CSE 421: Intro to Algorithms

Winter 2004 Graph Algorithms: BFS, DFS, Articulation Points Larry Ruzzo

Breadth-First Search

- Completely explore the vertices in order of their distance from v
- · Naturally implemented using a queue
- Works on general graphs, not just trees

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BFS analysis

- Each edge is explored once from each
 end-point
- Each vertex is discovered by following a different edge
- Total cost O(m) where m=# of edges
- Disconnected? Restart @ undiscovered vertices: O(m+n)

Properties of (Undirected) BFS(v)

- BFS(v) visits x if and only if there is a path in G from v to x.
- Edges into then-undiscovered vertices define a tree – the "breadth first spanning tree" of G
- Level i in this tree are exactly those vertices u such that the shortest path (in G, not just the tree) from the root v is of length i.
- All non-tree edges join vertices on the same or adjacent levels





















- draw a graph, ~ 10 nodes, A-J
- redraw as via DFS
- add dsf#s & tree/back edges (solid/dashed)
- find cycles
- · give alg to find cycles via dfs; does G have any?
- · find articulation points
- what do cycles have to do with articulation points?
- alg to find articulation points via DFS???





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