# CSE 427 Computational Biology Winter 2014 

3: BLAST, Alignment score significance

# BLAST: <br> Basic Local Alignment Search Tool <br> Altschul, Gish, Miller, Myers, Lipman, J Mol Biol 1990 

The most widely used comp bio tool
Which is better: long mediocre match or a few nearby, short, strong matches with the same total score?
score-wise, exactly equivalent
biologically, later may be more interesting, $\&$ is common
at least, if must miss some, rather miss the former
BLAST is a heuristic emphasizing the later
speed/sensitivity tradeoff: BLAST may miss former, but gains
greatly in speed

## BLAST: What

## Input:

A query sequence (say, 300 residues)
A data base to search for other sequences similar to the query (say, $10^{6}-10^{9}$ residues)
A score matrix $\sigma(r, s)$, giving cost of substituting $r$ for $s$ (\& perhaps gap costs)
Various score thresholds \& tuning parameters
Output:
"All" matches in data base above threshold
"E-value" of each

## Blast: demo

## E.g.

> http://expasy.org/sprot (or http://www.ncbi.nlm.nih.gov/blast/ ) look up MyoD
> go to blast tab
> paste in ID or seq for human MyoD
> set params (gapped=yes, blosum62,...)
> get top 100 (or 1000) hits

## BLAST: How

Idea: most interesting parts of the $D B$ have a good ungapped match to some short subword of the query
Break query into overlapping words $w_{i}$ of small fixed length (e.g. 3 aa or 11 nt )
For each $w_{i}$, find (empirically, $\sim 50$ ) "similar" words $\mathrm{v}_{\mathrm{ij}}$ with score $\sigma\left(w_{i}, v_{i j}\right)>$ thresh $_{1}$ (say, $1,2, \ldots$ letters different)
Look up each $v_{\mathrm{ij}}$ in database (via prebuilt index) --
i.e., exact match to short, high-scoring word

Grow each such "seed match" bidirectionally
Report those scoring > thresh ${ }_{2}$, calculate E-values

