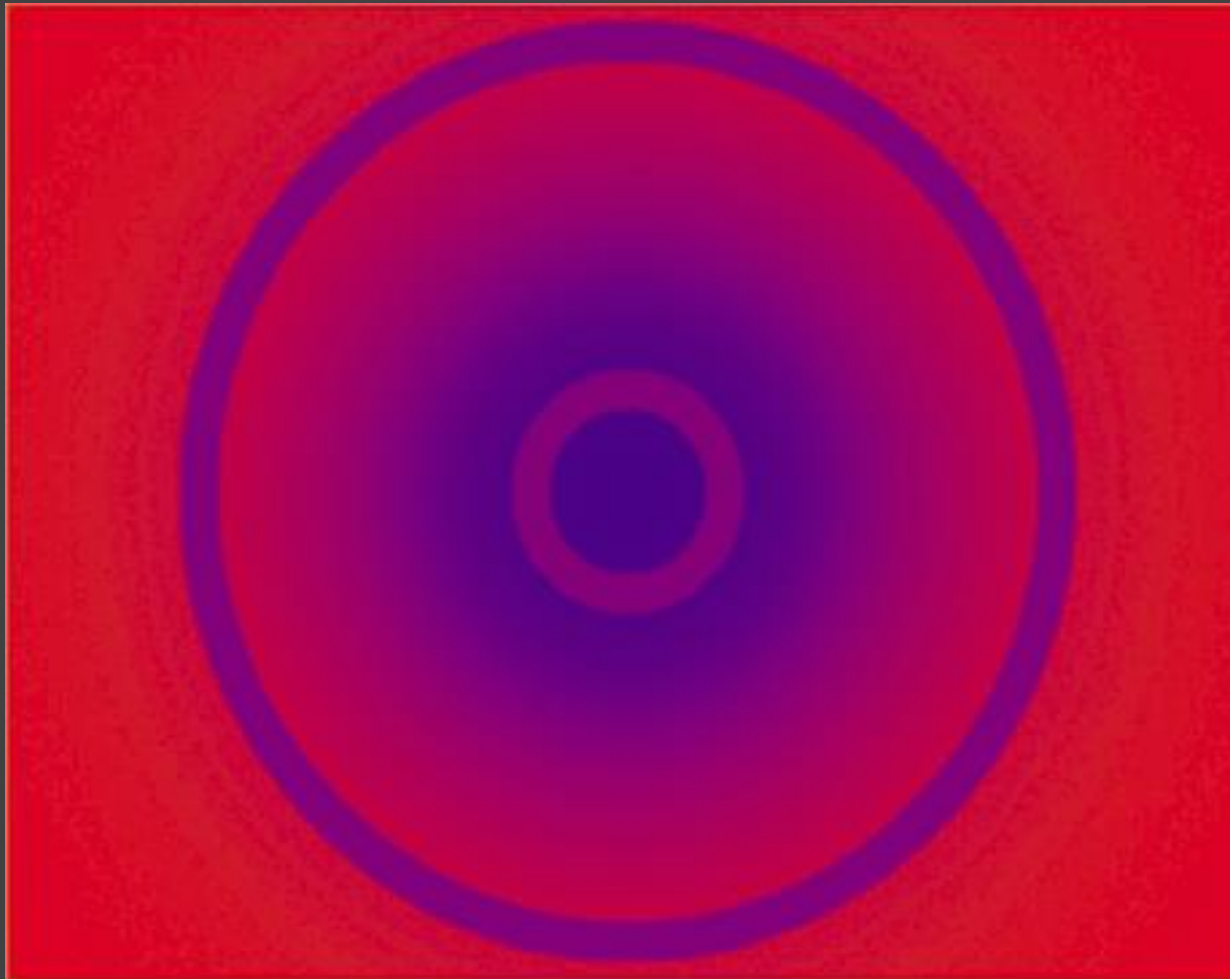
Simultaneous Contrast



Josef Albers

Simultaneous Contrast

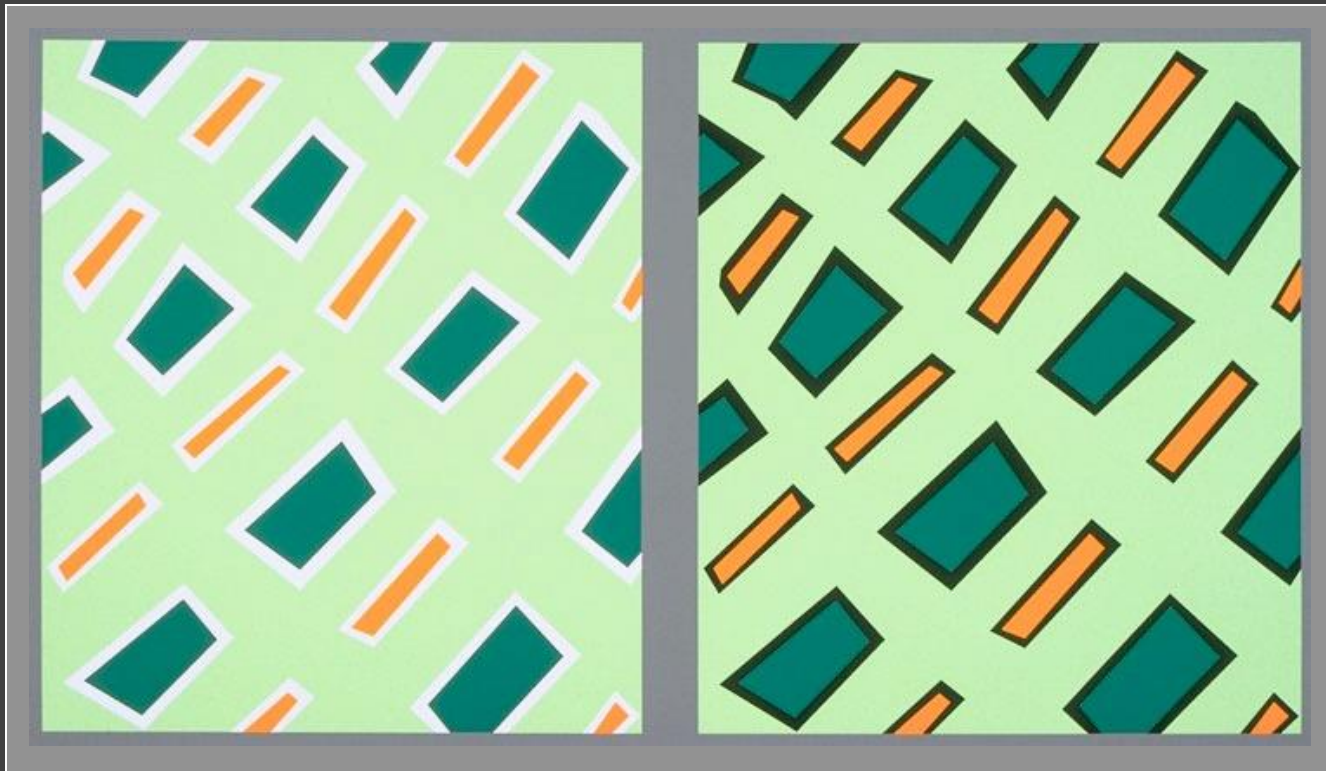
Inner & outer rings are the same physical purple.



Donald
MacLeod

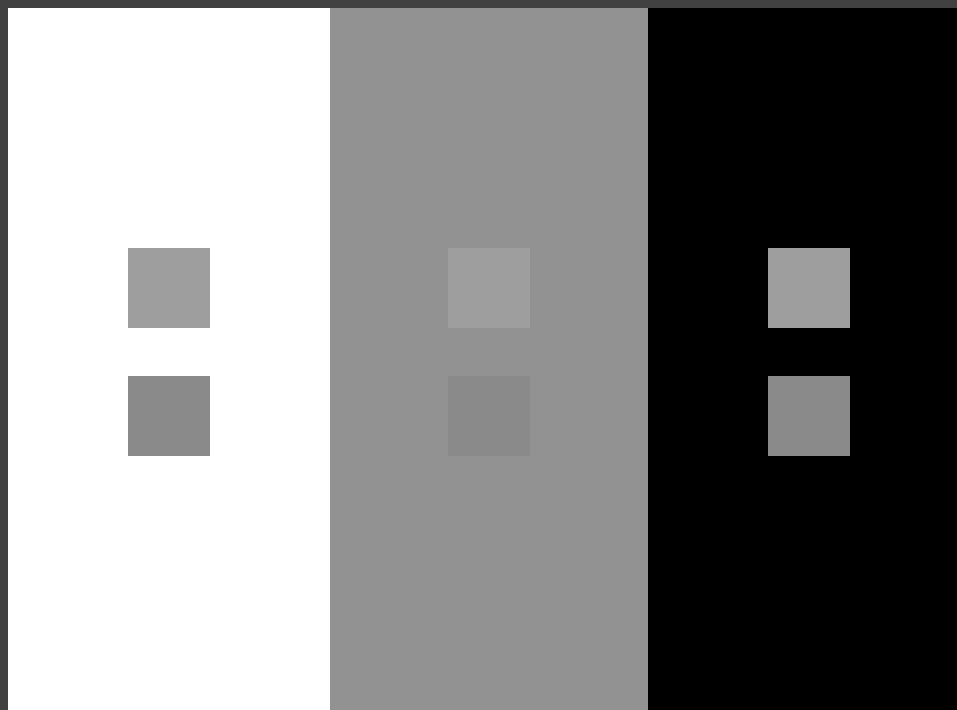
Bezold Effect

Color appearance depends on adjacent colors



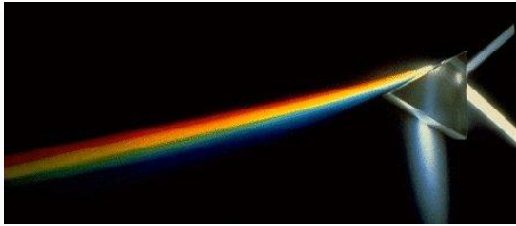
Crispening

Perceived difference depends on background

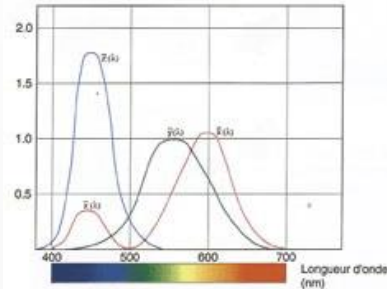


Color Appearance Models, Fairchild

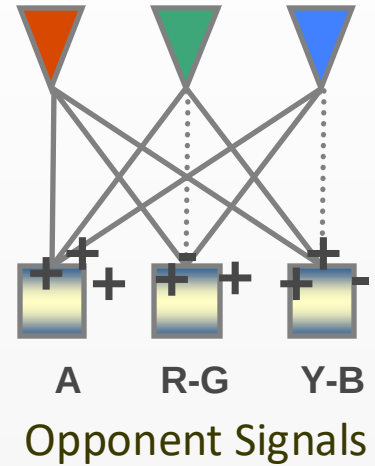
Perception of Color



Light



Cone Response



Opponent Signals

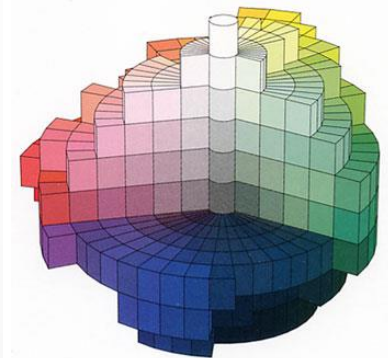
“Yellow”

Color Cognition



Mark D. Fairchild
**COLOR APPEARANCE
MODELS**

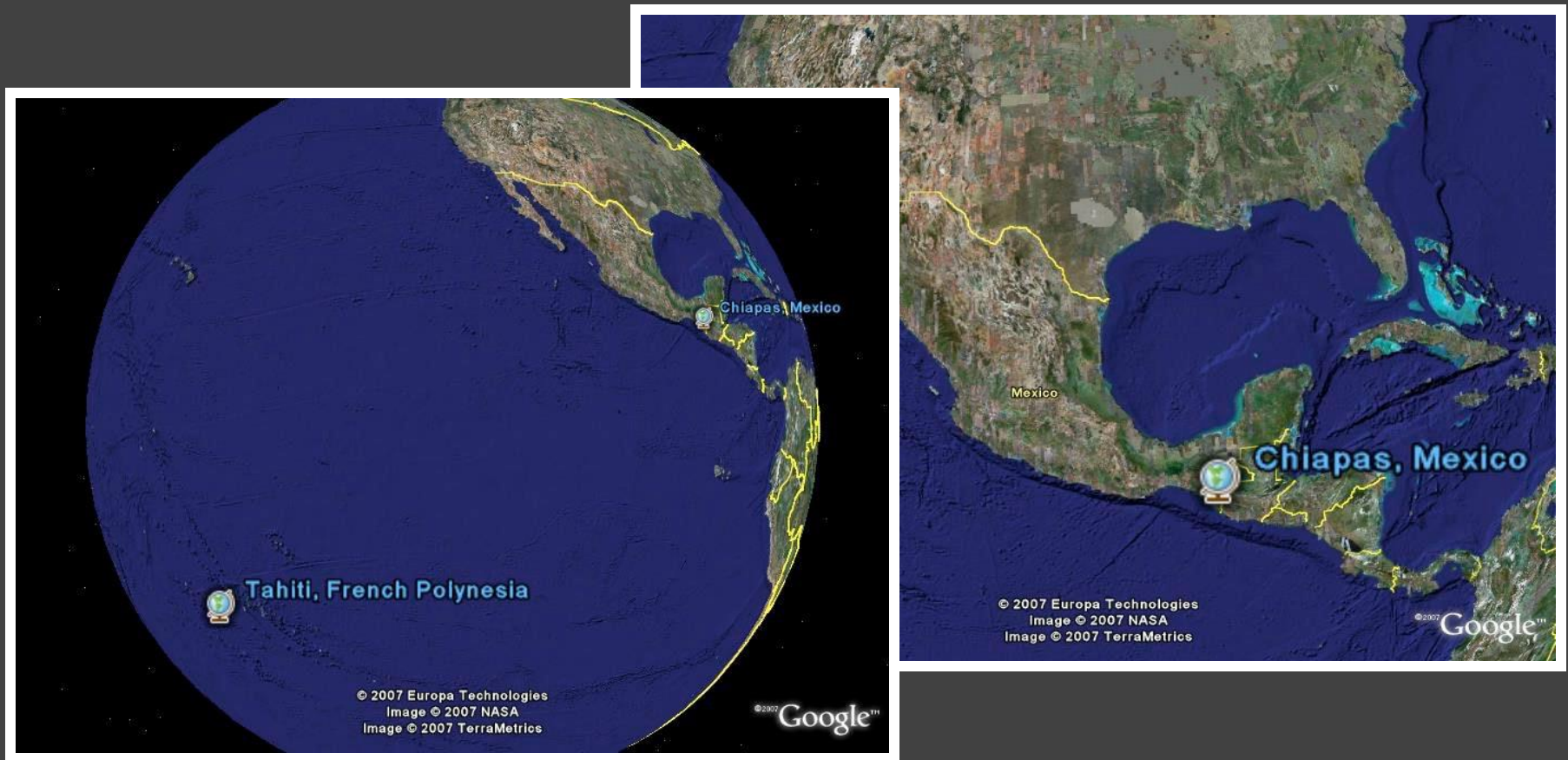
Color Appearance



Color Perception

Basic Color Terms

Chance discovery by Brent Berlin and Paul Kay.



