

CSE 431  
Spring Quarter 2001  
Assignment 5  
Due Friday, May 4

All solutions should be neatly written or type set. All major steps in proofs and algorithms must be justified.

1. (10 points) Recall the following definition:

$$A_{TM} = \{\langle M, w \rangle : M \text{ accepts } w\}.$$

Show that if  $L$  is Turing recognizable then  $L \leq_m A_{TM}$ .

2. (10 points) We know (from Theorem 5.23) that if  $A \leq_m B$  and  $A$  is not Turing recognizable then neither is  $B$ . Use this and the fact that the complement of  $A_{TM}$  is not Turing recognizable to show that

$$D_{TM} = \{\langle M \rangle : L(M) \text{ is decidable}\}$$

is not Turing recognizable.