

# CSE/STAT 416

## Classification

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# Roadmap So Far

1. Housing Prices - Regression
  - Regression Model
  - Assessing Performance
  - Ridge Regression
  - LASSO
2. Sentiment Analysis – Classification
  - Classification Overview
  - Logistic Regression
  - Decision Trees
  - Ensemble Methods

# Spam Filtering

Osman Khan to Carlos [show details](#) Jan 7 (6 days ago) [Reply](#)

sounds good  
+ok

Carlos Guestrin wrote:  
Let's try to chat on Friday a little to coordinate and more on Sunday in person?

Carlos

**Welcome to New Media Installation: Art that Learns**

Carlos Guestrin to 10615-announce, Osman, Miche [show details](#) 3:15 PM (8 hours ago) [Reply](#)

Hi everyone,

Welcome to New Media Installation:Art that Learns

The class will start tomorrow.  
\*\*\*Make sure you attend the first class, even if you are on the Wait List\*\*\*  
The classes are held in Doherty Hall C316, and will be Tue, Thu 01:30-4:20 PM.

By now, you should be subscribed to our course mailing list: [10615-announce@cs.cmu.edu](mailto:10615-announce@cs.cmu.edu).  
You can contact the instructors by emailing: [10615-instructors@cs.cmu.edu](mailto:10615-instructors@cs.cmu.edu)

**Natural \_LoseWeight SuperFood Endorsed by Oprah Winfrey, Free Trial 1 bottle, pay only \$5.95 for shipping mfw rik** Spam | X

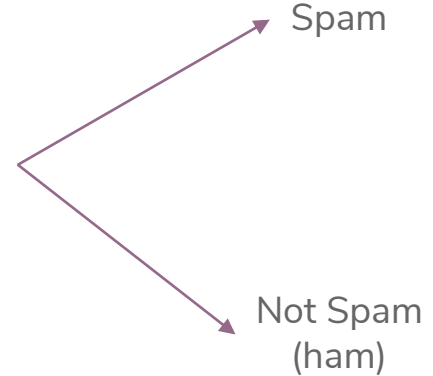
Jaquelyn Halley to nherlein, bcc: thehorney, bcc: ang [show details](#) 9:52 PM (1 hour ago) [Reply](#)

=== Natural WeightLOSS Solution ===

Vital Acai is a natural WeightLOSS product that Enables people to lose wieght and cleansing their bodies faster than most other products on the market.

Here are some of the benefits of Vital Acai that You might not be aware of. These benefits have helped people who have been using Vital Acai daily to Achieve goals and reach new heights in there dieting that they never thought they could.

- \* Rapid WeightLOSS
- \* Increased metabolism - BurnFat & calories easily!
- \* Better Mood and Attitude
- \* More Self Confidence
- \* Cleanse and Detoxify Your Body
- \* Much More Energy



Input: x  
Text of email  
Sender  
Subject  
...