Basic Color Terms

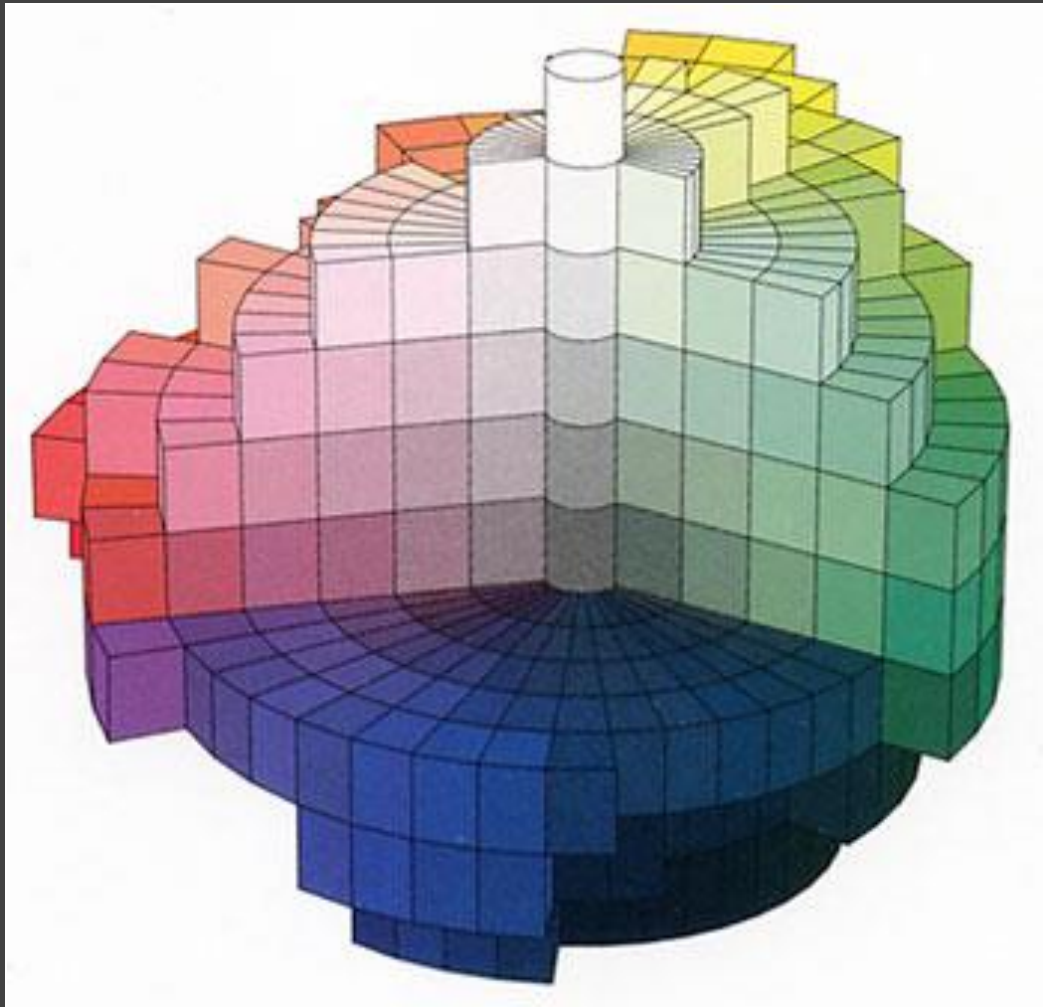
Chance discovery by Brent Berlin and Paul Kay.

Initial study in 1969

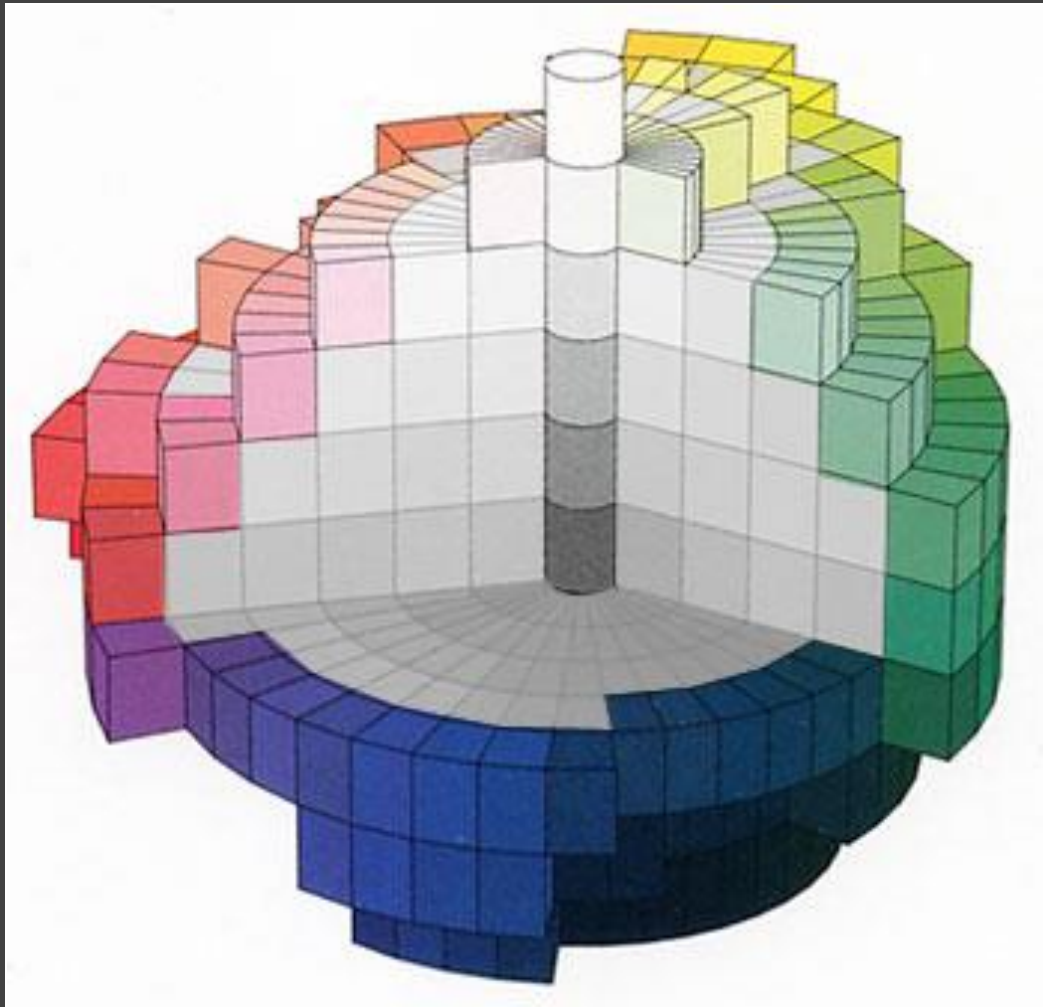
Surveyed speakers from 20 languages

Literature from 69 languages

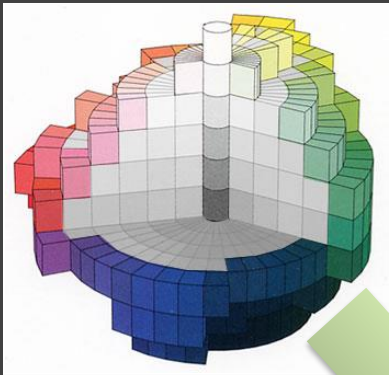
World Color Survey



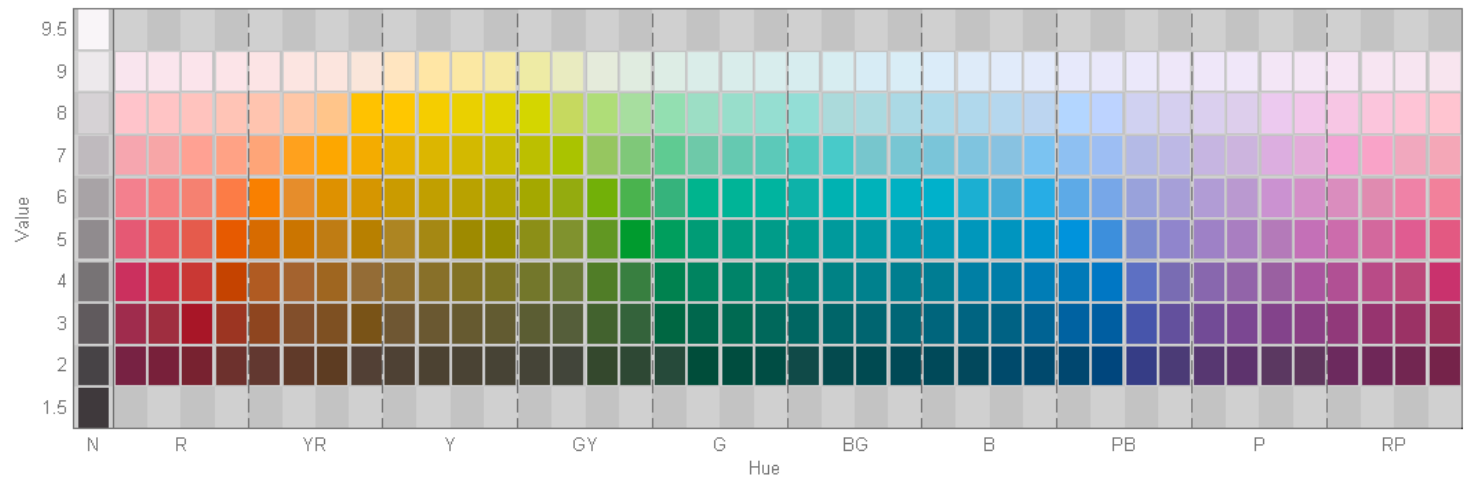
World Color Survey



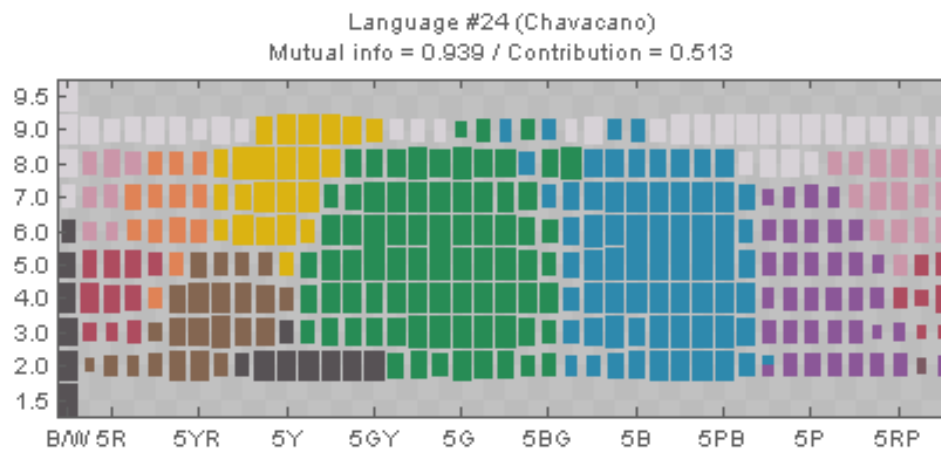
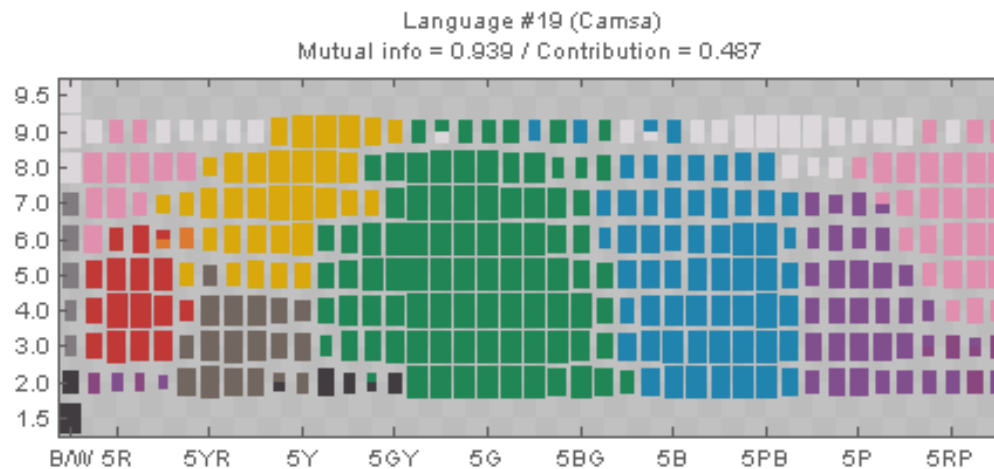
World Color Survey