## BLAST: Example


$D B \longrightarrow$ ddgearlyk • • •
hits $\longrightarrow$ ddge 10
early 18

$$
\geq 10 \quad\left(\text { thresh }_{2}\right)
$$

## BLOSUM 62 (the " " " scores)

|  | $\mathbf{A}$ | $\mathbf{R}$ | $\mathbf{N}$ | $\mathbf{D}$ | $\mathbf{C}$ | $\mathbf{Q}$ | $\mathbf{E}$ | $\mathbf{G}$ | $\mathbf{H}$ | $\mathbf{I}$ | $\mathbf{L}$ | $\mathbf{K}$ | $\mathbf{M}$ | $\mathbf{F}$ | $\mathbf{P}$ | $\mathbf{S}$ | $\mathbf{T}$ | $\mathbf{W}$ | $\mathbf{Y}$ | $\mathbf{V}$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $\mathbf{A}$ | $\mathbf{4}$ | -1 | -2 | -2 | 0 | -1 | -1 | 0 | -2 | -1 | -1 | -1 | -1 | -2 | -1 | 1 | 0 | -3 | -2 | 0 |
| $\mathbf{R}$ | -1 | $\mathbf{5}$ | 0 | -2 | -3 | 1 | 0 | -2 | 0 | -3 | -2 | 2 | -1 | -3 | -2 | -1 | -1 | -3 | -2 | -3 |
| $\mathbf{N}$ | -2 | 0 | $\mathbf{6}$ | 1 | -3 | 0 | 0 | 0 | 1 | -3 | -3 | 0 | -2 | -3 | -2 | 1 | 0 | -4 | -2 | -3 |
| $\mathbf{D}$ | -2 | -2 | 1 | $\mathbf{6}$ | -3 | 0 | 2 | -1 | -1 | -3 | -4 | -1 | -3 | -3 | -1 | 0 | -1 | -4 | -3 | -3 |
| $\mathbf{C}$ | 0 | -3 | -3 | -3 | $\mathbf{9}$ | -3 | -4 | -3 | -3 | -1 | -1 | -3 | -1 | -2 | -3 | -1 | -1 | -2 | -2 | -1 |
| $\mathbf{Q}$ | -1 | 1 | 0 | 0 | -3 | $\mathbf{5}$ | 2 | -2 | 0 | -3 | -2 | 1 | 0 | -3 | -1 | 0 | -1 | -2 | -1 | -2 |
| $\mathbf{E}$ | -1 | 0 | 0 | 2 | -4 | 2 | $\mathbf{5}$ | -2 | 0 | -3 | -3 | 1 | -2 | -3 | -1 | 0 | -1 | -3 | -2 | -2 |
| $\mathbf{G}$ | 0 | -2 | 0 | -1 | -3 | -2 | -2 | $\mathbf{6}$ | -2 | -4 | -4 | -2 | -3 | -3 | -2 | 0 | -2 | -2 | -3 | -3 |
| $\mathbf{H}$ | -2 | 0 | 1 | -1 | -3 | 0 | 0 | -2 | $\mathbf{8}$ | -3 | -3 | -1 | -2 | -1 | -2 | -1 | -2 | -2 | $\mathbf{2}$ | -3 |
| $\mathbf{I}$ | -1 | -3 | -3 | -3 | -1 | -3 | -3 | -4 | -3 | $\mathbf{4}$ | $\mathbf{2}$ | -3 | 1 | 0 | -3 | -2 | -1 | -3 | -1 | 3 |
| $\mathbf{L}$ | -1 | -2 | -3 | -4 | -1 | -2 | -3 | -4 | -3 | 2 | $\mathbf{4}$ | -2 | 2 | 0 | -3 | -2 | -1 | -2 | -1 | 1 |
| $\mathbf{K}$ | -1 | 2 | 0 | -1 | -3 | 1 | 1 | -2 | -1 | -3 | -2 | $\mathbf{5}$ | -1 | -3 | -1 | 0 | -1 | -3 | -2 | -2 |
| $\mathbf{M}$ | -1 | -1 | -2 | -3 | -1 | 0 | -2 | -3 | -2 | 1 | $\mathbf{2}$ | -1 | $\mathbf{5}$ | 0 | -2 | -1 | -1 | -1 | -1 | 1 |
| $\mathbf{F}$ | -2 | -3 | -3 | -3 | -2 | -3 | -3 | -3 | -1 | 0 | 0 | -3 | 0 | $\mathbf{6}$ | -4 | -2 | -2 | 1 | 3 | -1 |
| $\mathbf{P}$ | -1 | -2 | -2 | -1 | -3 | -1 | -1 | -2 | -2 | -3 | -3 | -1 | -2 | -4 | $\mathbf{7}$ | -1 | -1 | -4 | -3 | -2 |
| $\mathbf{S}$ | 1 | -1 | 1 | 0 | -1 | 0 | 0 | 0 | -1 | -2 | -2 | 0 | -1 | -2 | -1 | $\mathbf{4}$ | 1 | -3 | -2 | -2 |
| $\mathbf{T}$ | 0 | -1 | 0 | -1 | -1 | -1 | -1 | -2 | -2 | -1 | -1 | -1 | -1 | -2 | -1 | 1 | $\mathbf{5}$ | -2 | -2 | 0 |
| $\mathbf{W}$ | -3 | -3 | -4 | -4 | -2 | -2 | -3 | -2 | -2 | -3 | -2 | -3 | -1 | 1 | -4 | -3 | -2 | $\mathbf{1 1}$ | $\mathbf{2}$ | -3 |
| $\mathbf{Y}$ | -2 | -2 | -2 | -3 | -2 | -1 | -2 | -3 | 2 | -1 | -1 | -2 | -1 | 3 | -3 | -2 | -2 | 2 | $\mathbf{7}$ | -1 |
| $\mathbf{V}$ | 0 | -3 | -3 | -3 | -1 | -2 | -2 | -3 | -3 | 3 | 1 | -2 | 1 | -1 | -2 | -2 | 0 | -3 | -1 | $\mathbf{4}$ |

## BLAST Refinements

"Two hit heuristic" -- need 2 nearby, nonoverlapping, gapless hits before trying to extend either
"Gapped BLAST" -- run heuristic version of SmithWaterman, bi-directional from hit, until score drops by fixed amount below max

PSI-BLAST -- For proteins, iterated search, using "weight matrix" (next week?) pattern from initial pass to find weaker matches in subsequent passes

Many others

## Significance of alignment scores

## Significance of Alignments

Is "42" a good score?
Compared to what?

