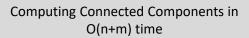
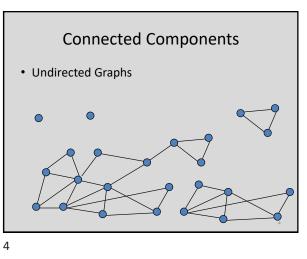
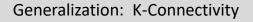


3



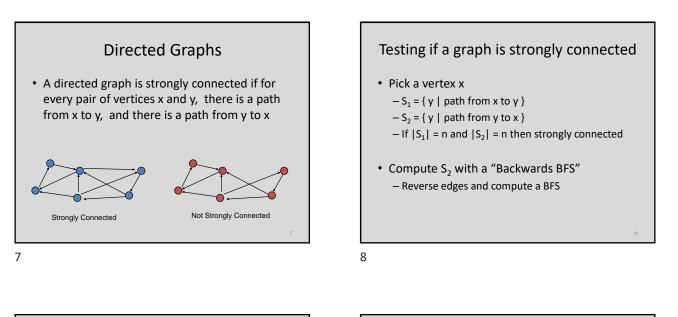
- A search algorithm from a vertex v can find all vertices in v's component
- While there is an unvisited vertex v, search from v to find a new component

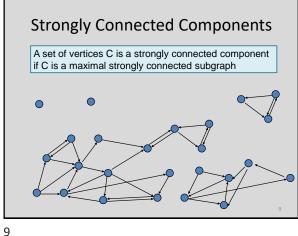


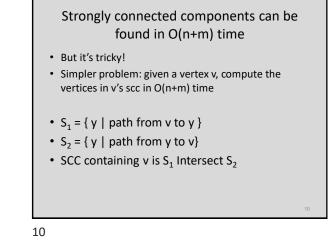


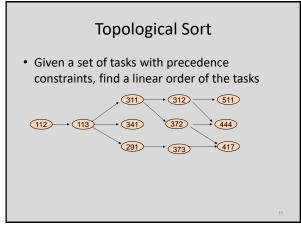
- An undirected graph is K-connected if every pair of distinct vertices is connected by at least K distinct paths
- Biconnected = 2-connected

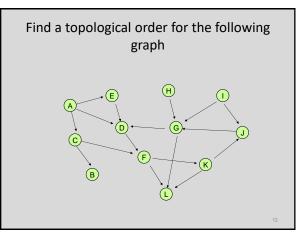
5

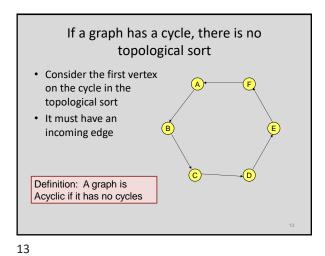










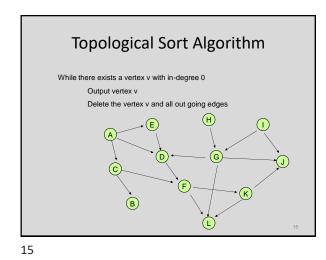


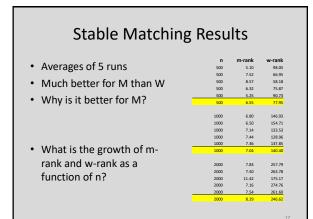
vertex with in-degree 0
Proof:

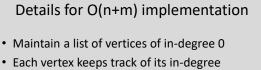
Pick a vertex v<sub>1</sub>, if it has in-degree 0 then done
If not, let (v<sub>2</sub>, v<sub>1</sub>) be an edge, if v<sub>2</sub> has in-degree 0 then done
If not, let (v<sub>3</sub>, v<sub>2</sub>) be an edge ...
If this process continues for more than n steps, we have a repeated vertex, so we have a cycle

Lemma: If a (finite) graph is acyclic, it has a

14

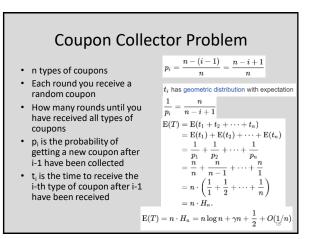






- Update in-degrees and list when edges are removed
- m edge removals at O(1) cost each

16



## Stable Matching and Coupon Collecting

19

- Assume random preference lists
- Runtime of algorithm determined by number of proposals until all w's are matched
- Each proposal can be viewed<sup>1</sup> as asking a random w
- Number of proposals corresponds to number of steps in coupon collector problem

<sup>1</sup>There are some technicalities here that are being ignored

19