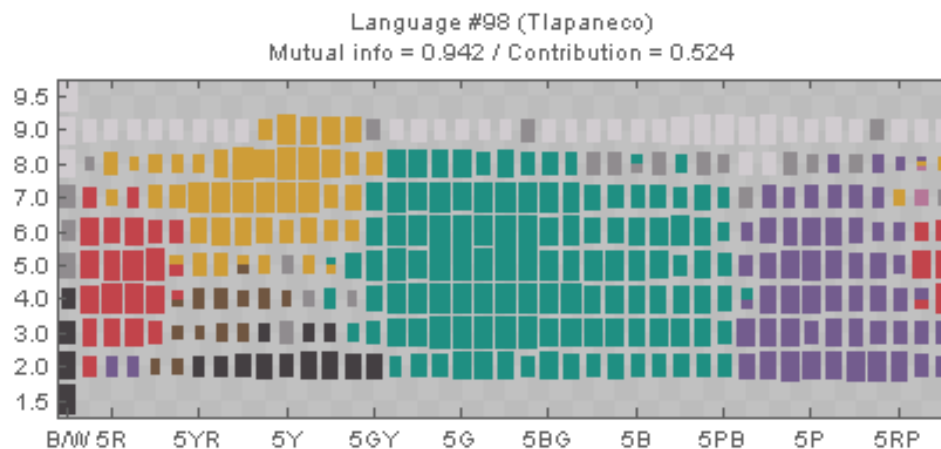
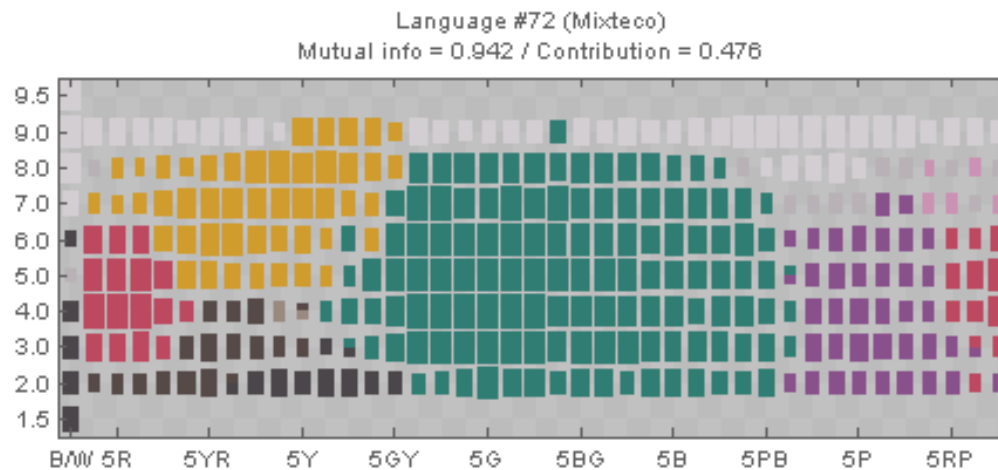
Naming information from 2,616 speakers
from 110 languages on 330 Munsell
color chips



Results from WCS



Results from WCS



Universal (?) Basic Color Terms

Basic color terms recur across languages.



White



Red



Pink



Grey



Yellow



Brown



Black



Green



Orange



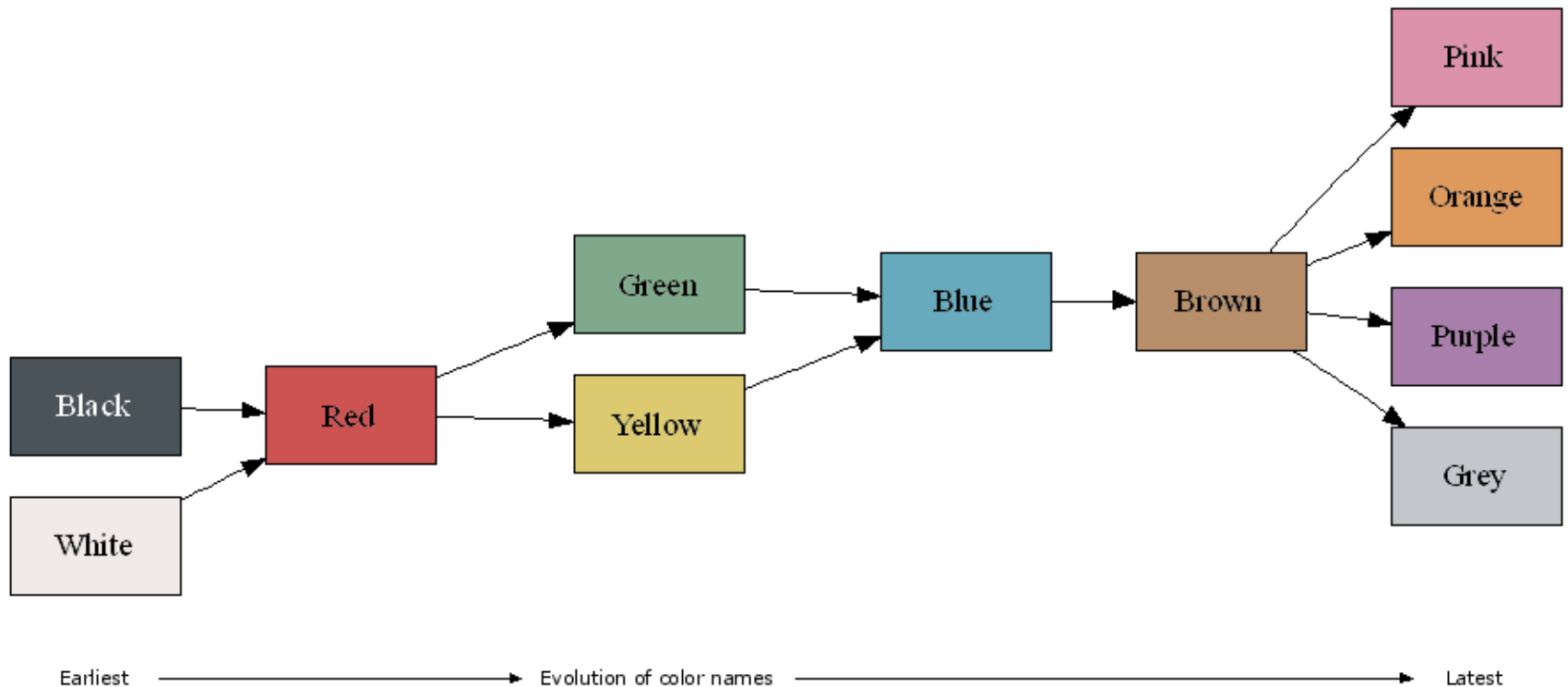
Blue



Purple

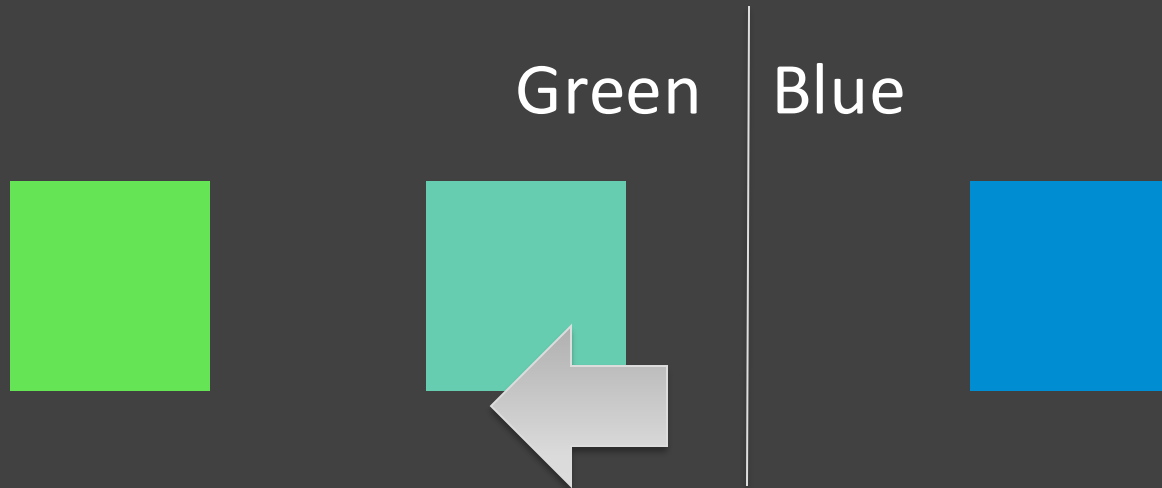
Evolution of Basic Color Terms

Proposed term evolution across languages.



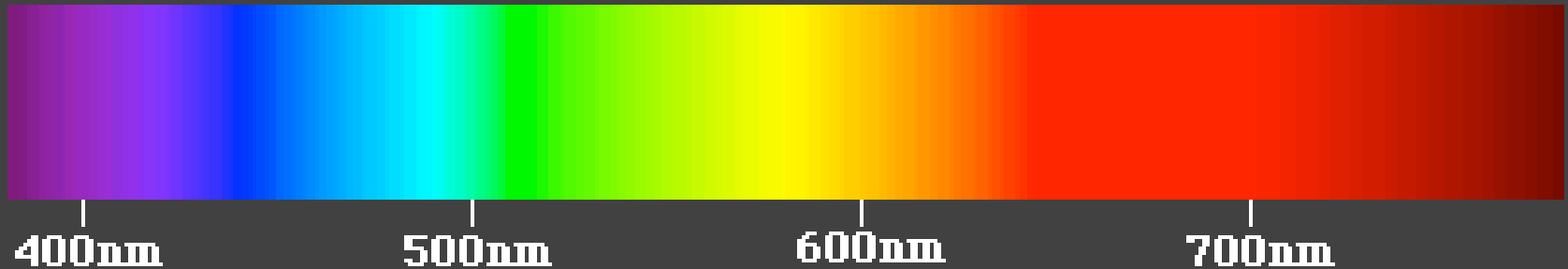
Naming Effects Color Perception

Color name boundaries



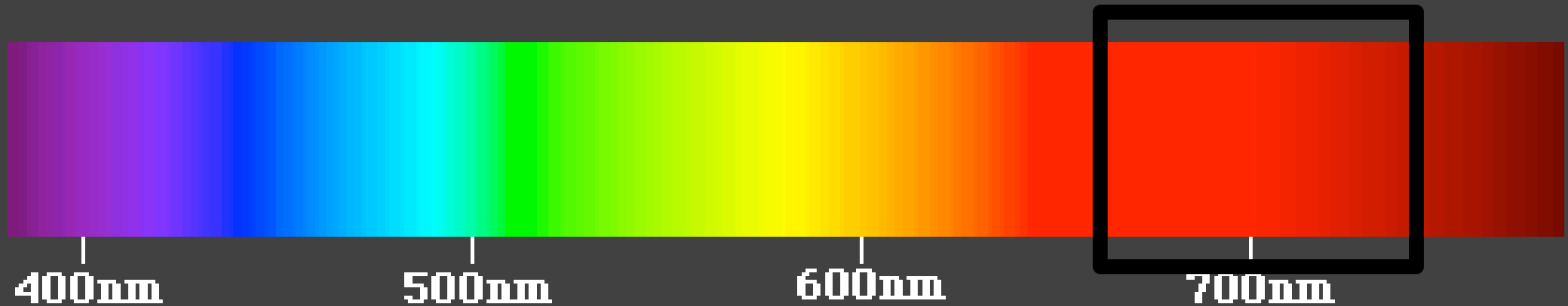
Rainbow Color Map

We associate and group colors together, often using the name we assign to the colors.



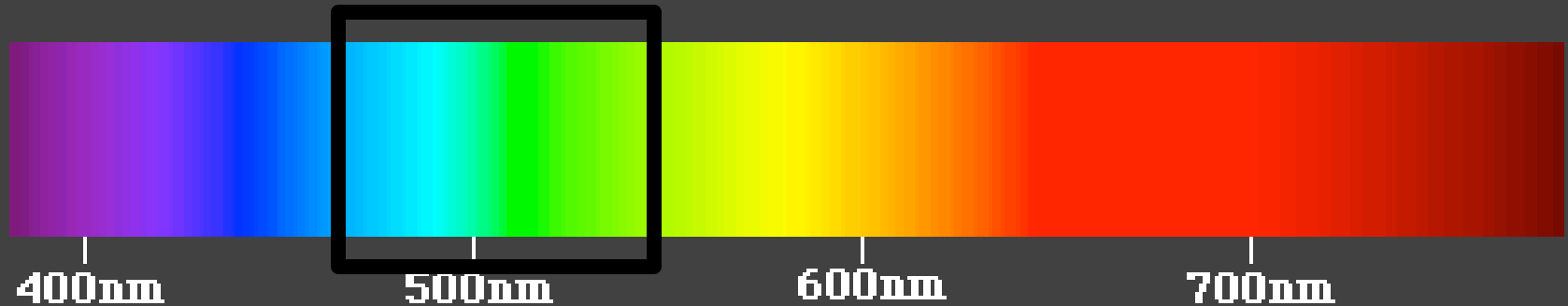
Rainbow Color Map

We associate and group colors together, often using the name we assign to the colors.