Usual approach: compared to a specific "null model", such as "random sequences"

## Brief Review of Probability

## random variables

Discrete random variable: takes values in a finite or countable set, e.g.
$X \in\{1,2, \ldots, 6\}$ with equal probability
$X$ is positive integer $i$ with probability $2^{-i}$

Continuous random variable: takes values in an uncountable set, e.g.
$X$ is the weight of a random person (a real number)
$X$ is a randomly selected point inside a unit square
$X$ is the waiting time until the next packet arrives at the server

## pdf and cdf

$f(x)$ : the probability density function (or simply "density")

$P(X<a)=F(x)$ : the cumulative distribution function
$\mathrm{P}(\mathrm{a}<\mathrm{X}<\mathrm{b})=\mathrm{F}(\mathrm{b})-\mathrm{F}(\mathrm{a})$
Need $\int_{-\infty}^{+\infty} f(x) d x(=F(+\infty))=1$
A key relationship:
$f(x)=\frac{d}{d x} F(x)$, since $F(a)=\int_{-\infty}^{a} f(x) d x$,

## densities

Densities are not probabilities; e.g. may be > I

$$
P(x=a)=0
$$

$$
P(a-\varepsilon / 2 \leq X \leq a+\varepsilon / 2)=
$$

$$
F(a+\varepsilon / 2)-F(a-\varepsilon / 2)
$$

$$
\approx \varepsilon \cdot f(\mathrm{a})
$$


I.e., the probability that a continuous random variable falls at a specified point is zero
The probability that it falls near that point is proportional to the density; in a large random sample, expect more samples where density is higher (hence the name "density").
$X$ is a normal (aka Gaussian) random variable $X \sim N\left(\mu, \sigma^{2}\right)$

$$
\begin{aligned}
& f(x)=\frac{1}{\sigma \sqrt{2 \pi}} e^{-(x-\mu)^{2} / 2 \sigma^{2}} \\
& E[X]=\mu \quad \operatorname{Var}[X]=\sigma^{2}
\end{aligned}
$$

The Standard Normal Density Function



## Z-scores

$Z=(X-\mu) / \sigma=(X-$ mean $) /$ standard deviation
e.g.
$Z=+3$ means " 3 standard deviations above the mean"

Applicable to any distribution, and gives a rough sense of how usual/unusual the datum is.
If $X$ is normal $\left(\mu, \sigma^{2}\right)$ then $Z$ is normal $(0,1)$, and you can easily calculate (or look up in a table) just how unusual E.g., if normal, $\mathrm{P}(\mathrm{Z}$-score $\geq+3) \approx 0.001$

## Central Limit Theorem

If a random variable $X$ is the sum of many independent random variables, then X will be approximately normally distributed.

## Hypothesis Tests and P-values

## Hypothesis Tests

Competing models might explain some data E.g., you've flipped a coin 5 times, seeing HHHTH

Model 0 (The "null" model): $\quad P(H)=1 / 2$
Model 1 (The "alternate" model): $P(H)=2 / 3$

Which is right?
A possible decision rule: reject the null if you see 4 or more heads in 5 tries

## p-values



The $p$-value of such a test is the probability, assuming that the null model is true, of seeing data as extreme or more extreme than what you actually observed
E.g., we observed 4 heads; p-value is prob of seeing 4 or 5 heads in 5 tosses of a fair coin
Why interesting? It measures probability that we would be making a mistake in rejecting null.
Can analytically find $p$-value for simple problems like coins; often turn to simulation/permutation tests (introduced earlier) or to approximation (coming soon) for more complex situations
Usual scientific convention is to reject null only if $p$-value is $<0.05$; sometimes demand $p<0.05$ (esp. if estimates are inaccurate)

## Alignment Scores

## Distribution of alignment scores

A straw man: suppose I want a simple null model for alignment scores of, say MyoD versus random proteins of similar lengths. Consider this: Write letters of MyoD in one row; make a random alignment by filling $2^{\text {nd }}$ row with random permutation of the other sequence plus gaps.

```
MELLSPPLR...
uv---wxyz...
```

Score for column 1 is a random number from the M row of BLOSUM 62 table, column 2 is random from $E$ row, etc.

By central limit theorem, total score would be approximately normal

Permutation Score Histogram vs Gaussian



## Rethinking score distribution

Strawman above is ok: random permutation of letters \& gaps should give normally distributed scores.

But S-W doesn't stop there; it then slides the gaps around so as to maximize score, in effect taking the maximum over a huge number of alignments with same sequence but different gap placements.

