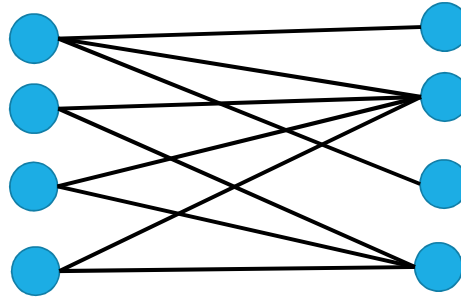


## A (possibly) simple problem

Design an algorithm to find a maximum matching on a bipartite graph.  
(*hint*: what if the vertices on one side are chores and the other are housemates).



## Algorithm for Bipartite Matching

Modify the (undirected) graph  $G$  into the network flow graph.

Find a maximum flow, taking all edges of  $G$  which have flow.

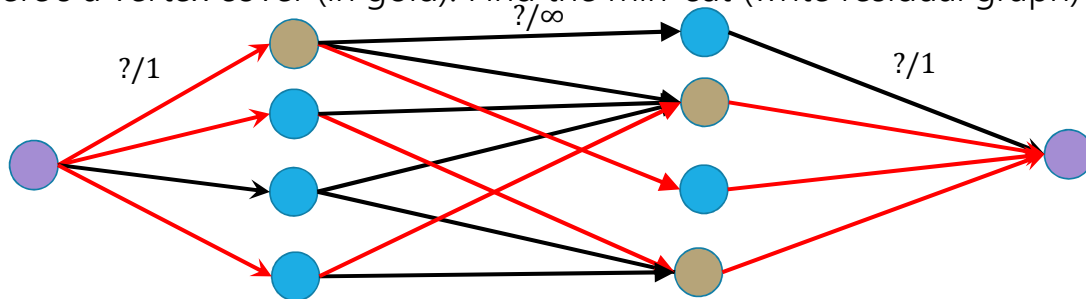
Is it correct?

The set of edges found should be a matching.

There should be no larger matching.

## Vertex Cover

Here's a vertex cover (in gold). Find the min-cut (write residual graph)



## Vertex Cover

Is  $A_T \cup B_S$  **always** a vertex cover? If so, how big is it?

There are 4 potential kinds of edges. Which kind is a problem for the vertex cover? Can they all exist?

$A_S$  to  $B_S$

$A_S$  to  $B_T$

$A_T$  to  $B_S$

$A_T$  to  $B_T$