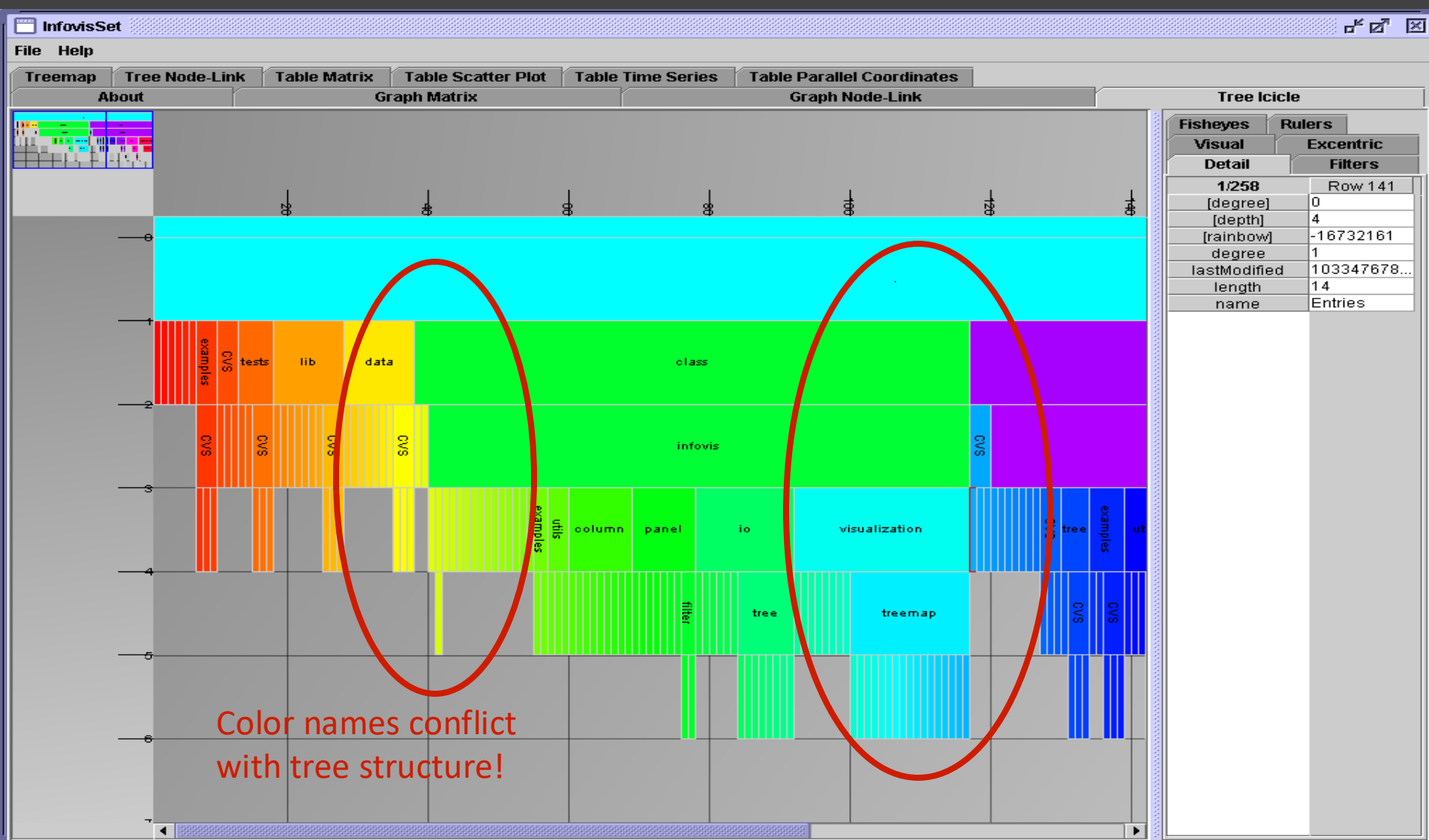


Rainbow Color Map

We associate and group colors together, often using the name we assign to the colors.



Icicle Tree with Rainbow Coloring



Color Naming Models

[Heer & Stone '12]

Model 3 million responses from XKCD survey

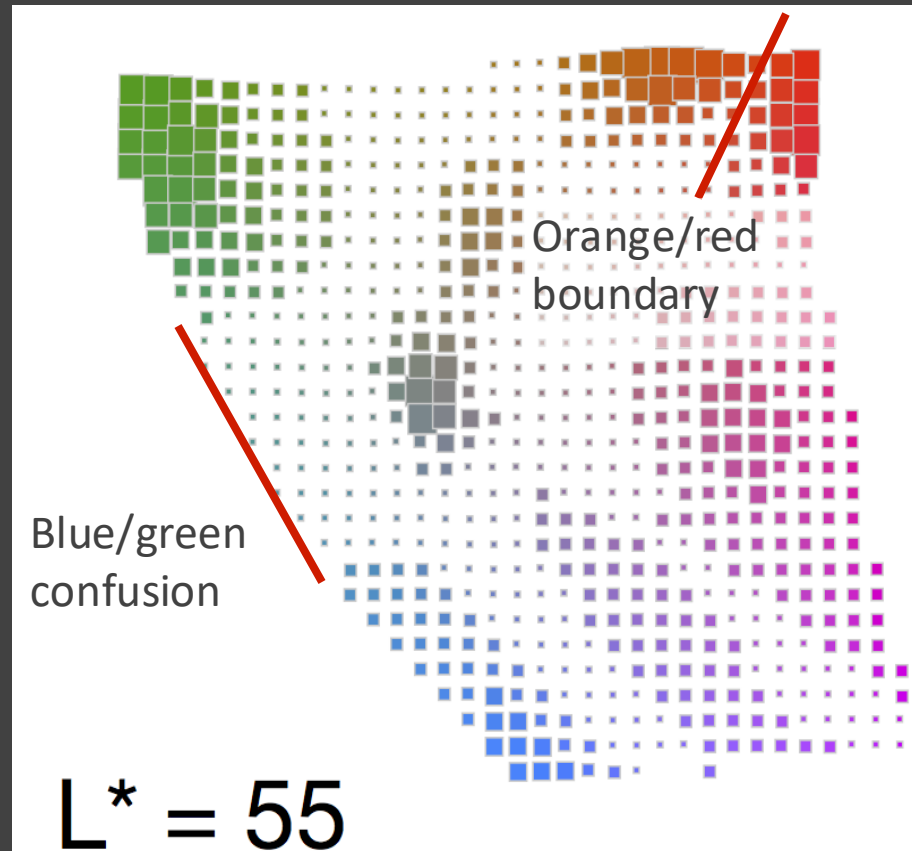
Bins in LAB space

sized by *saliency*:

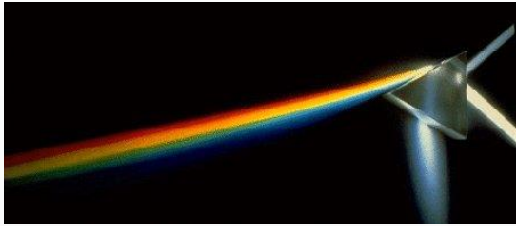
How much do people

agree on color name?

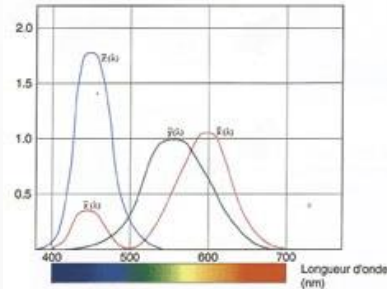
Modeled by entropy
of $p(\text{name} \mid \text{color})$



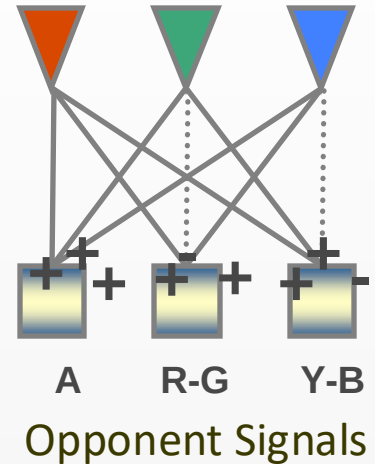
Perception of Color



Light



Cone Response



Opponent Signals

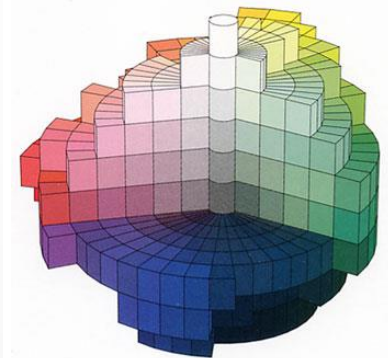
“Yellow”

Color Cognition



Mark D. Fairchild
**COLOR APPEARANCE
MODELS**

Color Appearance



Color Perception

Designing Colormaps

Colormap Design Considerations

- Perceptually distinguishable colors
- Value distance matches perceptual distance
- Colors and concepts properly align
- Aesthetically pleasing, intriguing
- Respect color vision deficiencies
- Should survive printing to black & white
- Don't overwhelm people's capability!

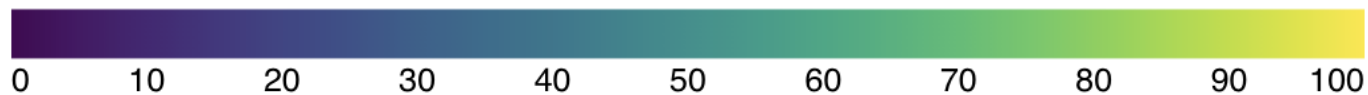
Discrete (Binary, Categorical)

Symbol Legend



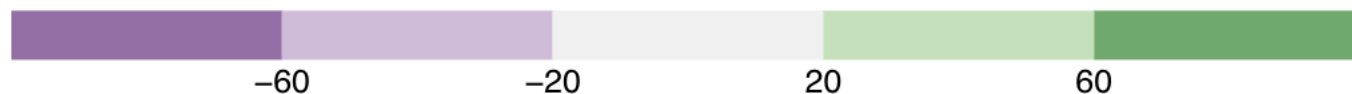
Continuous (Sequential, Diverging, Cyclic)

Gradient Legend



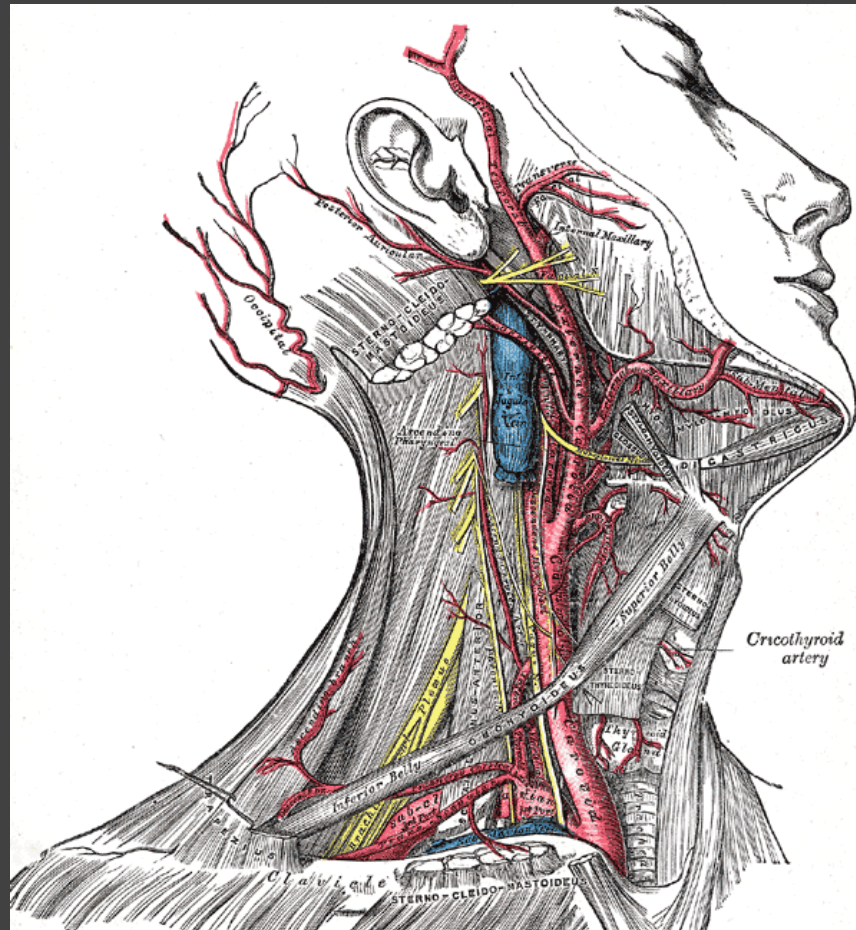
Discretized Continuous

Discrete Gradient



Categorical Color

Gray's Anatomy



Superficial dissection of the right side of the neck, showing the carotid and subclavian arteries. (<http://www.bartleby.com/107/illus520.html>)

Allocation of the Radio Spectrum

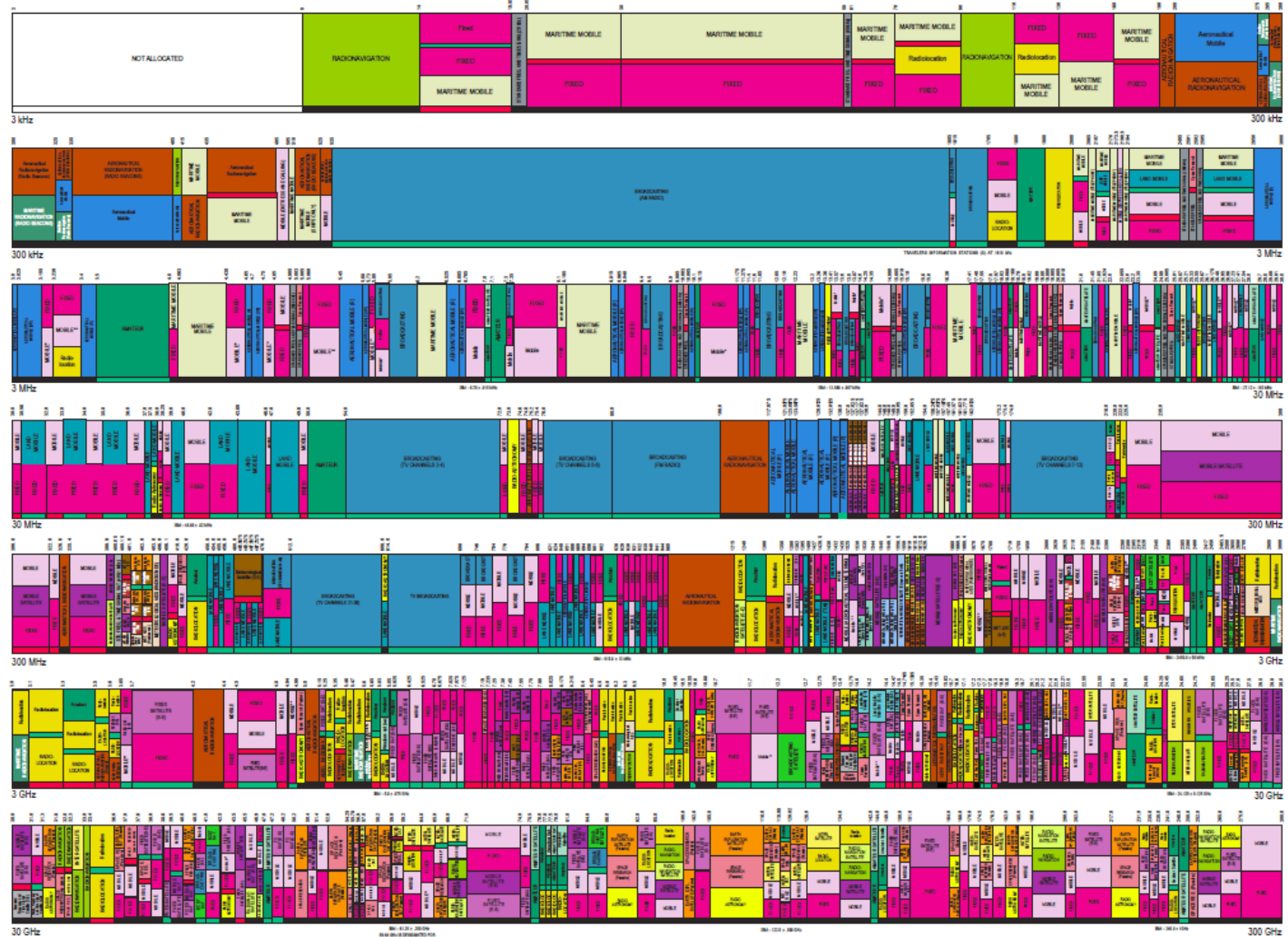
UNITED STATES FREQUENCY ALLOCATIONS THE RADIO SPECTRUM

RADIO SERVICES COLOR LEGEND

ACTIVITY CODE

ALLOCATION USAGE DESIGNATION

SERVICE	EXAMPLE	DESCRIPTION
Primary	FIXED	Capital Letters
Secondary	MOBILE	Small Letters