## Overall Alignment Significance, I A Theoretical Approach: EVD

Let $X_{i}, 1 \leq i \leq N$, be indp. random variables drawn from some (nonpathological) distribution
Q. what can you say about distribution of $y=\operatorname{sum}\left\{X_{i}\right\}$ ?
A. y is approximately normally distributed (central limit theorem)
Q. what can you say about distribution of $y=\max \left\{X_{i}\right\}$ ?
A. it's approximately an Extreme Value Distribution (EVD)
[one of only 3 kinds; for our purposes, the relevant one is:]

$$
P(y \leq z) \approx \exp \left(-K N e^{-\lambda(z-\mu)}\right)
$$

For ungapped local alignment of seqs $x, y, N \sim|x| *|y|$
$\lambda, \mathrm{K}$ depend on score table \& gap costs, or can be estimated by curve-fitting random scores to (*). (cf. reading)

Normal (blue) / EVD (red)


Both mean 0, variance 1; EVD has "fat tail"


## EVD Pro/Con

## Pro:

Gives p-values for alignment scores

## Con:

It's only approximate
You must estimate parameters
Theory may not apply. E.g., known to hold for ungapped local alignments (like BLAST seeds). It is NOT proven to hold for gapped alignments, although there is strong empirical support.

## Overall Alignment Significance, II Empirical (via randomization)

You just searched with $x$, found "good" score for $x$ : $y$
Generate N random "y-like" sequences (say N=103-106)
Align $x$ to each \& score
If $k$ of them have better score than alignment of $x$ to $y$, then the (empirical) probability of a chance alignment as good as observed $x$ :y alignment is $(k+1) /(N+1)$
e.g., if 0 of 99 are better, you can say "estimated $p<.01$ "

How to generate "random y-like" seqs? Scores depend on:
Length, so use same length as y
Sequence composition, so uniform $1 / 20$ or $1 / 4$ is a bad idea; even background $p_{i}$ can be dangerous
Better idea: permute y N times

## Generating Random Permutations

$$
\text { for }(i=n-1 ; i>0 ; i--)\{
$$

j = random(0..i);
swap X[i] <-> X[j];
\}


All $n$ ! permutations of the original data equally likely: A specific element will be last with prob $1 / n$; given that, a specific other element will be next-to-last with prob $1 /(n-1), \ldots$; overall: $1 /(n!)$
C.f. http://en.wikipedia.org/wiki/Fisher-Yates shuffle and (for subtle way to go wrong) $\qquad$

## Permutation Pro/Con

## Pro:

Gives empirical p-values for alignments with characteristics like sequence of interest, e.g. residue frequencies
Largely free of modeling assumptions (e.g., ok for gapped...)
Con:
Can be inaccurate if your method of generating random sequences is unrepresentative
E.g., probably better to preserve di-, tri-residue statistics and/or other higher-order characteristics, but increasingly hard to know exactly what to model \& how
Slow
Especially if you want to assess low-probability p-values

## Summary

BLAST is a highly successful search/alignment heuristic. It looks for alignments anchored by short, strong, ungapped "seed" alignments
Assessing statistical significance of alignment scores is crucial to practical applications

Score matrices derived from "likelihood ratio" test of trusted alignments vs random "null" model
For gapless alignments, Extreme Value Distribution (EVD) is theoretically justified for overall significance of alignment scores; empirically ok in other contexts, too, e.g., for gapped alignments Permutation tests are a simple (but brute force) alternative

More on p-values and hypothesis testing

## P-values \& E-values

p-value: $P(s, n)=$ probability of a score more extreme than $s$ in a random target data base of size $n$
E-value: $\mathrm{E}(\mathrm{s}, \mathrm{n})=$ expected number of such matches
They Are Related:

```
\(E(s, n)=p n(\) where \(p=P(s, 1))\)
\(P(s, n)=1-(1-p)^{n}=1-(1-1 /(1 / p))^{(1 / p)(p n)} \approx 1-\exp (-p n)=1-\exp (-E(s, n))\)
\(E\) big \(\Leftrightarrow P\) big
    \(E=5 \Leftrightarrow P \approx .993\)
    \(E=10 \Leftrightarrow P \approx .99995\)
\(E\) small \(\Leftrightarrow P\) small
    \(E=.01 \Leftrightarrow P \approx E-E^{2} / 2+E^{3} / 3!\ldots \approx E\)
```