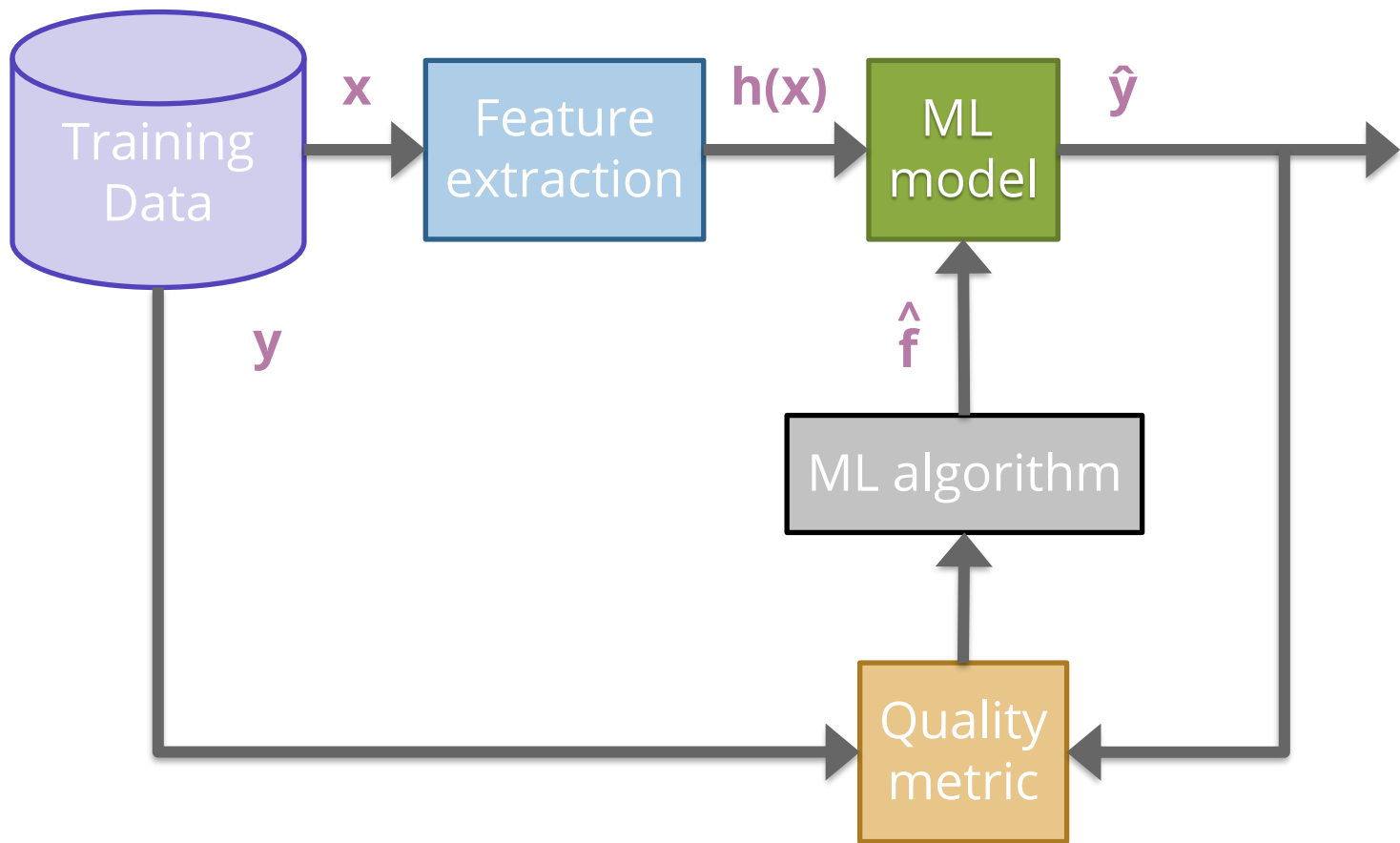
Output: y

# Object Detection



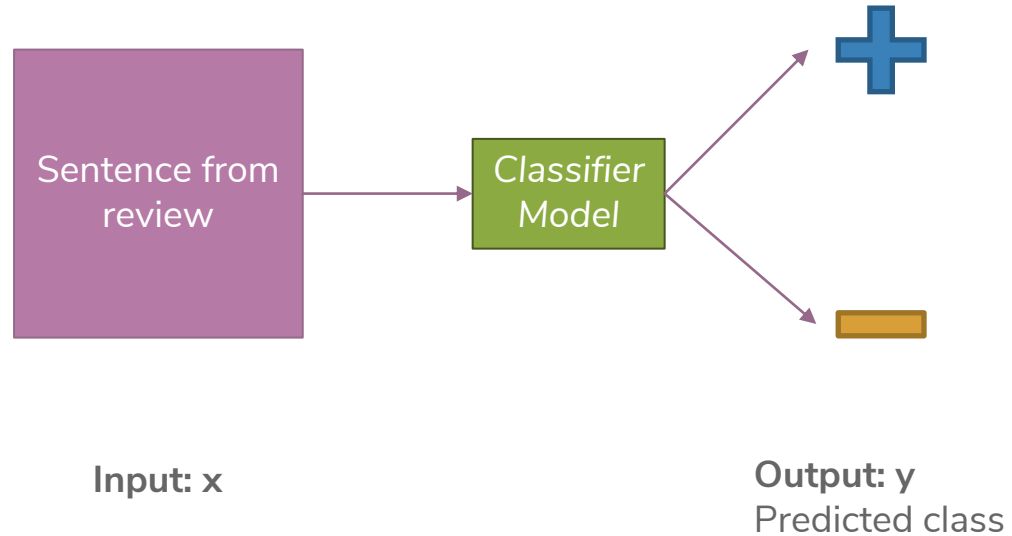
**Input: x**  
*Pixels*

**Output: y**  
*Class*  
*(+ Probability)*



# Sentiment Classifier

In our example, we want to classify a restaurant review as positive or negative.



## Implementation 1: Simple Threshold Classifier

**Idea:** Use a list of good words and bad words, classifier by most frequent type of word

- Positive Words: great, awesome, good, amazing, ...
- Negative Words: bad, terrible, disgusting, sucks, ...

### Simple Threshold Classifier

Input  $x$ : Sentence from review

- Count the number of positive and negative words, in  $x$
- If  $\text{num\_positive} > \text{num\_negative}$ :
  - $\hat{y} = +1$
- Else:
  - $\hat{y} = -1$

Example: "Sushi was great, the food was awesome, but the service was terrible"

# Problems with Threshold

How do we get list of positive/negative words?

Words have different degrees of sentiment.