<http://www.ntia.doc.gov/osmhome/allochrt.html>

Allocation

UNITED STATES FREQUENCY ALLOCATION THE RADIO SPECTRUM

RADIO SERVICES COLOR LEGEND

ACTIVITY CODE

ALLOCATION USAGE DESIGNATION

SERVICE	EXAMPLE	DESCRIPTION
Primary	FIXED	Capital Letters
Secondary	MOBILE	Alphabetical Letters, Numbers, Punctuation

RADIO SERVICES COLOR LEGEND

	AERONAUTICAL MOBILE		INTER-SATELLITE		RADIO ASTRONOMY
	AERONAUTICAL MOBILE SATELLITE		LAND MOBILE		RADIO DETERMINATION SATELLITE
	AERONAUTICAL RADIONAVIGATION		LAND MOBILE SATELLITE		RADIOLOCATION
	AMATEUR		MARITIME MOBILE		RADIOLOCATION SATELLITE
	AMATEUR SATELLITE		MARITIME MOBILE SATELLITE		RADIONAVIGATION
	BROADCASTING		MARITIME RADIONAVIGATION		RADIONAVIGATION SATELLITE
	BROADCASTING SATELLITE		METEOROLOGICAL AIDS		SPACE OPERATION
	EARTH EXPLORATION SATELLITE		METEOROLOGICAL SATELLITE		SPACE RESEARCH
	FIXED		MOBILE		STANDARD FREQUENCY AND TIME SIGNAL
	FIXED SATELLITE		MOBILE SATELLITE		STANDARD FREQUENCY AND TIME SIGNAL SATELLITE

ACTIVITY CODE



Allocation of the Radio Spectrum

UNITED STATES FREQUENCY ALLOCATIONS THE RADIO SPECTRUM

RADIO SERVICES COLOR LEGEND

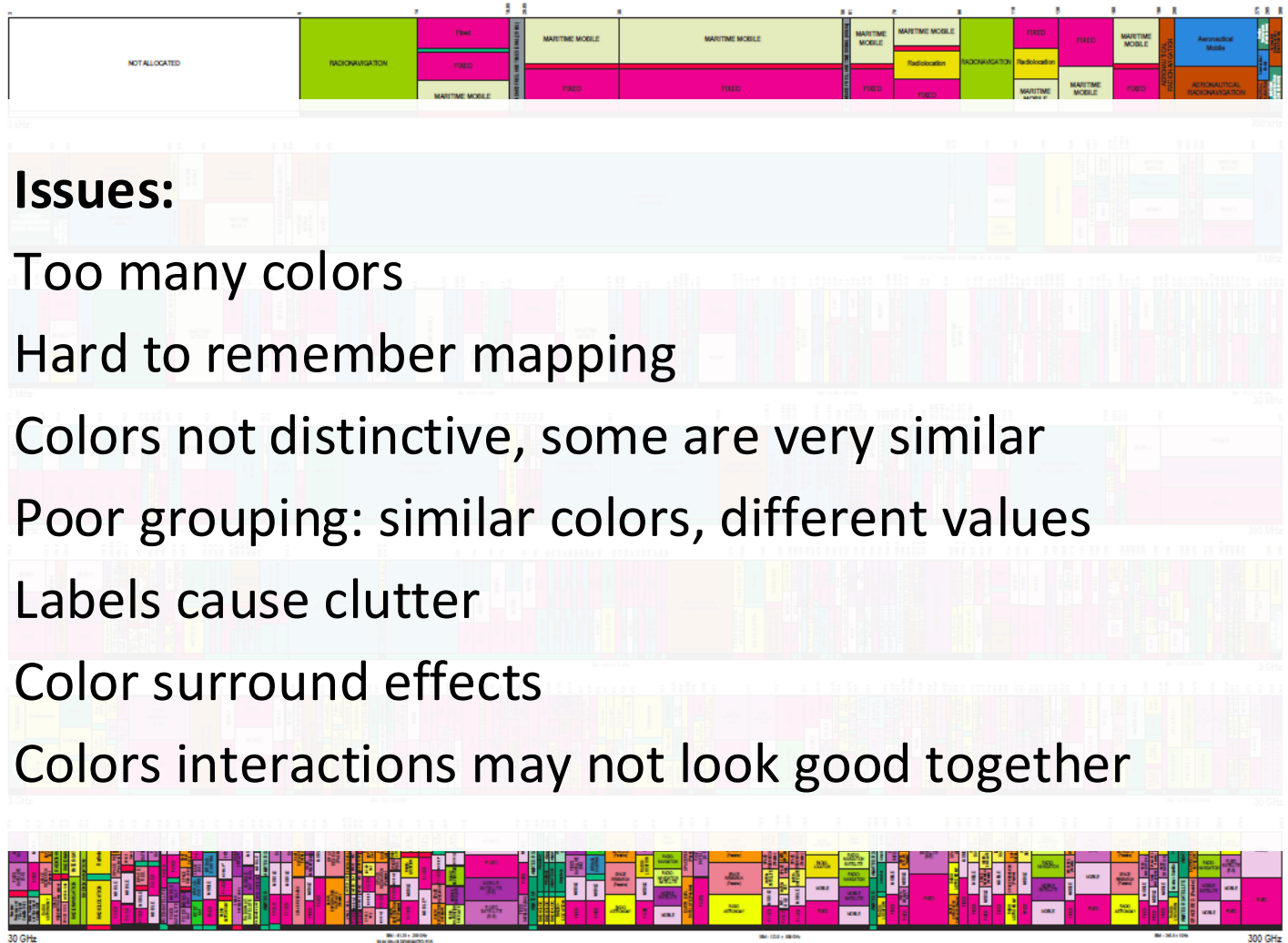
AERONAUTICAL MOBILE	INTER-SATELLITE	RADIO ASTRONOMY
AERONAUTICAL MOBILE SATELLITE	LAND MOBILE	RADIO DETERMINATION SATELLITE
AERONAUTICAL RADIO NAVIGATION	LAND MOBILE SATELLITE	RADIO LOCATION
NAVSTAR	NAVSTAR MOBILE	RADIO LOCATION SATELLITE
NAVSTAR SATELLITE	NAVSTAR MOBILE SATELLITE	RADIO NAVIGATION
BROADCASTING	NAVSTAR RADIO NAVIGATION	RADIO NAVIGATION SATELLITE
BROADCASTING SATELLITE	METEOROLOGICAL AID	SPACE OPERATION
EARTH EXPLORATION SATELLITE	METEOROLOGICAL SATELLITE	SPACE RESEARCH
FIXED	MOBILE	STANDARD FREQUENCY AND TIME SIGNAL
FIXED SATELLITE	MOBILE SATELLITE	STANDARD FREQUENCY AND TIME SIGNAL SATELLITE

ACTIVITY CODE

GOVERNMENT EXCLUSIVE	GOVERNMENT/NON-GOVERNMENT SHARED
NON-GOVERNMENT EXCLUSIVE	

ALLOCATION USAGE DESIGNATION

SERVICE	EXAMPLE	DESCRIPTION
Primary	FIXED	Capital Letters
Secondary	FIXED	Small Letters



Issues:

Too many colors

Hard to remember mapping

Colors not distinctive, some are very similar

Poor grouping: similar colors, different values

Labels cause clutter

Color surround effects

Colors interactions may not look good together

Palette Design & Color Names

Minimize overlap and ambiguity of colors.

Color Name Distance										Saliency	Name
0.00	1.00	1.00	1.00	0.98	1.00	1.00	1.00	1.00	0.20	 .47	blue 62.9%
1.00	0.00	1.00	0.97	1.00	1.00	1.00	1.00	0.96	1.00	 .90	orange 93.9%
1.00	1.00	0.00	1.00	1.00	1.00	1.00	1.00	0.90	0.99	 .67	green 79.8%
1.00	0.97	1.00	0.00	1.00	0.95	0.99	1.00	1.00	1.00	 .66	red 80.4%
0.98	1.00	1.00	1.00	0.00	0.96	0.91	0.97	1.00	0.99	 .47	purple 51.4%
1.00	1.00	1.00	0.95	0.96	0.00	0.97	0.93	0.98	1.00	 .37	brown 54.0%
1.00	1.00	1.00	0.99	0.91	0.97	0.00	1.00	1.00	1.00	 .58	pink 71.7%
1.00	1.00	1.00	1.00	0.97	0.93	1.00	0.00	1.00	1.00	 .67	grey 79.4%
1.00	0.96	0.90	1.00	1.00	0.98	1.00	1.00	0.00	1.00	 .18	yellow 31.2%
0.20	1.00	0.99	1.00	0.99	1.00	1.00	1.00	1.00	0.00	 .25	blue 25.4%
Average 0.97										.52	

Tableau-10

Palette Design & Color Names

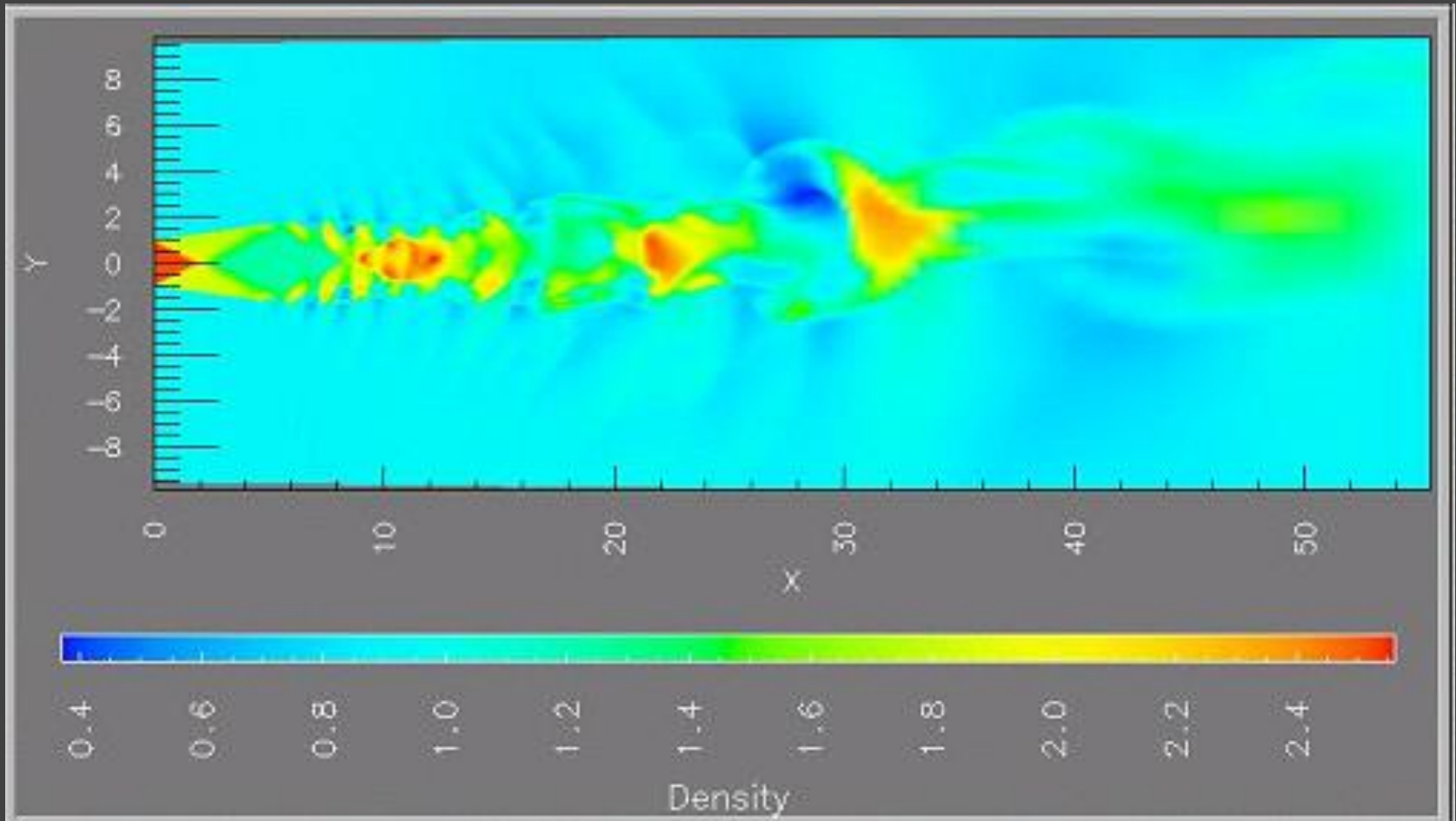
Minimize overlap and ambiguity of colors.