Both equally valid; E-value is perhaps more intuitively interpretable

## Hypothesis Testing: A Very Simple Example

Given: A coin, either fair $(p(H)=1 / 2)$ or biased $(p(H)=2 / 3)$
Decide: which
How? Flip it 5 times. Suppose outcome D $=$ HHHTH
Null Model/Null Hypothesis $\mathrm{M}_{0}$ : $\mathrm{p}(\mathrm{H})=1 / 2$
Alternative Model/Alt Hypothesis $\mathrm{M}_{1}$ : $\mathrm{p}(\mathrm{H})=2 / 3$
Likelihoods:

$$
\begin{aligned}
& \mathrm{P}\left(\mathrm{D} \mid \mathrm{M}_{0}\right)=(1 / 2)(1 / 2)(1 / 2)(1 / 2)(1 / 2)=1 / 32 \\
& \mathrm{P}\left(\mathrm{D} \mid \mathrm{M}_{1}\right)=(2 / 3)(2 / 3)(2 / 3)(1 / 3)(2 / 3)=16 / 243 \\
& \text { Likelihood Ratio: } \quad \frac{p\left(D \mid M_{1}\right)}{p\left(D \mid M_{0}\right)}=\frac{16 / 243}{1 / 32}=\frac{512}{243} \approx 2.1
\end{aligned}
$$

I.e., given data is $\approx 2.1 \mathrm{x}$ more likely under alt model than null model

## Hypothesis Testing, II

Log of likelihood ratio is equivalent, often more convenient
add logs instead of multiplying...
"Likelihood Ratio Tests": reject null if LLR > threshold LLR > 0 disfavors null, but higher threshold gives stronger evidence against
Neyman-Pearson Theorem: For a given error rate, LRT is as good a test as any (subject to some fine print).

## A Likelihood Ratio

Defn: two proteins are homologous if they are alike because of shared ancestry; similarity by descent

Suppose among proteins overall, residue $x$ occurs with frequency $p_{x}$
Then in a random alignment of 2 random proteins, you would expect to find $x$ aligned to $y$ with prob $p_{x} p_{y}$
Suppose among homologs, $x \& y$ align with prob $p_{x y}$
Are seqs $X \& Y$ homologous? Which is more likely, that the alignment reflects chance or homology? Use a likelihood ratio test.

$$
\sum_{i} \log \frac{p_{x_{i} y_{i}}}{p_{x_{i}} p_{y_{i}}}
$$

## Non-ad hoc Alignment Scores

Take alignments of homologs and look at frequency of $x-y$ alignments vs freq of $x, y$ overall Issues
biased samples
evolutionary distance

BLOSUM approach
Large collection of trusted alignments
(the BLOCKS DB)
Subset by similarity
BLOSUM62 $\Rightarrow \geq 62 \%$ identity

