### P (stands for "Polynomial")

The set of all decision problems that have an algorithm that runs in time  $O(n^k)$  for some constant k (on input of size n).

#### NP (stands for "nondeterministic polynomial")

The set of all decision problems such that for every YES-instance (of size n), there is a certificate (of size  $O(n^k)$ ) for that instance which can be verified in polynomial time.

#### **NP-hard**

The problem B is NP-hard if for all problems A in NP, A reduces to B.

#### **NP-Complete**

The problem B is NP-complete if B is in NP and B is NP-hard

# If we had a nondeterministic computer...

Can you think of a polynomial time algorithm on a nondeterministic computer to:

Solve 2-COLOR?

Solve 3-COLOR?

## What's 3-SAT?

**Input**: A list of Boolean variables  $x_1, ..., x_n$ 

"AND" of "ORs"

A outside parens

V inside parens

An expression in Conjunctive Normal Form, where each clause has exactly 3 literals.

One of the

Something like:

One of the subexpressions inside parens

 $(z_i \lor z_j \lor z_k) \land (z_i \lor z_\ell \lor z_a) \land \cdots \land (z_a \lor z_b \lor z_c)$ 

Where z is a "literal" a variable or the negation of a variable  $(x_i, \neg x_j, \text{ etc.})$ .

**Output**: true if there is a setting of the variables where the expression evaluates to true, false otherwise.

Why is it called 3-SAT? 3 because you have 3 literals per clause SAT is short for "satisfiability" can you satisfy all of the constraints?