Color Name Distance

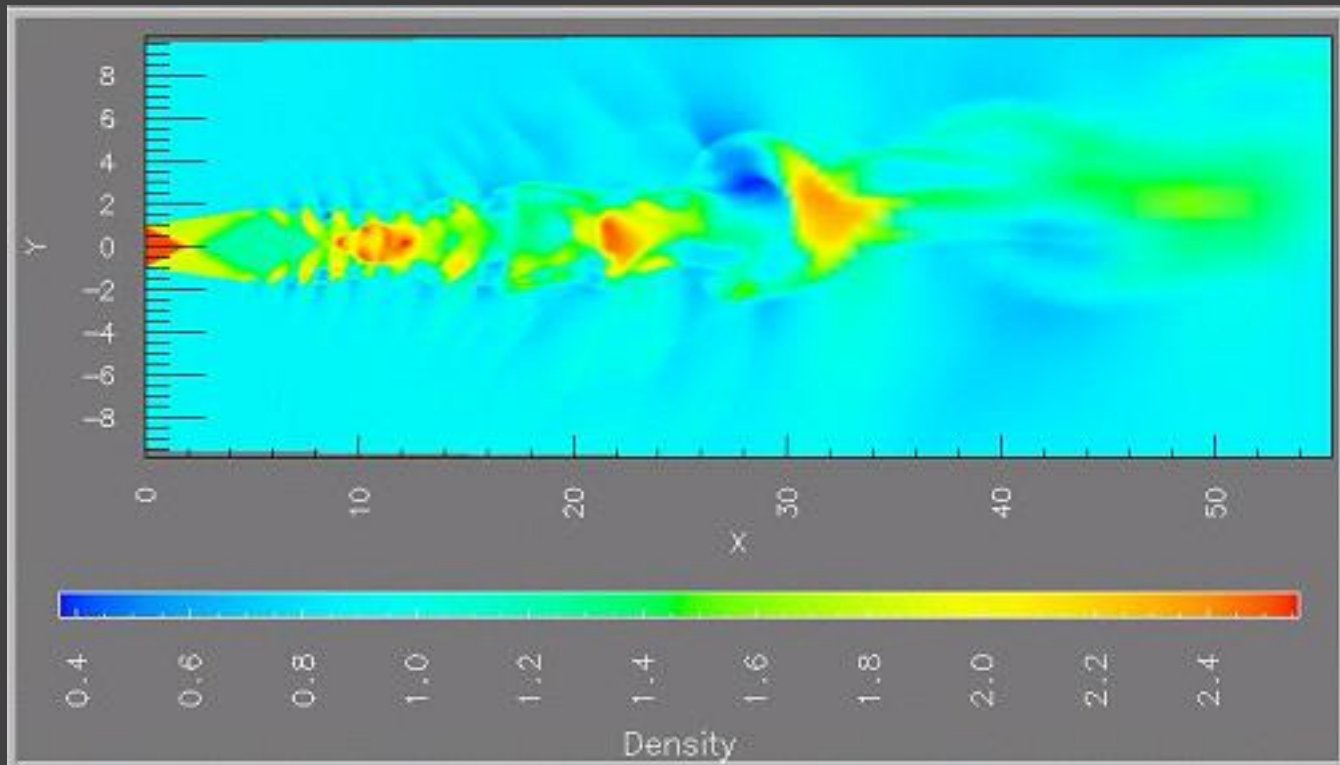
0.00	1.00	1.00	0.89	0.07	1.00	0.35	0.99	1.00	0.89		.30	blue 50.5%
1.00	0.00	0.99	1.00	1.00	0.92	1.00	0.84	0.98	0.99		.21	red 27.8%
1.00	0.99	0.00	1.00	0.98	1.00	1.00	1.00	0.17	1.00		.34	green 36.8%
0.89	1.00	1.00	0.00	0.98	1.00	0.71	0.93	1.00	0.32		.55	purple 67.3%
0.07	1.00	0.98	0.98	0.00	1.00	0.36	1.00	0.97	0.95		.20	blue 36.6%
1.00	0.92	1.00	1.00	1.00	0.00	1.00	0.97	0.99	1.00		.39	orange 51.9%
0.35	1.00	1.00	0.71	0.36	1.00	0.00	0.95	0.92	0.42		.13	blue 15.7%
0.99	0.84	1.00	0.93	1.00	0.97	0.95	0.00	0.98	0.85		.16	pink 29.4%
1.00	0.98	0.17	1.00	0.97	0.99	0.92	0.98	0.00	0.97		.12	green 21.7%
0.89	0.99	1.00	0.32	0.95	1.00	0.42	0.85	0.97	0.00		.30	purple 23.9%
Excel-10										Average	0.87	.27

Quantitative Color

Rainbow Color Maps

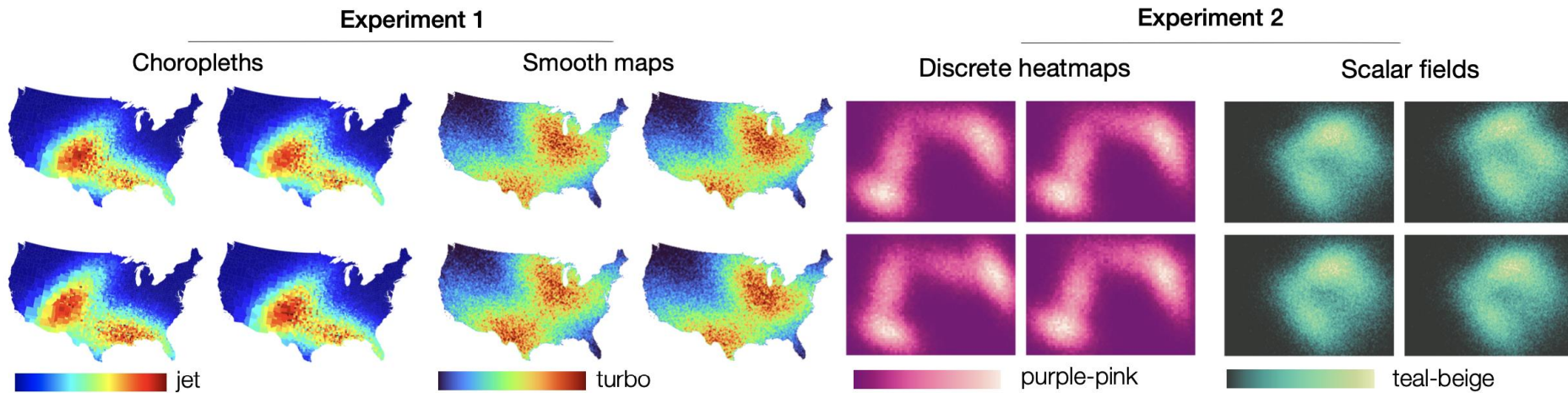


Be Wary of Naïve Rainbows!



1. Hues are not naturally ordered
2. People segment colors into classes, perceptual banding
3. Naive rainbows are unfriendly to color blind viewers
4. Some colors are less effective at high spatial frequencies

But rainbow helpful for inference?



Reda et al. '21: Color Nameability Predicts Inference Accuracy in Spatial Visualizations

Rainbow found ineffective for *value comparison* [Liu '18]...

...but color name salience found to improve performance on *inference task* of distinguishing distributions [Reda '21]

Task matters!

Steps, rather than Gradients?

number of data classes on your map
3 [learn more >](#)

the nature of your data
sequential [learn more >](#)

pick a color scheme: BuGn

multihue single hue

(optional) only show schemes that are:
☐ colorblind safe ☐ print friendly
☐ photocopy-able [learn more >](#)

pick a color system
229, 245, 249
153, 216, 201
44, 162, 95
☒ RGB ☐ CMYK ☐ HEX

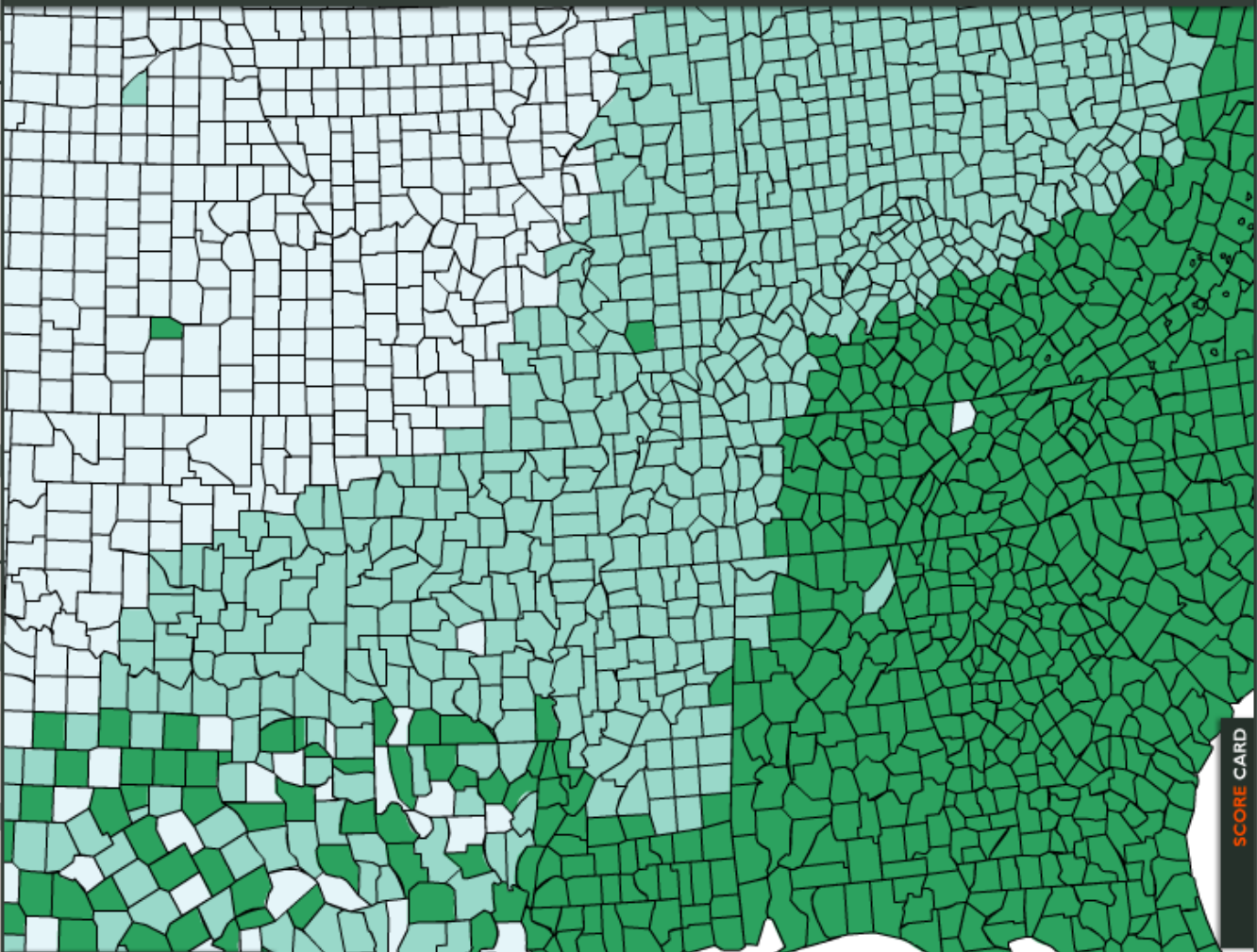
adjust map context
☐ roads ☐ cities ☒ borders

