# CSE 421 Section 10

#### **Final Review**

#### **Announcements & Reminders**

#### • HW8

- Was due yesterday, Wednesday 12/4
- Final review with Professor Beame: Sunday, 12/8 @ TBA on Zoom
  - He will go over the practice final, so try it before the session if you can
- The final exam is on Monday, 12/9 @ 2:30-4:45 @ CSE2 G20
  - If you are sick the day of the exam, let us know and we will schedule a makeup
- Course evaluations are due Sunday, 12/8 @ 11:59pm
  - Section evaluations are due Monday, 12/9 @ 11:59pm

# Final exam format

- Similar to midterm exam, but longer
  - A sample final is available on Ed
- 135 minutes
- You will be given a standard reference sheet
  - Is expanded from the midterm, attached to sample final on Ed
- You may bring one sheet of double sided 8.5x11" paper containing your own handwritten notes.
  - Must write name, student number, and UW NetID
  - Must turn in with exam
  - If you want to access your midterm notes sheet, go to Prof. Beame's OH

# Today's plan

1. (35 min) 6 stations around the room with practice problems

(focused on second half of course, but exam is cumulative)

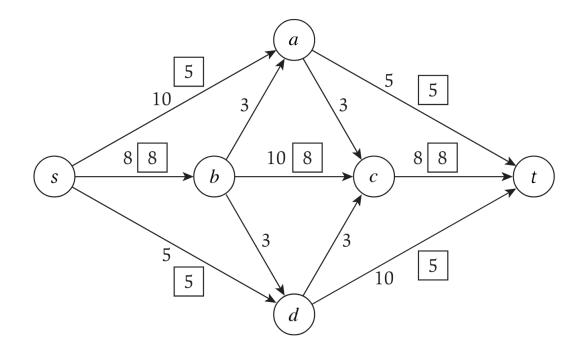
- Station 1: Short answer
- Station 2: Dynamic programming\*
- Station 3: Network flow
- Station 4: Linear programming\*
- Station 5: Reduction
- Station 6: Bonus problem
- 1. (10 min) Go over some of these problems

\*the problem at this station was an extra problem on a previous section handout

#### **Problems**



In the network flow below, is the depicted flow a maximum flow?



Recall Interval Scheduling: Given a collection of intervals and an integer k, determine if the collection contains at least k nonoverlapping intervals.

i. Does Interval Scheduling  $\leq_p$  Vertex Cover?

Recall Interval Scheduling: Given a collection of intervals and an integer k, determine if the collection contains at least k nonoverlapping intervals.

ii. Does Independent Set  $\leq_p$  Interval Scheduling?

A greedy attempt at Set Cover is:

**while** there exists an uncovered object **do** choose a set that covers the most number of still-uncovered objects

Suppose you are given an instance where every set contains exactly 2 elements. Then this algorithm returns a set cover that is at most a factor 2 larger than the minimum.

# Problem 2 – Dynamic programming

Given two strings,  $s = s_1, ..., s_m$  with length m and  $t = t_1, ..., t_n$  with length n, find the length of their longest common subsequence.

### Problem 3 – Network flows

The bank has  $C_j$  of currency j, and the exchange rate is  $R_j$  of currency j for every 1 Franc. Trader i has  $T_i$  Francs to convert and is willing to convert between  $L_{ij}$  and  $H_{ij}$  of their Francs to currency j. Determine if the bank can satisfy all requests, and if so, how to maximize the amount of Francs it collects.

# Problem 4 – Linear programming

There are k groups and  $m_i$  voters in group i, of which  $a_i$  are already voting for you. If you spend \$1000 advertising issue j, then  $d_{ij}$  more voters in group i will vote for you. Determine the minimum spending so that at least half of each group votes for you.

# **Problem 5 – Reduction**

A Hamiltonian path/cycle is a path/cycle that visits every vertex exactly once. Suppose that HamiltonianPath is NP-hard. Show that HamiltonianCycle is NP-hard.

### Problem 6 – Bonus problem

In a country with *n* states and  $p_i$  people voting in state *i*, the winner of state *i* receives  $v_i$  electoral college votes. In a two-candidate election with no state-level ties, determine the minimum percent of the total popular vote necessary to win at least  $V = \lfloor (\sum_i v_i)/2 \rfloor + 1$  electoral votes.