

Classic Application

Suppose you need to multiply **really** big numbers.

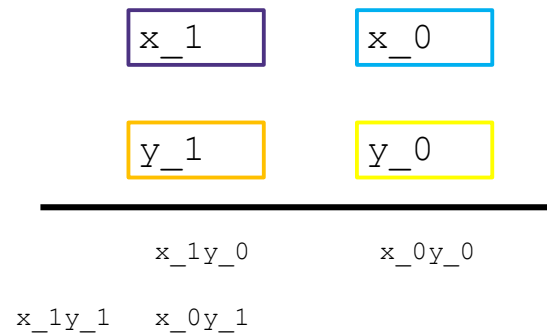
Much bigger than `ints`

Split the n bit numbers in half

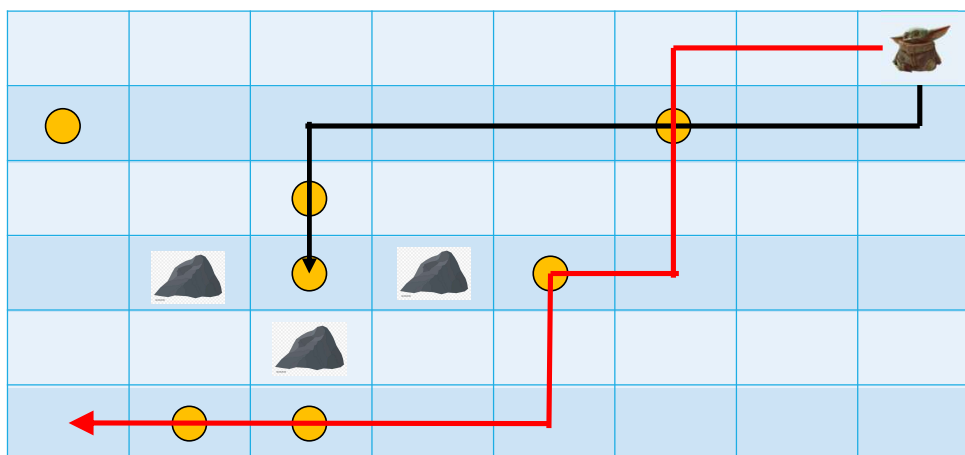
Think of them as written in base $2^{n/2}$

What would the "normal" multiplication algorithm do?

4 multiplications, i.e. 4 recursive calls.



Baby Yoda Searching



Black path: get stuck. Invalid.

Red path: valid!
And optimal (no path collects more than 4 eggs.)

Let $\text{OPT}(i, j)$ be the maximum number of eggs we can get on a legal path from (i, j) to $(0, 0)$ (including the egg in (i, j) if there is one)

What recursive calls do we need?

Don't try to divide & conquer, think closer to home...

We have to decide whether to go down or left...

Activity

Fill out the question at
pollev.com/robbie

Figure out how to take advantage of the repeated calculation.

What do you think the running time will be of your new algorithm?

```
FindOPT(int i, int j, bool[][] rocks, bool[][] eggs)
    if(i < 0 || j < 0) return -∞
    if(rocks[i][j]) return -∞
    if(i == 0 && j == 0) return eggs[0][0]
    int left = FindOPT(i-1, j, rocks, eggs)
    int down = FindOPT(i, j-1, rocks, eggs)
    return Max(left, down) + eggs[i][j]
```