select a background
☒ solid color ☐ terrain

how to use | updates | credits

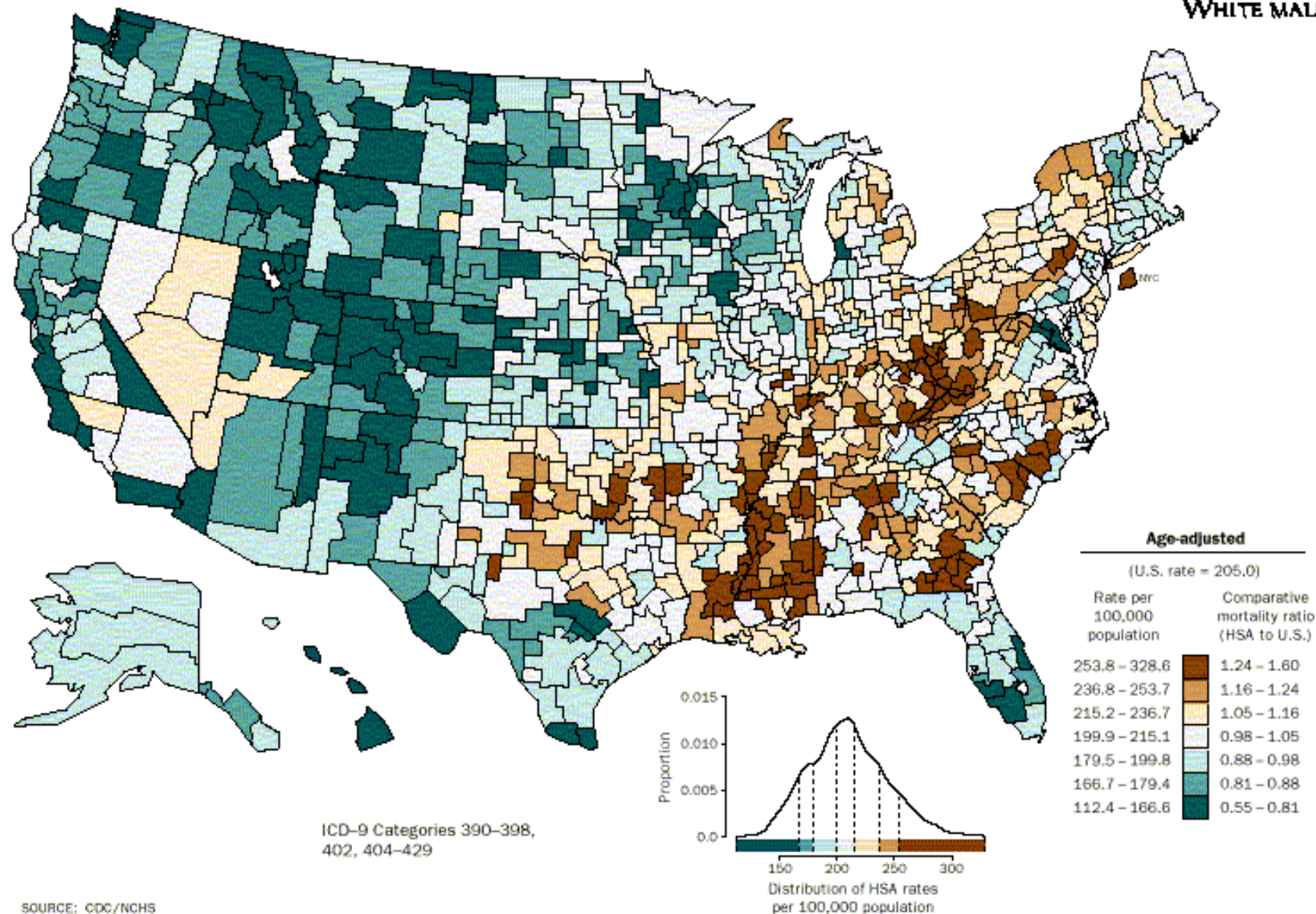
COLORBREWER 2.0

color advice for cartography



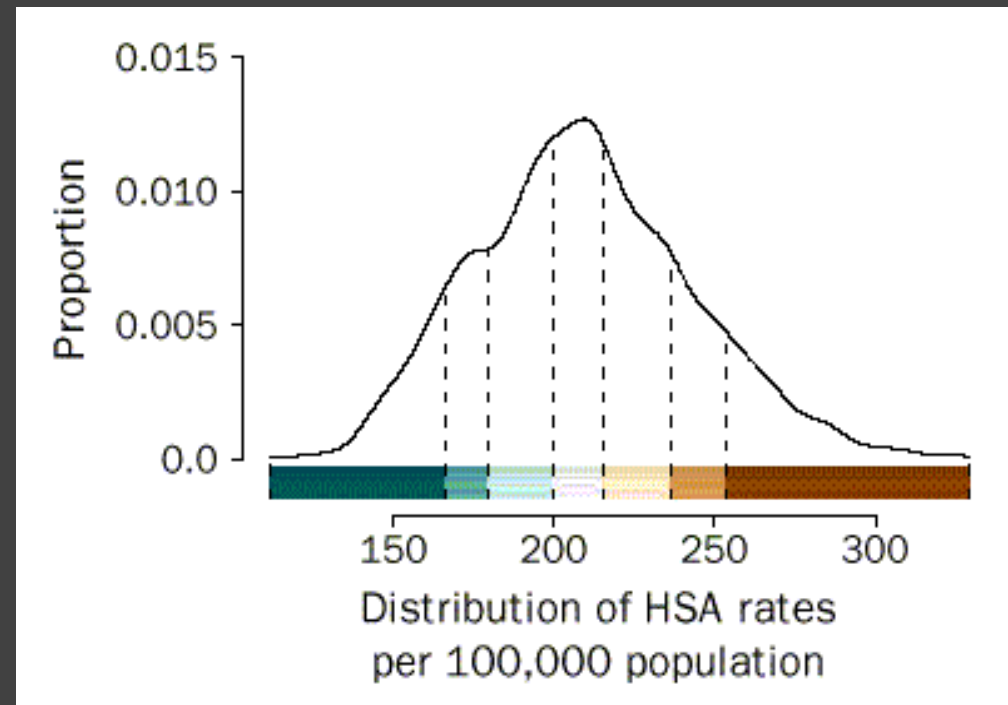
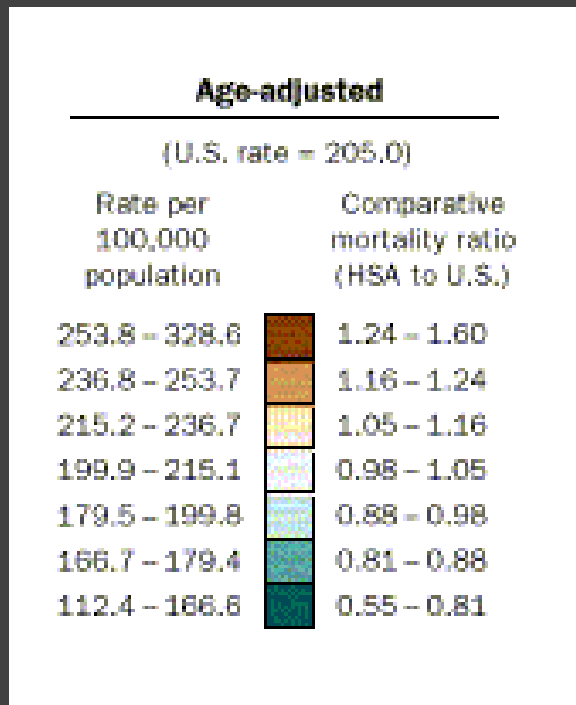
SCORE CARD

AGE-ADJUSTED DEATH RATES BY HSA, 1988-92

HEART DISEASE
WHITE MALE

SOURCE: CDC/NCHS

Classing Quantitative Data



Age-adjusted mortality rates for the United States.
Common option: break into 5 or 7 quantiles.

Classing Quantitative Data

1. Equal interval (arithmetic progression)
2. Quantiles (*recommended*)
3. Standard deviations
4. Clustering (Jenks' natural breaks / 1D K-Means)

Minimize within group variance

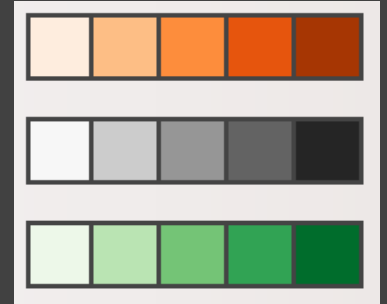
Maximize between group variance

Quantitative Color Encoding

Sequential color scale

Ramp in luminance, possibly also hue

Higher value -> darker color (or vice versa)



Quantitative Color Encoding

Sequential color scale

Ramp in luminance, possibly also hue

Higher value -> darker color (or vice versa)

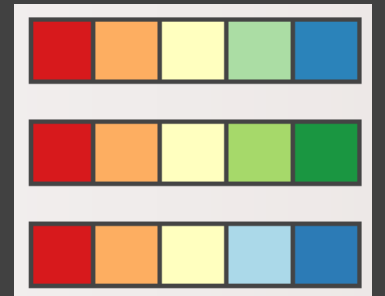


Diverging color scale

Useful when data has meaningful “midpoint”

Use neutral color (e.g., grey) for midpoint

Use saturated colors for endpoints



Quantitative Color Encoding

Sequential color scale

Ramp in luminance, possibly also hue

Higher value -> darker color (or vice versa)



Diverging color scale

Useful when data has meaningful “midpoint”

Use neutral color (e.g., grey) for midpoint

Use saturated colors for endpoints



Limit number of steps in color to 3-9

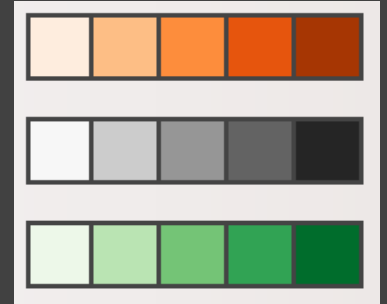
Why?

Quantitative Color Encoding

Sequential color scale

Ramp in luminance, possibly also hue

Higher value -> darker color (or vice versa)



Diverging color scale

Useful when data has meaningful “midpoint”