$$
\frac{1}{\lambda} \log _{2} \frac{p_{x y}}{p_{x} p_{y}}
$$

e.g. http://blocks.fhcrc.org/blocks-bin/getblock.pl?IPB002546

## BLOSUM 62

|  | $\mathbf{A}$ | $\mathbf{R}$ | $\mathbf{N}$ | $\mathbf{D}$ | $\mathbf{C}$ | $\mathbf{Q}$ | $\mathbf{E}$ | $\mathbf{G}$ | $\mathbf{H}$ | $\mathbf{I}$ | $\mathbf{L}$ | $\mathbf{K}$ | $\mathbf{M}$ | $\mathbf{F}$ | $\mathbf{P}$ | $\mathbf{S}$ | $\mathbf{T}$ | $\mathbf{W}$ | $\mathbf{Y}$ | $\mathbf{V}$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $\mathbf{A}$ | $\mathbf{4}$ | -1 | -2 | -2 | 0 | -1 | -1 | 0 | -2 | -1 | -1 | -1 | -1 | -2 | -1 | 1 | 0 | -3 | -2 | 0 |
| $\mathbf{R}$ | -1 | $\mathbf{5}$ | 0 | -2 | -3 | 1 | 0 | -2 | 0 | -3 | -2 | 2 | -1 | -3 | -2 | -1 | -1 | -3 | -2 | -3 |
| $\mathbf{N}$ | -2 | 0 | $\mathbf{6}$ | 1 | -3 | 0 | 0 | 0 | 1 | -3 | -3 | 0 | -2 | -3 | -2 | 1 | 0 | -4 | -2 | -3 |
| $\mathbf{D}$ | -2 | -2 | 1 | $\mathbf{6}$ | -3 | 0 | 2 | -1 | -1 | -3 | -4 | -1 | -3 | -3 | -1 | 0 | -1 | -4 | -3 | -3 |
| $\mathbf{C}$ | 0 | -3 | -3 | -3 | $\mathbf{9}$ | -3 | -4 | -3 | -3 | -1 | -1 | -3 | -1 | -2 | -3 | -1 | -1 | -2 | -2 | -1 |
| $\mathbf{Q}$ | -1 | 1 | 0 | 0 | -3 | $\mathbf{5}$ | 2 | -2 | 0 | -3 | -2 | 1 | 0 | -3 | -1 | 0 | -1 | -2 | -1 | -2 |
| $\mathbf{E}$ | -1 | 0 | 0 | 2 | -4 | $\mathbf{2}$ | $\mathbf{5}$ | -2 | 0 | -3 | -3 | 1 | -2 | -3 | -1 | 0 | -1 | -3 | -2 | -2 |
| $\mathbf{G}$ | 0 | -2 | 0 | -1 | -3 | -2 | -2 | $\mathbf{6}$ | -2 | -4 | -4 | -2 | -3 | -3 | -2 | 0 | -2 | -2 | -3 | -3 |
| $\mathbf{H}$ | -2 | 0 | 1 | -1 | -3 | 0 | 0 | -2 | $\mathbf{8}$ | -3 | -3 | -1 | -2 | -1 | -2 | -1 | -2 | -2 | 2 | -3 |
| $\mathbf{I}$ | -1 | -3 | -3 | -3 | -1 | -3 | -3 | -4 | -3 | $\mathbf{4}$ | 2 | -3 | 1 | 0 | -3 | -2 | -1 | -3 | -1 | 3 |
| $\mathbf{L}$ | -1 | -2 | -3 | -4 | -1 | -2 | -3 | -4 | -3 | 2 | $\mathbf{4}$ | -2 | 2 | 0 | -3 | -2 | -1 | -2 | -1 | 1 |
| $\mathbf{K}$ | -1 | 2 | 0 | -1 | -3 | 1 | 1 | -2 | -1 | -3 | -2 | $\mathbf{5}$ | -1 | -3 | -1 | 0 | -1 | -3 | -2 | -2 |
| $\mathbf{M}$ | -1 | -1 | -2 | -3 | -1 | 0 | -2 | -3 | -2 | 1 | 2 | -1 | $\mathbf{5}$ | 0 | -2 | -1 | -1 | -1 | -1 | 1 |
| $\mathbf{F}$ | -2 | -3 | -3 | -3 | -2 | -3 | -3 | -3 | -1 | 0 | 0 | -3 | 0 | $\mathbf{6}$ | -4 | -2 | -2 | 1 | 3 | -1 |
| $\mathbf{P}$ | -1 | -2 | -2 | -1 | -3 | -1 | -1 | -2 | -2 | -3 | -3 | -1 | -2 | -4 | $\mathbf{7}$ | -1 | -1 | -4 | -3 | -2 |
| $\mathbf{S}$ | 1 | -1 | 1 | 0 | -1 | 0 | 0 | 0 | -1 | -2 | -2 | 0 | -1 | -2 | -1 | $\mathbf{4}$ | 1 | -3 | -2 | -2 |
| $\mathbf{T}$ | 0 | -1 | 0 | -1 | -1 | -1 | -1 | -2 | -2 | -1 | -1 | -1 | -1 | -2 | -1 | 1 | $\mathbf{5}$ | -2 | -2 | 0 |
| $\mathbf{W}$ | -3 | -3 | -4 | -4 | -2 | -2 | -3 | -2 | -2 | -3 | -2 | -3 | -1 | 1 | -4 | -3 | -2 | $\mathbf{1 1}$ | 2 | -3 |
| $\mathbf{Y}$ | -2 | -2 | -2 | -3 | -2 | -1 | -2 | -3 | 2 | -1 | -1 | -2 | -1 | 3 | -3 | -2 | -2 | 2 | $\mathbf{7}$ | -1 |
| $\mathbf{V}$ | 0 | -3 | -3 | -3 | -1 | -2 | -2 | -3 | -3 | 3 | 1 | -2 | 1 | -1 | -2 | -2 | 0 | -3 | -1 | $\mathbf{4}$ |

## ad hoc Alignment Scores?

Make up any scoring matrix you like
Somewhat surprisingly, under pretty general assumptions**, it is equivalent to the scores constructed as above from some set of probabilities $p_{x y}$, so you might as well understand what they are

```
NCBI-BLAST: +1/-2 tuned for ~ 95% sequence identity
WU-BLAST: +5/-4 tuned for ~ 66% identity ("twilight zone")
```

[^0]
[^0]:    **e.g., average scores should be negative, but you probably want that anyway, otherwise local alignments turn into global ones, and some score must be $>0$, else best match is empty

