

Claim: Every woman gets matched to her most valued partner in GS. ( $S^*$ )

Pf. By contradiction.

Supp  $\exists w$  gets matched to  $m$  in  $S^*$

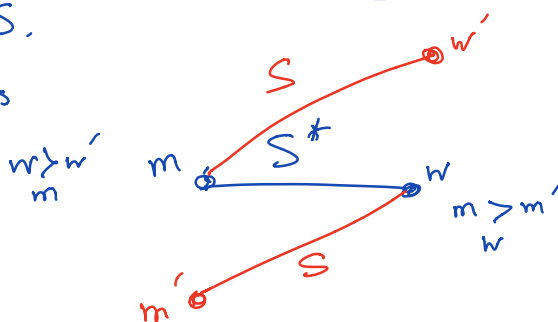
$m$  is not  $w$ 's most valued partner  $\Rightarrow \exists$  stable matching  $S$

s.t.  $w$  gets matched to  $m'$  and  $\boxed{m \succ m'}$   
 $w$

Say  $w'$  is  $m$ 's partner in  $S$ .

I claim  $w \succ w'$ . BC  $S^*$  is man-optimal.

$\Rightarrow (m, w)$  is an unstable pair for  $S$ . Contradiction!



Order  $\sqrt[n]{n^n}$ ,  $n^{5/3}$ ,  $2^{\sqrt{2n}}$ ,  $2^n$ ,  $\frac{n^2}{\sqrt{2n}}$

Rule for  $\log$ :

$$\log a \cdot b = \log a + \log b$$

$$\log a^b = b \cdot \log a$$

$$\log n^{5/3} = \frac{5}{3} \log n \quad (2)$$

$$\log 2^{\sqrt{2n}} = \sqrt{2n} \cdot \log 2 = \sqrt{2n} \quad (1)$$

$$\log 2^n = n \cdot \log 2 = n \quad (4)$$

$$\log \sqrt[n]{n^n} = \log (n^n)^{1/2} = \frac{1}{2} \log n^n = \frac{1}{2} \cdot n \cdot \log n \quad (5)$$

$$\log \frac{n^2}{\sqrt{2n}} = \log n^2 - \log \sqrt{2n} = 2 \log n - \frac{1}{2} \log 2n \quad (3)$$

