

CSE 421 Introduction to Algorithms

Richard Anderson Winter 2024 Lecture 6 – Greedy Algorithms II

Announcements

- Today's lecture - Kleinberg-Tardos, 4.2, 4.3
- Friday

 Kleinberg-Tardos, 4.4, 4.5



- Averages of 5 runs
- Much better for M than W
- Why is it better for M?
- What is the growth of mrank and w-rank as a function of n?

n	m-rank	w-rank
500	5.10	98.05
500	7.52	66.95
500	8.57	58.18
500	6.32	75.87
500	5.25	90.73
500	6.55	77.95
1000	6.80	146.93
1000	6.50	154.71
1000	7.14	133.53
1000	7.44	128.96
1000	7.36	137.85
1000	7.04	140.40
2000	7.83	257.79
2000	7.50	263.78
2000	11.42	175.17
2000	7.16	274.76
2000	7.54	261.60
2000	9.20	246.62

Approximation Algorithms Compare solution of approximation

- Compare solution of approximation algorithm with the optimal algorithm
 - Earliest deadline first
 - Earliest starttime first
 - Shortest interval first
 - Fewest conflicts first

Scheduling Intervals

- · Given a set of intervals
 - What is the largest set of non-overlapping intervals
 - Compare heuristics with optimal
- · Suppose the n intervals are "random"
 - What is the expected number of independent intervals
 - Determine [x,y] by
 - x = randomDouble(0, 1.0)
 - y = randomDouble(x, 1.0)



Greedy Algorithms

- Solve problems with the simplest possible algorithm
- The hard part: showing that something simple actually works
- Today's problems (Sections 4.2, 4.3)
 - Homework Scheduling
 - Optimal Caching
 - Subsequence testing

Homework Scheduling

- · Tasks to perform
- · Deadlines on the tasks
- · Freedom to schedule tasks in any order
- · Can I get all my work turned in on time?
- If I can't get everything in, I want to minimize the maximum lateness

Scheduling tasks

- · Each task has a length t_i and a deadline d_i
- All tasks are available at the start
- One task may be worked on at a time
- All tasks must be completed
- Goal minimize maximum lateness
 Lateness: L_i = f_i − d_i if f_i ≥ d_i





















Result

• Earliest Deadline First algorithm constructs a schedule that minimizes the maximum lateness

Homework Scheduling



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