

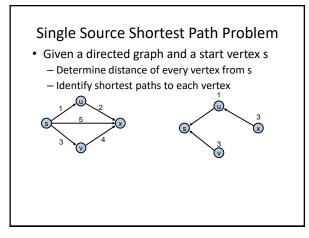


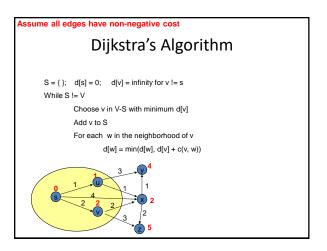
CSE 417 Algorithms and Complexity

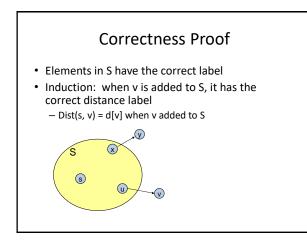
Autumn 2020 Lecture 12 Shortest Paths Algorithm and Minimum Spanning Trees

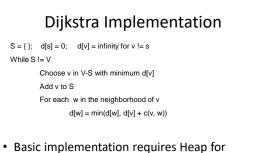
Announcements

- Reading
 4.4, 4.5, 4.7, 4.8
- Homework
 - Assignment will include a sample midterm







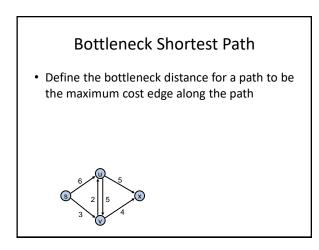


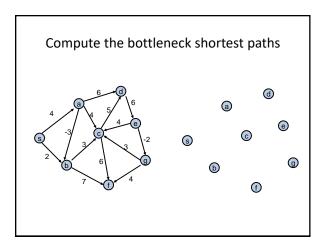
- Basic implementation requires Heap for tracking the distance values
- Run time O(m log n)

O(n²) Implementation for Dense Graphs

Future stuff for shortest paths

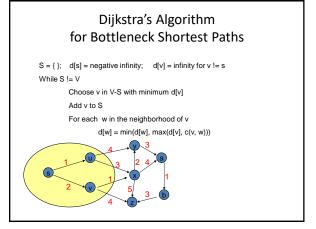
- Bellman-Ford Algorithm
 - O(nm) time
 - Handles negative cost edges
 - Identifies negative cost cycle if present
 - Dynamic programming algorithm
 - Very easy to implement





How do you adapt Dijkstra's algorithm to handle bottleneck distances

• Does the correctness proof still apply?

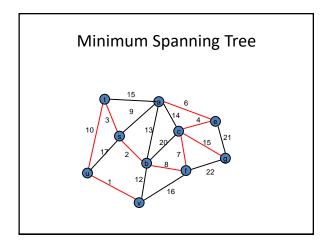


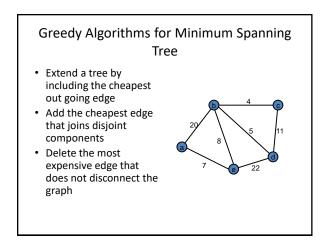
Minimum Spanning Tree

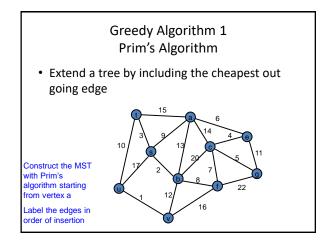
- Introduce Problem
- Demonstrate three different greedy algorithms
- Provide proofs that the algorithms work

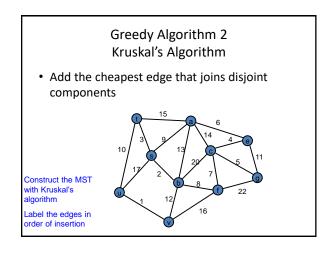
Minimum Spanning Tree Definitions

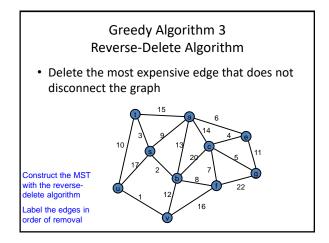
- G=(V,E) is an UNDIRECTED graph
- Weights associated with the edges
- Find a spanning tree of minimum weight - If not connected, complain

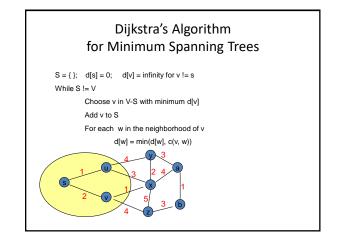


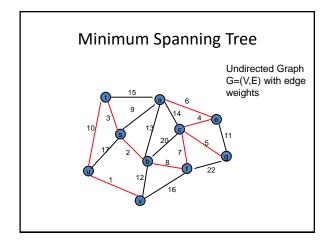


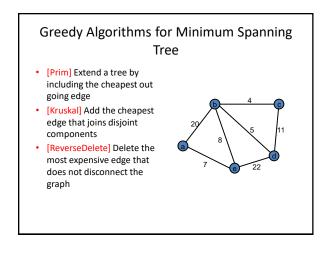












Why do the greedy algorithms work?

• For simplicity, assume all edge costs are distinct

