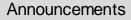


CSE 417 Algorithms and Complexity

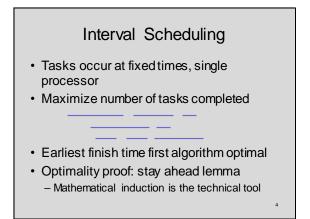
Autumn 2024 Lecture 9 – Greedy Algorithms II

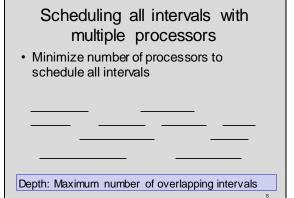


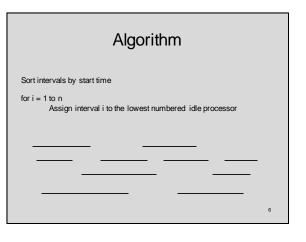
- Today's lecture - Kleinberg-Tardos, 4.2, 4.3
- Wednesday and Friday
  Kleinberg-Tardos, 4.4, 4.5

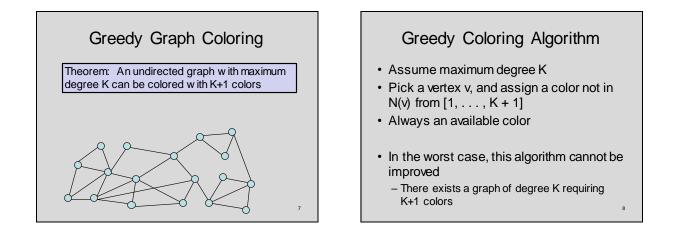
## Greedy Algorithms

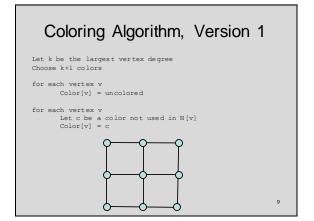
- Solve problems with the simplest possible algorithm
- The hard part: showing that something simple actually works
- Today's problems (Sections 4.2, 4.3) – Graph Coloring
  - Homew ork Scheduling
  - Optimal Caching

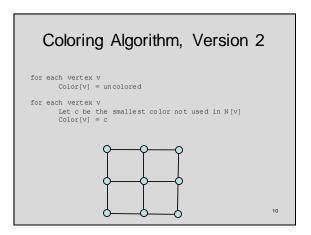


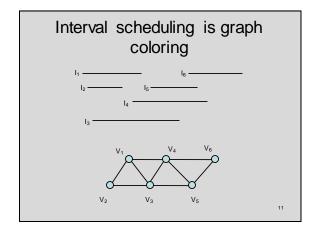


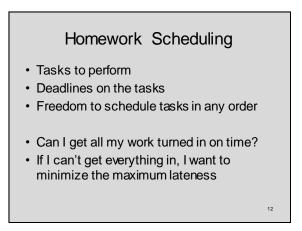












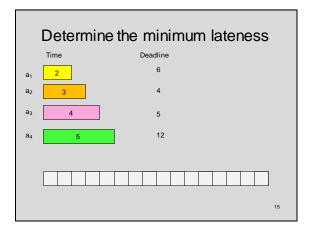
## Scheduling tasks

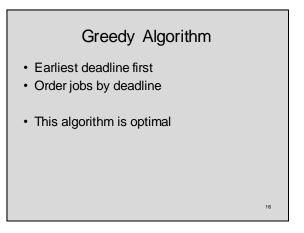
Each task has a length t<sub>i</sub> and a deadline d<sub>i</sub>