Use neutral color (e.g., grey) for midpoint

Use saturated colors for endpoints

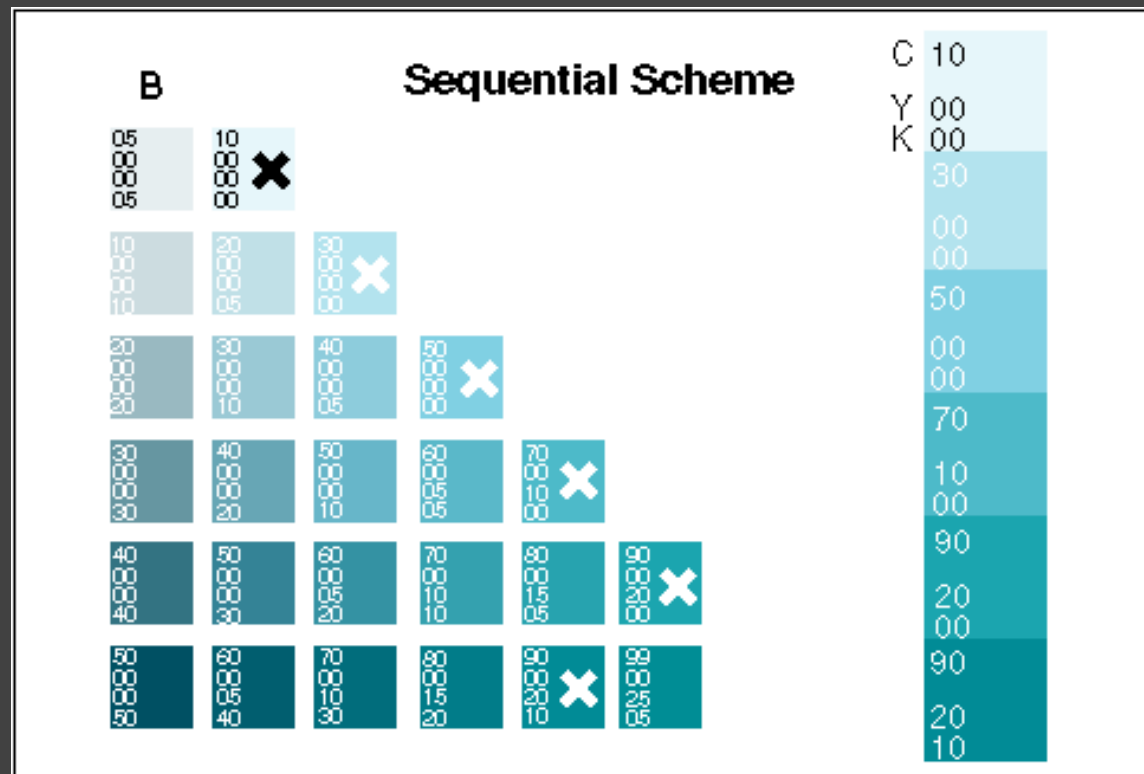


Limit number of steps in color to 3-9

Avoid simultaneous contrast, hold mappings in memory

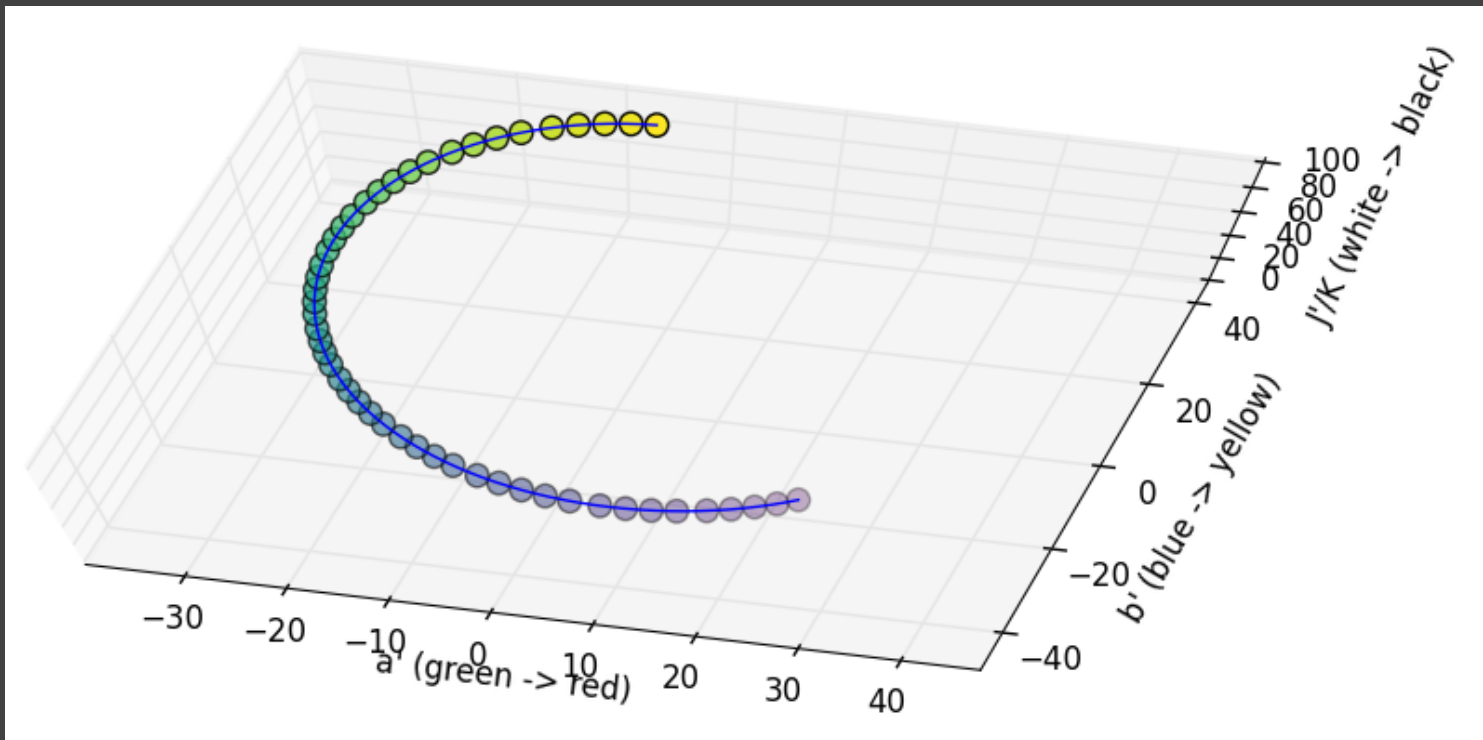
Sequential Scales: Single-Hue

Ramp primarily in luminance, subtle hue difference

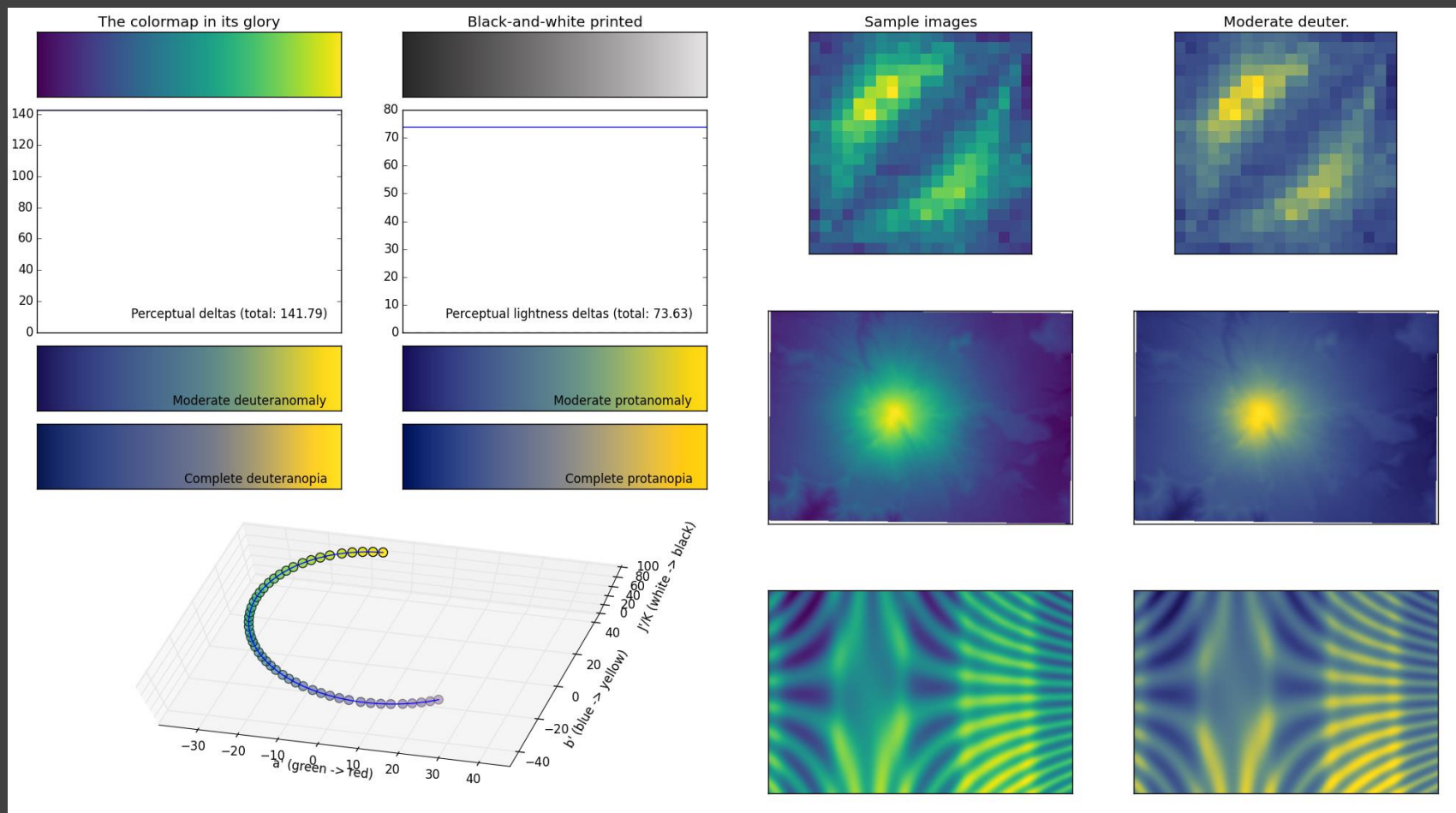


Sequential Scales: Multi-Hue

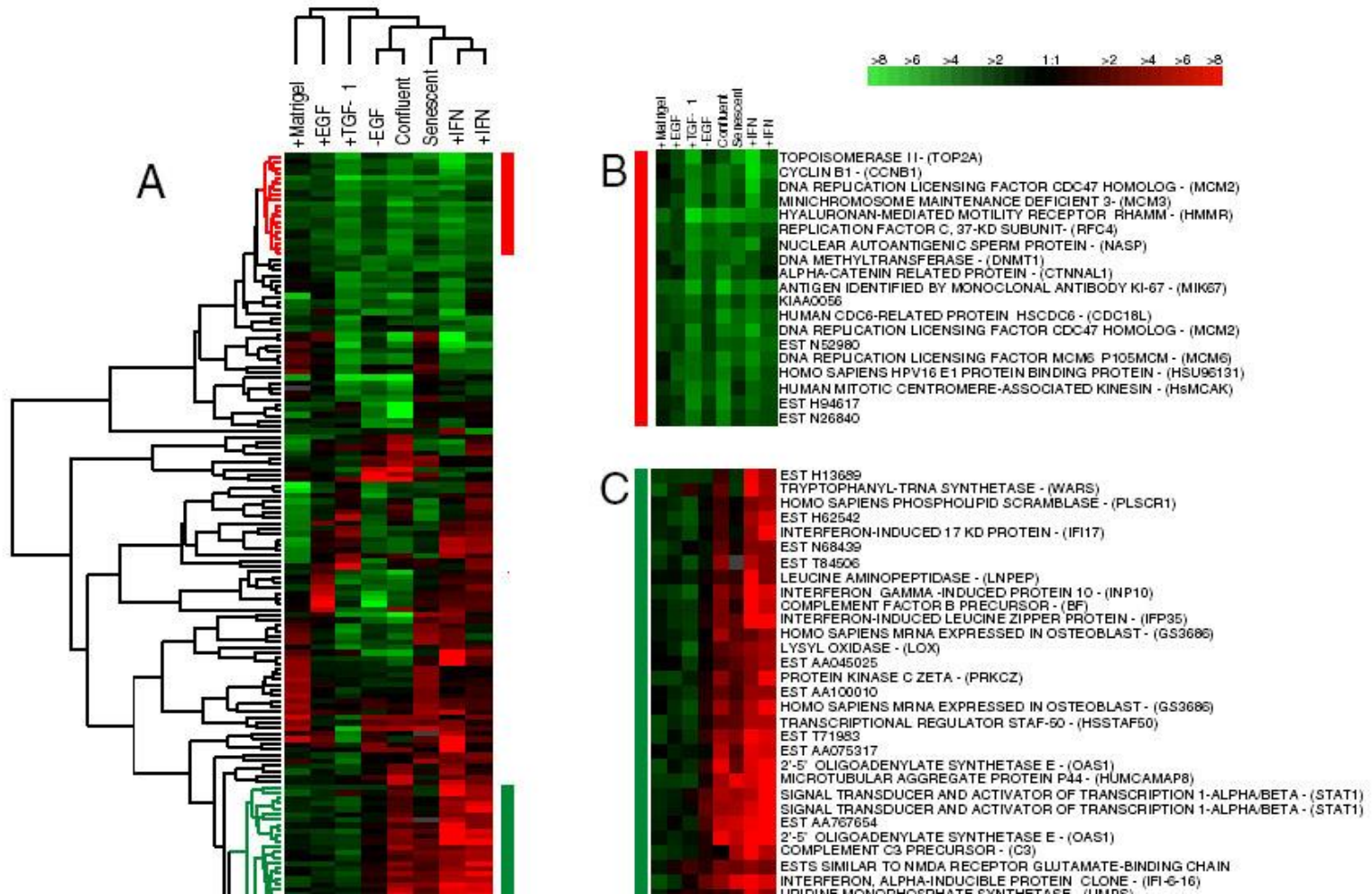
Ramp luminance & hue in perceptual color space
Avoid contrasts subject to color blindness!



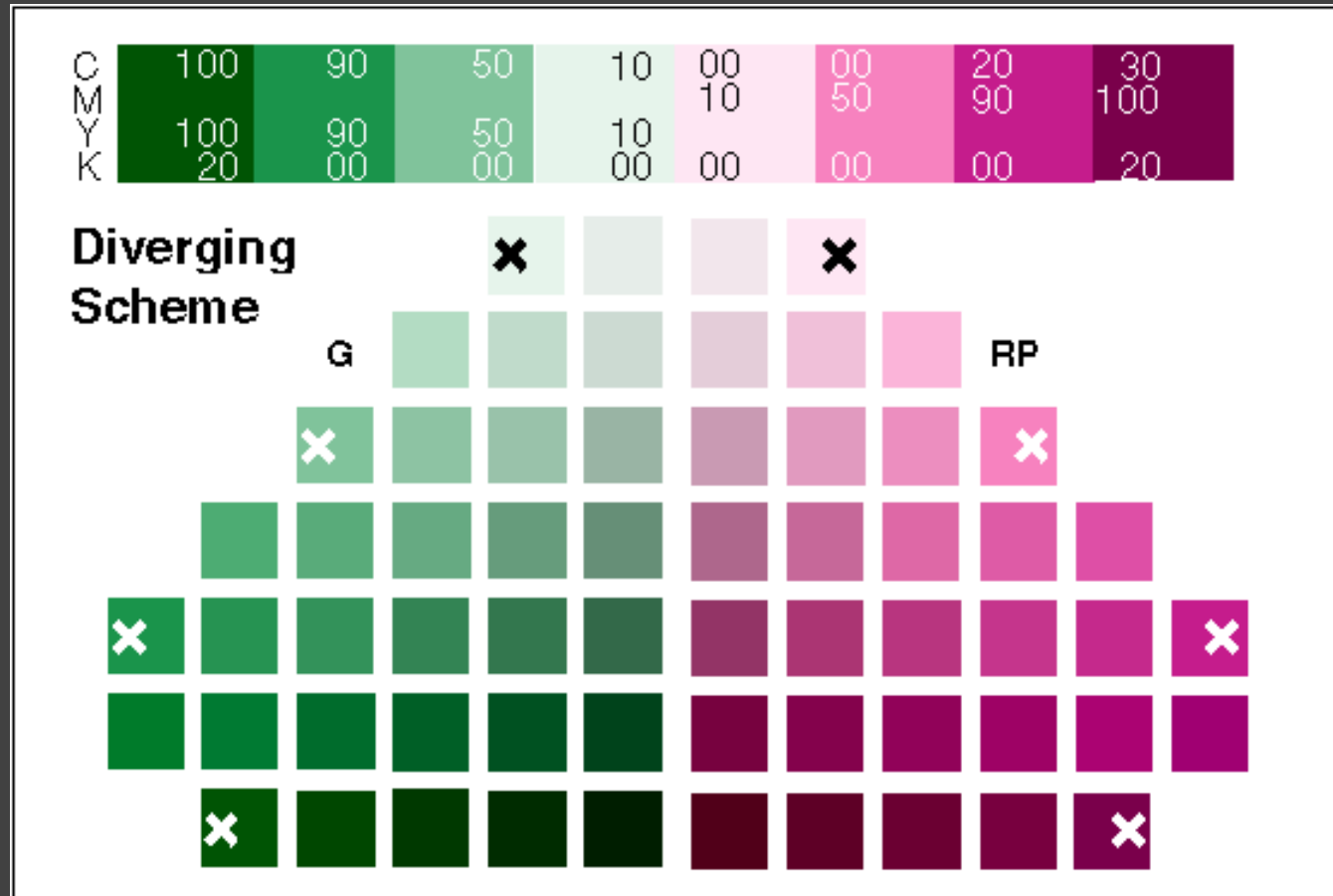
Sequential Scales: Multi-Hue



Diverging Color Scheme



Designing Diverging Scales



Designing Diverging Scales

Hue Transition

Carefully Handle Midpoint

Choose classes of values

Low, Average, High - Average should be gray

Critical Breakpoint

Defining value e.g., 0

Positive & negative should use different hues

Extremes saturated, middle desaturated

Hints for the Colorist

Use only a few colors (~6 ideal)

Colors should be distinctive and named

Strive for color harmony (natural colors?)

Use cultural conventions; appreciate symbolism

Get it right in black and white

Respect the color blind

Take advantage of perceptual color spaces

Color is cultural and a matter of taste!

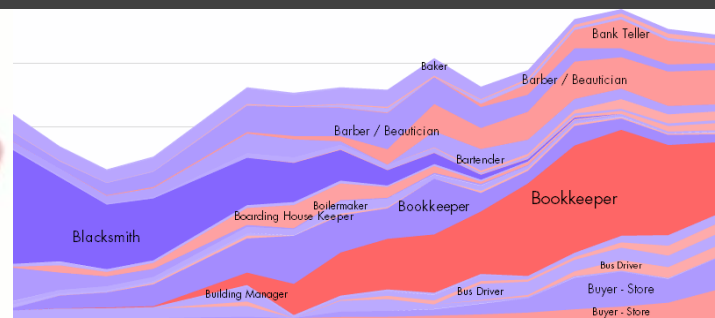
Administrivia

A3: Interactive Prototype

Create an interactive visualization. Choose a driving question for a dataset and develop an appropriate visualization + interaction techniques, then deploy your visualization on the web.

Due by *11:59pm* on **Tue, Feb 18.**

We encourage you to form teams of 2-4 people.

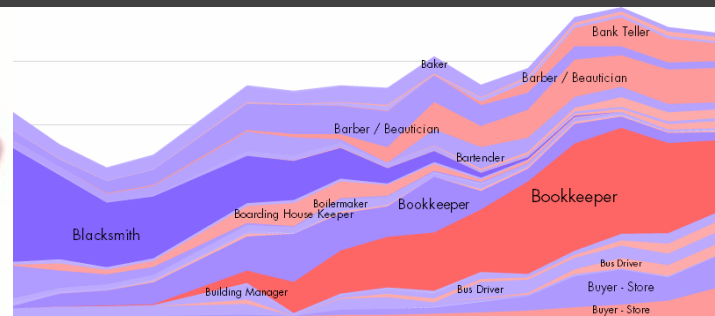


Requirements

Interactive. You must implement interaction methods! However, this is not only selection / filtering / tooltips. Also consider annotations or other narrative features to draw attention and provide additional context

Web-based. D3 is encouraged, but not required. Deploy visualization with GitHub pages or Observable.

Write-up. Provide design rationale on your web page.

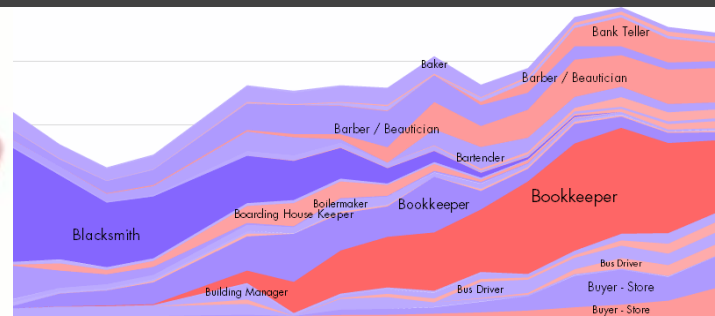


Interactive Prototype Tips

Start now. It will take longer than you think.

Keep it simple. Choose a *minimal* set of interactions that enables users to explore and generate interesting insights. Do not feel obligated to convey *everything* about the data: focus on a compelling subset.

Promote engagement. How do your chosen interactions reveal interesting observations?



Final Project Schedule

<i>Proposal</i>	<i>Wed Feb 19</i>
<i>Prototype</i>	<i>Tues Mar 4</i>
<i>Demo Video</i>	Tue Mar 11
<i>Video Showcase</i>	Thu Mar 13 (in class)

Deliverables Tue Mar 18

Logistics

Final project description posted online

Work in groups of up to 4 people