

# CSE 417: Algorithms and Computational Complexity

## 4: Dynamic Programming, I Fibonacci

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Lecture 4  
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## Some Algorithm Design Techniques, I

- General overall idea
  - Reduce solving a problem to a smaller problem or problems of the same type
- Greedy algorithms
  - Used when one needs to build something a piece at a time
  - Repeatedly make the **greedy** choice - the one that looks the best right away
    - e.g. closest pair in TSP search
  - Usually fast if they work (but often don't)

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## Some Algorithm Design Techniques, II

- Divide & Conquer
  - Reduce problem to one or more sub-problems of the same type
  - Typically, each sub-problem is at most a constant fraction of the size of the original problem
    - e.g. Mergesort, Binary Search, Strassen's Algorithm, Quicksort (kind of)

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## Some Algorithm Design Techniques, III

- Dynamic Programming
  - Give a solution of a problem using smaller sub-problems, e.g. a recursive solution
  - Useful when the same sub-problems show up again and again in the solution

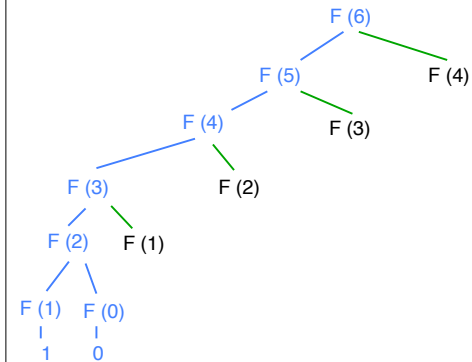
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## A simple case: Computing Fibonacci Numbers

- Recall  $F_n = F_{n-1} + F_{n-2}$  and  $F_0 = 0, F_1 = 1$
- Recursive algorithm:
  - Fibo(n)
    - if**  $n=0$  **then return**(0)
    - else if**  $n=1$  **then return**(1)
    - else return**(Fibo(n-1)+Fibo(n-2))

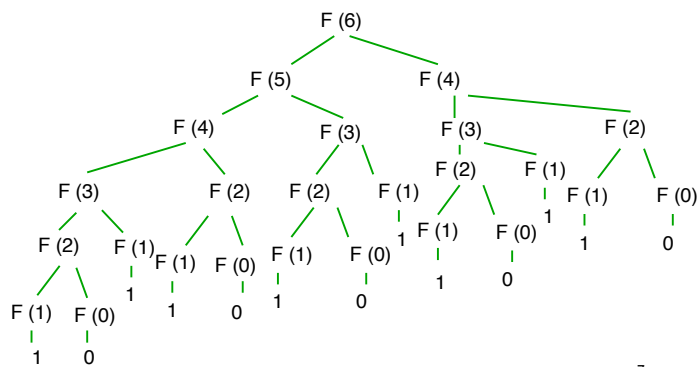
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## Call tree - start



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## Full call tree



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## Memo-ization (Caching)

- Remember all values from previous recursive calls
- Before recursive call, test to see if value has already been computed
- Dynamic Programming
  - Convert memo-ized algorithm from a recursive one to an iterative one

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## Fibonacci - Dynamic Programming Version

- FiboDP(n):  
  F[0] ← 0  
  F[1] ← 1  
  **for** i=2 **to** n **do**  
    F[i]=F[i-1]+F[i-2]  
  **endfor**  
  **return**(F[n])

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## Dynamic Programming

- Useful when
  - same recursive sub-problems occur repeatedly
  - Can anticipate the parameters of these recursive calls
  - The solution to whole problem can be figured out with knowing the internal details of how the sub-problems are solved
    - principle of optimality

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