### CSE 417: Algorithms and Computational Complexity

### **1: Algorithms and Efficiency**

Winter 2002 Instructor: Larry Ruzzo TA: Justin Campbell TA: Bill Pentney

#### **Algorithms: definition**

- Procedure to accomplish a task or solve a well-specified problem
  - Well-specified: know what all possible inputs look like and what output looks like given them
  - Ex: sorting names
  - Ex: checking for primality

# Algorithms: an example problem

- Printed circuit-board company has a robot arm that solders components to the board
- Time to do it depends on
  - I total distance the arm must move from initial rest position around the board and back to the initial positions

3

For each board design, must figure out good order to do the soldering









- Start at some point p<sub>0</sub>
- Walk first to its nearest neighbor p1
- Repeatedly walk to the nearest unvisited neighbor until all points have been visited
- Then walk back to p<sub>0</sub>













- For each of the n! orderings of the points check the length of the cycle you get
- Keep the best one



#### Measuring efficiency: The RAM model

- RAM = Random Access Machine
- Time ≈ # of instructions executed in an ideal assembly language
  - each simple operation (+,\*,-,=,if,call) takes
    one time step
  - each memory access takes one time step
- No bound on the memory

15

17

13

## We left out things but...

- Things we've dropped
  - memory hierarchy
     disk, caches, registers have many orders of magnitude differences in access time
  - I not all instructions take the same time in practice
- However,
  - I the RAM model is useful for designing algorithms and measuring their efficiency

16

I one can usually tune implementations so that the hierarchy etc. is not a huge factor

# Efficiency: What kind of analysis?

- Problem size n
  - Worst-case complexity: max # steps algorithm takes on any input of size n
  - Best-case complexity: min # steps algorithm takes on any input of size n
  - Average-case complexity: avg # steps algorithm takes on inputs of size n

Best-case

 unrealistic overselling
 can tune an algorithm so it works on one easy input

 Worst-case

 a fact algorithm has a comfacting guarantee

- a fast algorithm has a comforting guarantee
- no way to cheat by hard-coding special cases
  maybe too pessimistic
- Average-case

**Pros and cons:** 

- Average-case
- over what distribution?
- I different people may have different average problems