

Claim: If G has no cycle \Rightarrow it has a vertex of $deg \leq 1$.

PF: by contradiction!

Supp all vertices of G have $deg \geq 2$

Start with a vertex v_1

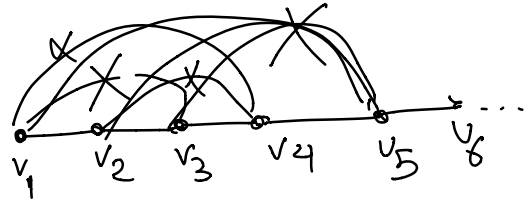
Say v_2 is a neighbor

$deg(v_2) \geq 2 \Rightarrow v_2$ has a neighbor v_3

$deg(v_3) \geq 2 \Rightarrow v_3$ has a neighbor $\neq v_2$, it cannot be v_1 (get a cycle) so it is v_4 .

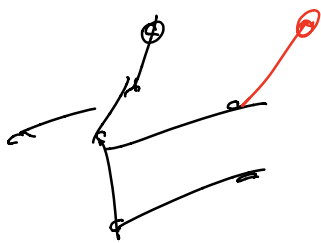
$deg(v_4) \geq 2 \Rightarrow v_4$ has a neighbor $\neq v_3$, cannot be v_1, v_2 (cycle) so it is v_5 and so on.

But this must stop BC. G has finitely many vertices. so at some point we get a cycle contradiction



$$|E| = n = \frac{n(n+1)}{2}$$

Every tree with n vertices has $n-1$ edges



Instead of adding delete