

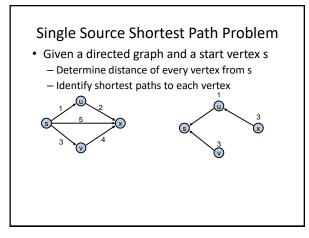


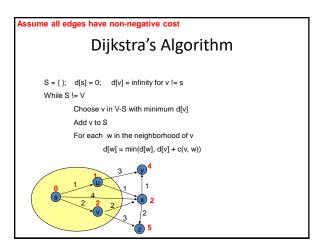
## CSE 417 Algorithms and Complexity

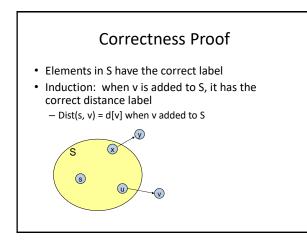
Autumn 2020 Lecture 12 Shortest Paths Algorithm and Minimum Spanning Trees

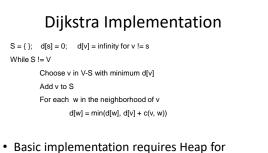
## Announcements

- Reading
  4.4, 4.5, 4.7, 4.8
- Homework
  - Assignment will include a sample midterm







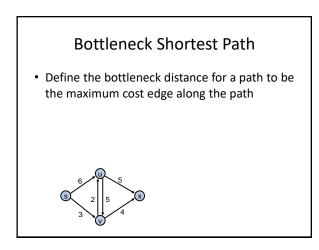


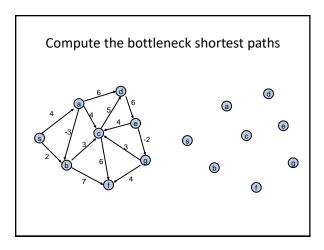
- Basic implementation requires Heap for tracking the distance values
- Run time O(m log n)

# O(n<sup>2</sup>) Implementation for Dense Graphs

# Future stuff for shortest paths

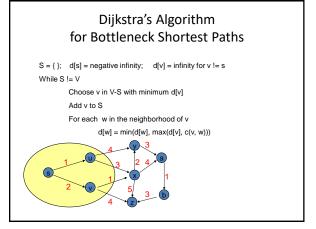
- Bellman-Ford Algorithm
  - O(nm) time
  - Handles negative cost edges
  - Identifies negative cost cycle if present
  - Dynamic programming algorithm
  - Very easy to implement





How do you adapt Dijkstra's algorithm to handle bottleneck distances

• Does the correctness proof still apply?

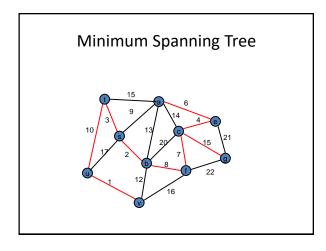


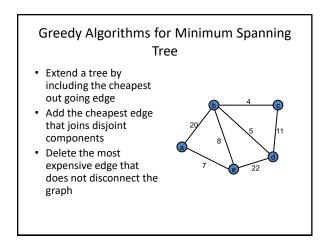
# Minimum Spanning Tree

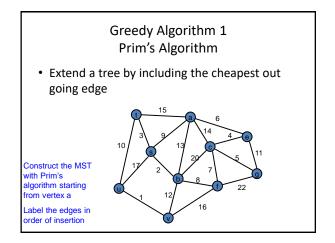
- Introduce Problem
- Demonstrate three different greedy algorithms
- Provide proofs that the algorithms work

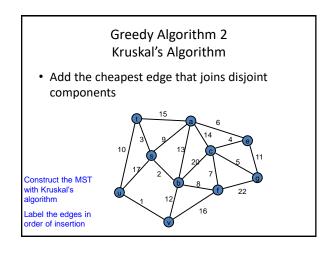
#### Minimum Spanning Tree Definitions

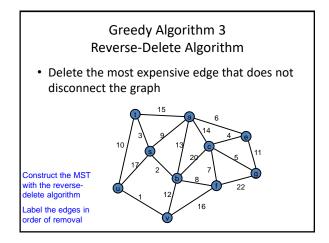
- G=(V,E) is an UNDIRECTED graph
- Weights associated with the edges
- Find a spanning tree of minimum weight - If not connected, complain

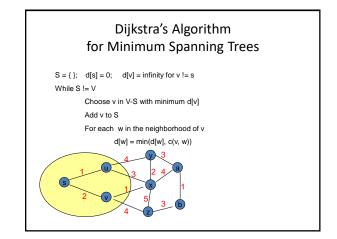


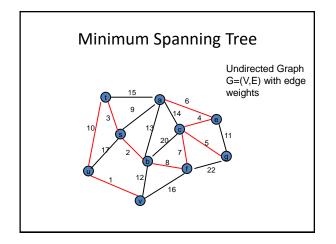


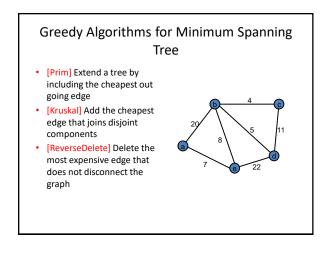












# Why do the greedy algorithms work?

• For simplicity, assume all edge costs are distinct

