

$$F = \{f: \mathbb{N} \rightarrow \mathbb{N}\}$$

$$F_{\mathbb{R}} = \{f_i: \mathbb{N} \rightarrow \{0, 1\}\}$$

$\mathbb{R} \rightarrow$

$$3.14\dots \rightarrow 1110 \text{ ---}$$

binary. 14...

$$0.01$$

$$00000001\dots$$

f_1

f_2

f_3

\vdots

$$f(i) = 1 - f_i(i)$$

$F \rightarrow \mathbb{R}$

f	0	1	2	3
0	1	0	0	0
1	0	1	0	0
2	0	0	1	0
3	0	0	0	1

$$L \text{ rec} \iff \exists^D L = \{x \mid \exists y \langle x, y \rangle \in D\}$$

← try y 's one after another

$$M \implies D(x, y) = \text{accpt. of M on } x \text{ within } y \text{ steps}$$

$$L \text{ co-rec} \iff \exists \text{ dec } D \text{ st } L = \{x \mid \forall y \langle x, y \rangle \notin D\}$$

\bar{L}

$$\bar{L} = \{x \mid \exists y \langle x, y \rangle \in D\}$$

Harder still! :

$$L = \{x \mid \exists y \forall z \langle x, y, z \rangle \in D\}$$

Rec Enum of Decidables

	ϵ	a	b	ab	...
M_1	1	1	1	1	
M_2	0	0	0	0	
M_3					

$L = 01\dots$

L decidable? Yes: on i th input, run enumerators until i th TM is output, then run it on i , then do opposite.