CSE 421 Algorithms

Richard Anderson Lecture 21 Shortest Path Network Flow Introduction

Announcements

- Friday, 11/18, Class will meet in CSE 305
- Reading 7.1-7.3, 7.5-7.6
 Section 7.4 will not be covered

Find the shortest paths from v with exactly k edges

Express as a recurrence

- $Opt_k(w) = min_x [Opt_{k-1}(x) + c_{xw}]$
- Opt₀(w) = 0 if v=w and infinity otherwise

Algorithm, Version 1

foreach w

$$\begin{split} M[0,w] &= \text{infinity;} \\ M[0,v] &= 0; \\ \text{for i = 1 to n-1} \\ & \text{foreach } w \\ M[i,w] &= \min_x (M[i\text{-}1,x] + \text{cost}[x,w]); \end{split}$$

Algorithm, Version 2

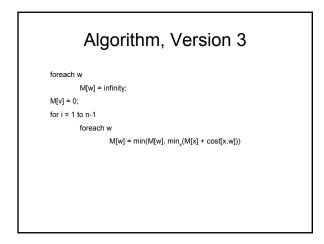
foreach w

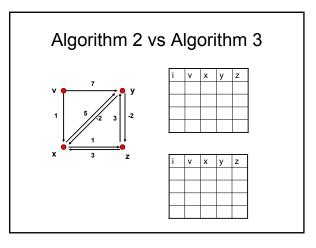
M[0, w] = infinity;

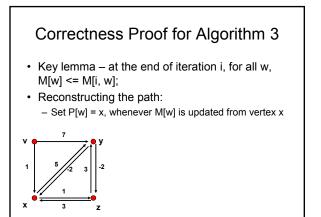
M[0, v] = 0; for i = 1 to n-1

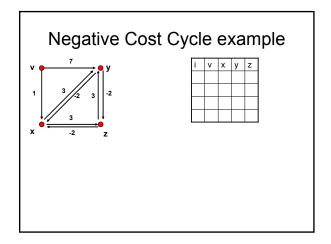
foreach w

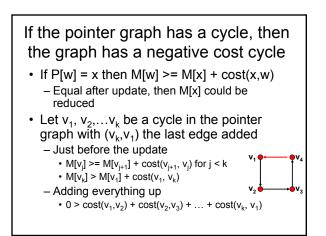
 $\mathsf{M}[\mathsf{i},\mathsf{w}] = \mathsf{min}(\mathsf{M}[\mathsf{i}\text{-}1,\mathsf{w}],\mathsf{min}_\mathsf{x}(\mathsf{M}[\mathsf{i}\text{-}1,\mathsf{x}]+\mathsf{cost}[\mathsf{x},\mathsf{w}]))$

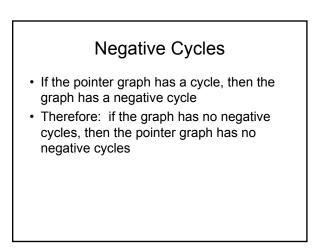


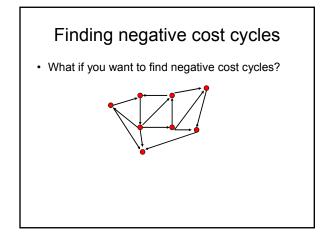


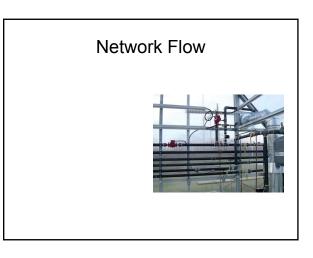












Network Flow Definitions

- · Capacity
- · Source, Sink
- Capacity Condition
- Conservation Condition
- · Value of a flow

