

CSE 417 Algorithms and Complexity

Autumn 2024 Lecture 11 Dijkstra's algorithm

Announcements

• Topics

- Dijkstra's Algorithm (Section 4.4)
 Algorithm and why it works
- Next Week: Minimum Spanning Trees
- Reading
 - 4.4, 4.5, 4.7, 4.9
- Midterm: Friday, November 1, in class













http://www.cs.utexas.edu/users/EWD/

• Edsger Wybe Dijkstra was one of the most influential members of computing science's founding generation. Among the domains in which his scientific contributions are fundamental are

- algorithm design
- programming languages
- program design
- operating systems
- distributed processing
- formal specification and verification
- design of mathematical arguments



Dijkstra's Algorithm as a greedy algorithm

• Elements committed to the solution by order of minimum distance

Correctness Proof

- Elements in S have the correct label
- Key to proof: when v is added to S, it has the correct distance label.





Negative Cost Edges

• Draw a small example a negative cost edge and show that Dijkstra's algorithm fails on this example

Dijkstra Implementation

```
\begin{array}{lll} S = \{ \; \}; & d[s] = 0; & d[v] = infinity \mbox{ for } v != s \\ \\ While S != V \\ & Choose v \mbox{ in V-S with minimum } d[v] \\ & Add v \mbox{ to S} \\ & For each \ w \mbox{ in the neighborhood of } v \\ & d[w] = min(d[w], \ d[v] + c(v, w)) \end{array}
```

- Basic implementation requires Heap for tracking the distance values
- Run time O(m log n)







