CSE 417 Algorithms and Computational Complexity

Richard Anderson Autumn 2020 Lecture 1

CSE 417 Course Introduction

- CSE 417, Algorithms and Computational Complexity
 - MWF 1:30-2:20 pm
 - Zoomistan
- Instructor
 - Richard Anderson, anderson@cs.washington.edu
 - Office hours:
 - Zoom
 - Office hours: TBD
- · Teaching Assistants
 - Josh Curtis, Anny Kong, Alon Milchgrub, Ivy Wang

Announcements

- · It's on the course website
- · Homework weekly
 - Usually due Wednesdays
 - HW 1, Due Wednesday October 7, 2020
 - It's on the website (or will be soon)
- · Homework is to be submitted electronically
 - Due at 1:30 PM. No late days.
- You should be on the course mailing list
 - But it will probably go to your uw.edu account

Teaching on Zoom

- This is my first time teaching Algorithms on Zoom
- · My concerns
 - How do I interact with the class
 - To get cues on how the material is coming across
 - To support my teaching style of quick questions
 - To allow questions and clarifications
 - I encourage questions
 - Chat is available, and will be moderated by TAs
 - Will try to use classroom activities and breakout rooms

Textbook

- Algorithm Design
- · Jon Kleinberg, Eva Tardos
 - Only one edition
- Read Chapters 1 & 2
- · Expected coverage:
- Chapter 1 through 7
- Book available at:
- UW Bookstore (\$171.25/\$128.45)
- Ebay (\$12.96 to \$307.10)
- Amazon (\$19.18 and up)
- Electronic (\$59.99 / \$39.99)
- PDF







Course Mechanics

- Homework
 - Due Wednesdays
 - Mix of written problems and programming
 - Target: 1-week turnaround on grading
- Exams
 - Midterm, Tentatively, Monday, November 2
 - Final, Monday, December 14, 2:30-4:20 pm
 - Approximate grade weighting:
 - HW: 50, MT: 15, Final: 35
- · Course web
 - Slides, Handouts, Piazza Discussion Board

All of Computer Science is the Study of Algorithms

How to study algorithms

- Zoology
- · Mine is faster than yours is
- · Algorithmic ideas
 - Where algorithms apply
 - What makes an algorithm work
 - Algorithmic thinking
- · Algorithm practice

Introductory Problem: Stable Matching

- · Setting:
 - Assign TAs to Instructors
 - Avoid having TAs and Instructors wanting changes
 - E.g., Prof A. would rather have student X than her current TA, and student X would rather work for Prof A. than his current instructor.

Formal notions

- · Perfect matching
- · Ranked preference lists
- Stability



Example (1 of 3)

 W_2 : $M_2 M_1$ $M_2 M_2$ M_2

Example (2 of 3)

 m_1 : w_1 w_2 m_1 ov_1 ov_2 m_2 : w_1 w_2 w_1 : m_1 m_2

 W_2 : M_1 M_2 M_2 M_2

Example (3 of 3)

Formal Problem

- Input
 - Preference lists for m₁, m₂, ..., m_n
 - Preference lists for $w_1, w_2, ..., w_n$
- Output
 - Perfect matching M satisfying stability property:

If $(m', w') \in M$ and $(m'', w'') \in M$ then (m') prefers w' to w'') or (w'') prefers m'' to m')

Idea for an Algorithm

m proposes to w

If w is unmatched, w accepts

If w is matched to m2

If w prefers m to m₂ w accepts m, dumping m₂
If w prefers m₂ to m, w rejects m

Unmatched m proposes to the highest w on its preference list that it has not already proposed to

Algorithm

Initially all m in M and w in W are free While there is a free m

w highest on m's list that m has not proposed to

if w is free, then match (m, w) else

suppose (m₂, w) is matched if w prefers m to m₂ unmatch (m₂, w) match (m, w)

Example

 $m_3 \bigcirc$

 \bigcirc W₃

Does this work?

- · Does it terminate?
- Is the result a stable matching?
- Begin by identifying invariants and measures of progress
 - m's proposals get worse (have higher m-rank)
 - Once w is matched, w stays matched
 - w's partners get better (have lower w-rank)

Claim: If an m reaches the end of its list, then all the w's are matched

Claim: The algorithm stops in at most n² steps

When the algorithms halts, every w is matched

Why?

Hence, the algorithm finds a perfect matching

The resulting matching is stable

Suppose

$$(m_1, w_1) \in M, (m_2, w_2) \in M$$

 $m_1 \text{ prefers } w_2 \text{ to } w_1$



How could this happen?

Result

- Simple, O(n²) algorithm to compute a stable matching
- Corollary
 - A stable matching always exists