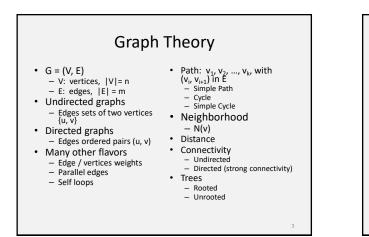
## CSE 421 Introduction to Algorithms

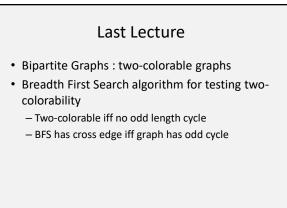
Winter 2024 Lecture 4

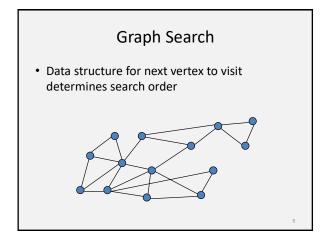
#### Announcements

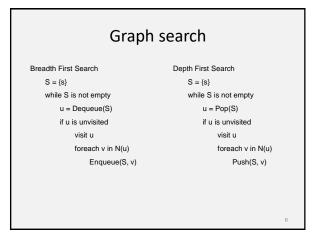
- Reading

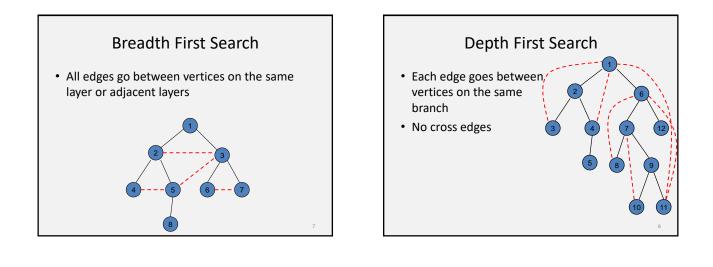
   Start on Chapter 4
- Homework due tonight, new homework available
- Class Friday???
- No class next Monday (MLK)

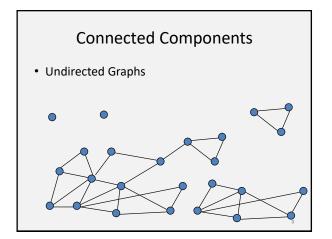


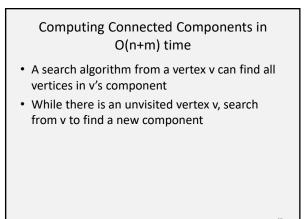


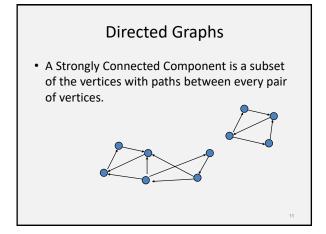


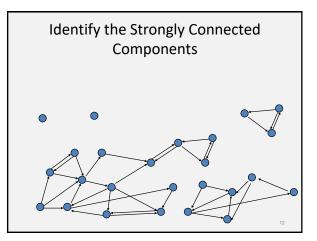






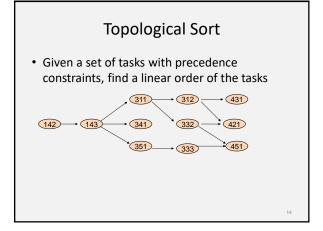


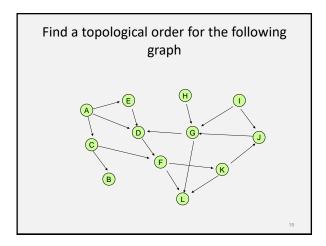


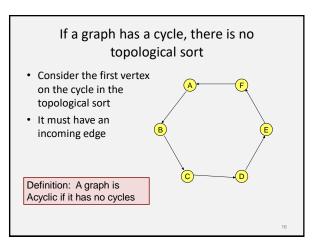


# Strongly connected components can be found in O(n+m) time

- But it's tricky!
- Simpler problem: given a vertex v, compute the vertices in v's scc in O(n+m) time

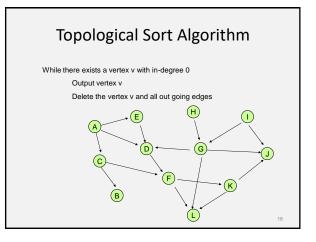






## Lemma: If a (finite) graph is acyclic, it has a vertex with in-degree 0

- Proof:
  - Pick a vertex v<sub>1</sub>, if it has in-degree 0 then done
  - If not, let  $(v_2, v_1)$  be an edge, if  $v_2$  has in-degree 0 then done
  - If not, let  $(v_3, v_2)$  be an edge . . .
  - If this process continues for more than n steps, we have a repeated vertex, so we have a cycle



### Details for O(n+m) implementation

- Maintain a list of vertices of in-degree 0
- Each vertex keeps track of its in-degree
- Update in-degrees and list when edges are removed

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• m edge removals at O(1) cost each