## **CSE 421: Introduction to** Algorithms

## **Greedy Algorithms**

Winter 2005 Paul Beame



## **Greedy Algorithms**

- Hard to define exactly but can give general properties
  - n Solution is built in small steps
  - Decisions on how to build the solution are made to maximize some criterion without looking to the future
    - Want the 'best' current partial solution as if the current step were the last step
- May be more than one greedy algorithm using different criteria to solve a given problem















- Only eliminate incompatible requests as needed
  - Walk along array of requests sorted by finish times skipping those whose start time is before current latest finish time scheduled
  - n O(n) additional time for greedy algorithm



























- <sup>n</sup> Given sequence **D**=**d**<sub>1</sub>,**d**<sub>2</sub>,...,**d**<sub>m</sub>
- <sup>n</sup> When d<sub>i</sub> needs to be brought into the cache evict the item that is needed farthest in the future
  - Let NextAccess<sub>i</sub>(d)=min{ j≥i : d<sub>j</sub>=d} be the next point in D that item d will be requested
  - n Evict d such that NextAccess<sub>i</sub>(d) is largest





























































































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n call such an edge safe







## The greedy algorithms always choose safe edges

- n Kruskal's Algorithm
  - Always chooses cheapest edge connecting two pieces of the graph that aren't yet connected
  - This is the cheapest edge across any cut which has those two pieces on different sides and doesn't split any current pieces.

Kruskal's Algorithm



















Two components may choose to add the same edge

 Useful for parallel algorithms since components may be processed (almost) independently



- D(m α(m) log α(m)) time
  Incredibly hairy algorithm
- n Karger, Klein & Tarjan
  - $\ _{\rm n} \ O(m+n)$  time randomized algorithm that works most of the time



- <sup>n</sup> Minimum cost network design:
  - . Build a network to connect all locations  $\{v_1, \dots, v_n\}$
  - <sup>n</sup> Cost of connecting  $v_i$  to  $v_j$  is  $w(v_i, v_j) > 0$
  - Choose a collection of links to create that will be as cheap as possible
  - Any minimum cost solution is an MST
    If there is a solution containing a cycle
    - then we can remove any edge and get a cheaper solution