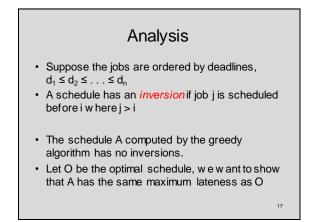
13

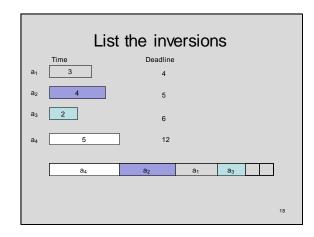
- · All tasks are available at the start
- One task may be worked on at a time
- All tasks must be completed
- Goal minimize maximum lateness - Lateness:  $L_i = f_i - d_i$  if  $f_i \ge d_i$

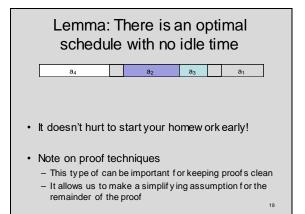
Example		
Time	Deadline	
a <sub>1</sub> 2	2	
a <sub>2</sub> 3	4	
2 3	Lateness 1	
3	2 Lateness 3	
		14

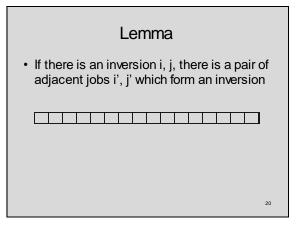


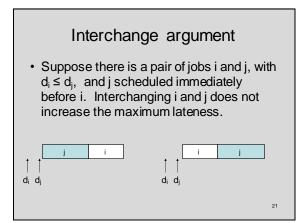


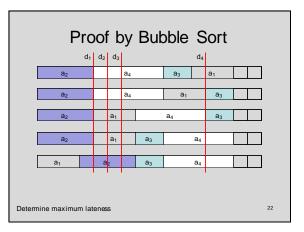










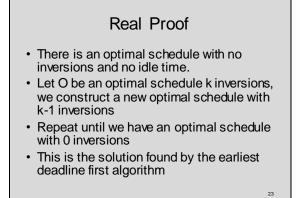


Result

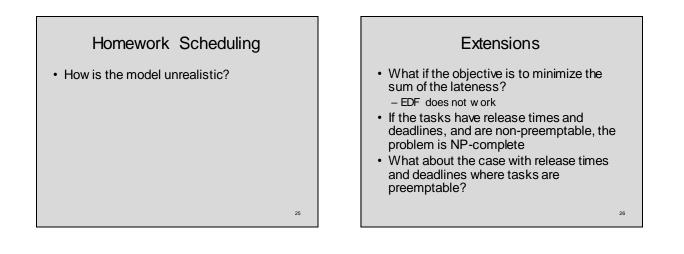
constructs a schedule that minimizes the

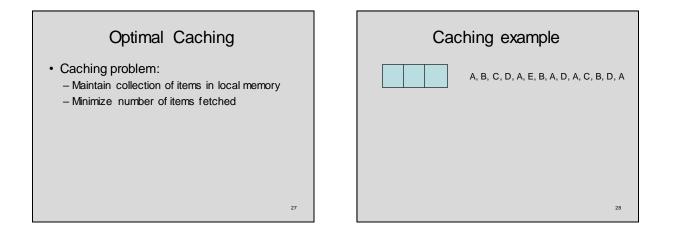
Earliest Deadline First algorithm

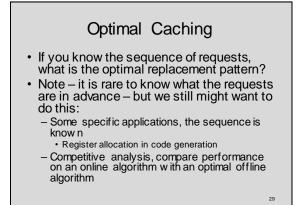
maximum lateness

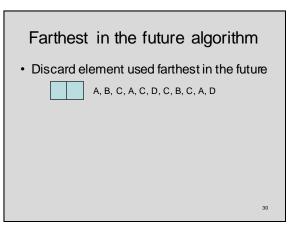


4









## Correctness Proof

- Sketch
- Start with Optimal Solution O
- Convert to Farthest in the Future Solution  $\ensuremath{\mathsf{F}}\xspace{\mathsf{F}}\xspace{\mathsf{F}}$
- Look at the first place where they differ
- Convert O to evict F-F element
  - There are some technicalities here to ensure the caches have the same configuration . . .

31

