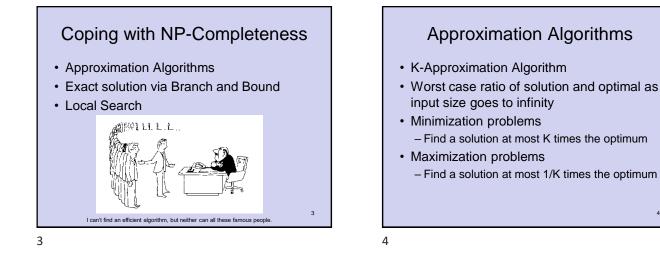
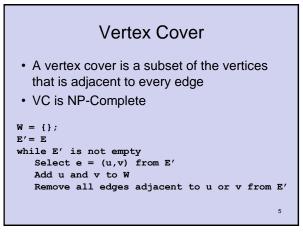
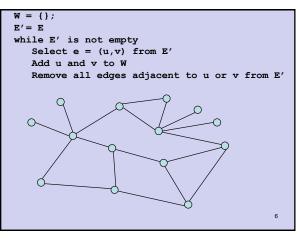


### Announcements

- Today, Coping with NP-Completeness
  Chapters 11 and 12
- Friday, Beyond NP-Completeness – Section 8.9, Chapter 9
- Homework 9, Due Friday, March 8
- Final exam,
  - Monday, March 11, 2:30-4:20 pm PDT
  - Comprehensive (~60% post midterm, ~40% pre midterm)
  - Old finals / answers on home page







## VC 2-Opt Bound

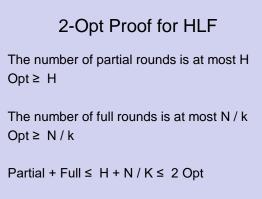
- When edge e = (u,v) is selected, neither u nor v is in W
- At least one of u or v must be in the VC to cover e
- Thus, at least ½ the vertices placed in W are necessary

## Multiprocessor Scheduling

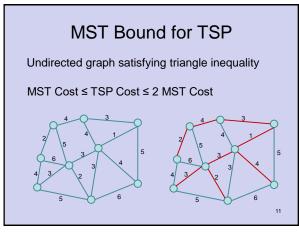
- Unit execution tasks
- Precedence graph
- K-Processors
- Polynomial time for k=2
- Open for k = constant
- NP-complete if k is part of the problem

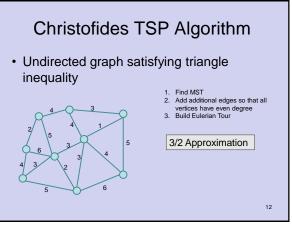
8

Highest level first is 2-Optimal Choose k items on the highest level Claim: number of rounds is at least twice the optimal. Suppose the maximum height of a task is H A partial round removes < k elements A full round removes k elements



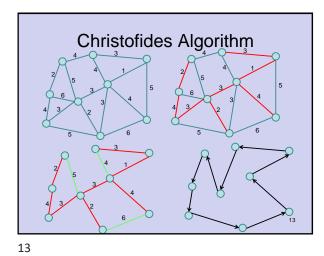
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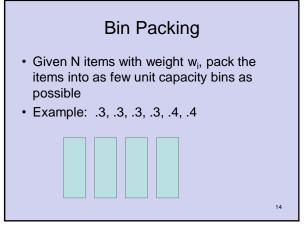




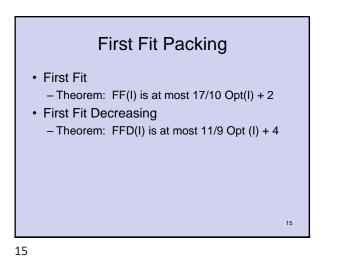
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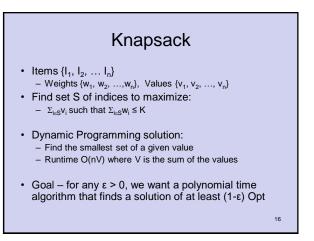
9





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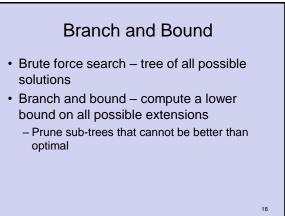


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# PTAS (Polynomial time approximation scheme)

- Idea for approximation algorithm\*
- Scale values so that ½ ≤ Opt ≤ 1
- Let ε = 2<sup>-k</sup>
- Round the values down to multiples of  $\epsilon^2$
- Solve the DP using ε<sup>2</sup> values
- Runtime O(nε<sup>2</sup>), Approximation (1-ε)

#### \*Some details omitted in dealing with very small items.

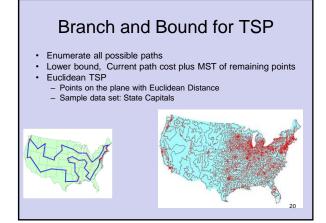


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## Branch and Bound for SAT

- Solving SAT by setting one variable at a time
- · Setting a literal to 1 removes the clause
- Setting a literal to 0 removes the literal – Removing the last literal kills the subtree
- · Heuristics for variable ordering
- Very important algorithms in practice, especially for software verification

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# Enhancements to Local Search

- Randomized Local Search
  Start from lots of places
- · Metropolis Algorithm
  - Choose random neighbor
    - Move if cheaper
    - If worse, move with some probability
- Simulated Annealing
  - Like Metropolis, but adjust probabilities to simulate cooling

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