# CSE 417: Algorithms and Computational Complexity

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- Input: Given a set **S** of **n** points in the plane
- Output: The shortest cycle tour that visits each point in the set **S**.
- How might you solve it?

## **Nearest Neighbor Heuristic**

- Start at some point p<sub>0</sub>
- Walk first to its nearest neighbor p<sub>1</sub>
- Repeatedly walk to the nearest unvisited neighbor until all points have been visited
- Then walk back to p<sub>0</sub>













#### Efficiency

- The two incorrect algorithms were greedy
  - I they made choices and never reconsidered their choices
  - often it does not work
  - when it does the algorithms are typically efficient
- Our correct algorithm is incredibly slow
  - 20! is so large that counting to one billion in a second it would still take 2.4 billion seconds
     (around 70 years!)

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#### Measuring efficiency: The RAM model

- RAM = Random Access Machine
- Time ≈ # of instructions executed in an ideal assembly language
  - each simple operation (+,\*,-,=,if,call) takes
    one time step
  - each memory access takes one time step
- No bound on the memory

## We left out things but...

- Things we've dropped
  - I memory hierarchy
    - I disk, caches, registers have many orders of magnitude differences in access time
- not all instructions take the same time in practiceHowever,
  - I the RAM model is very useful for understanding how to design algorithms and get a good sense of how
    - quickly they will work
  - one can usually tune implementations so that the hierarchy etc is not a huge factor

# What kind of analysis?

#### Problem size n

- Worst-case complexity: max # steps algorithm takes on any input of size n
- Best-case complexity: min # steps algorithm takes on any input of size n
- Average-case complexity: avg # steps algorithm takes on inputs of size n

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#### **Pros and cons:**

- Best-case
  - unrealistic overselling
  - I can tune an algorithm so it works on one easy input
  - guarantee isn't comforting
- Worst-case
  - a fast algorithm has a comforting guarantee
  - I no way to cheat by hard-coding special cases
  - maybe too pessimistic
- Average-case
  - over what distribution?
  - I different people may have different average problems