- Great > Good
- How can we weigh them differently?

Single words are not enough sometimes...

- “Good” → Positive
- “Not Good” → Negative



## Implementation 2: Linear Classifier

**Idea:** Use labelled training data to learn a weight for each word.  
Use weights to score a sentence.

Word	Weight
good	1.0
great	1.5
awesome	2.7
bad	-1.0
terrible	-2.1
awful	-3.3
restaurant, the, we, where, ...	0.0
...	...

# Score a Sentence

Word	Weight
good	1.0
great	1.5
awesome	2.7
bad	-1.0
terrible	-2.1
awful	-3.3
restaurant, the, we, where, ...	0.0
...	...

Input  $x_i$ :

“Sushi was **great**, the food was **awesome**, but the service was **terrible**”

Linear classifier, because output is linear weighted sum of inputs.

Will learn how to learn weights soon!

## Implementation 2: Linear Classifier

**Idea:** Use labelled training data to learn a weight for each word.  
Use weights to score a sentence.

- See last slide for example weights and scoring.

### Linear Classifier

Input  $x$ : Sentence from review

- Compute  $Score(x)$
- If  $Score(x) \geq 0$ :
  - $\hat{y} = +1$
- Else:
  - $\hat{y} = -1$

# Linear Classifier Notation

**Model:**  $\hat{y}_i = \text{sign}(\text{Score}(x_i))$

$$\begin{aligned}\text{Score}(x_i) &= w_0 h_0(x_i) + w_1 h_1(x_i) + \dots + w_D h_D(x_i) \\ &= \sum_{j=0}^D w_j h_j(x_i) \\ &= w^T h(x)\end{aligned}$$

We will also use the notation

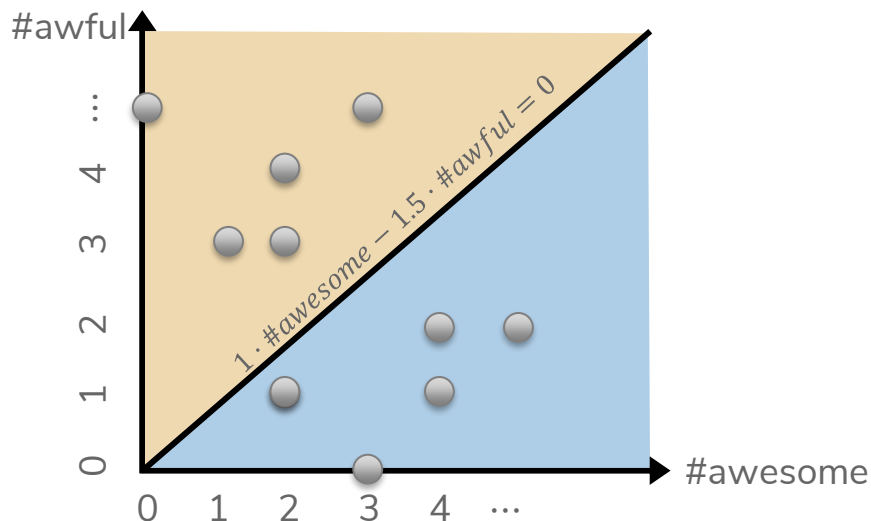
$$\begin{aligned}\hat{s}_i &= \text{Score}(x_i) = w^T h(x_i) \\ \hat{y}_i &= \text{sign}(\hat{s}_i)\end{aligned}$$

# Decision Boundary

Consider if only two words had non-zero coefficients

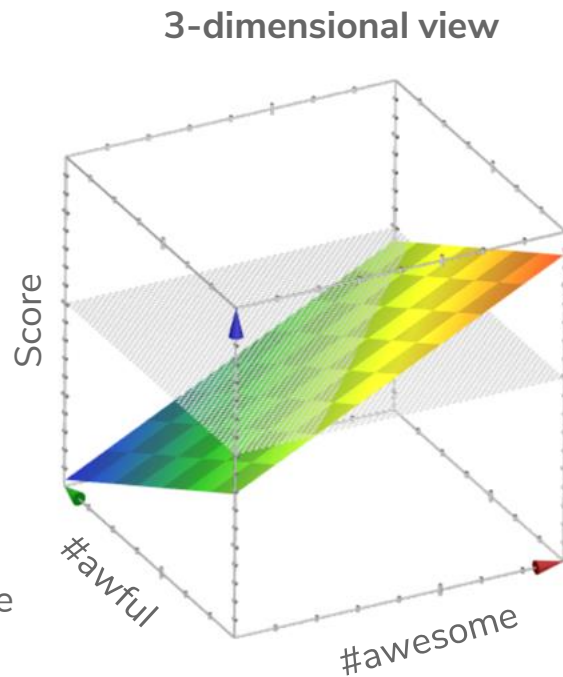
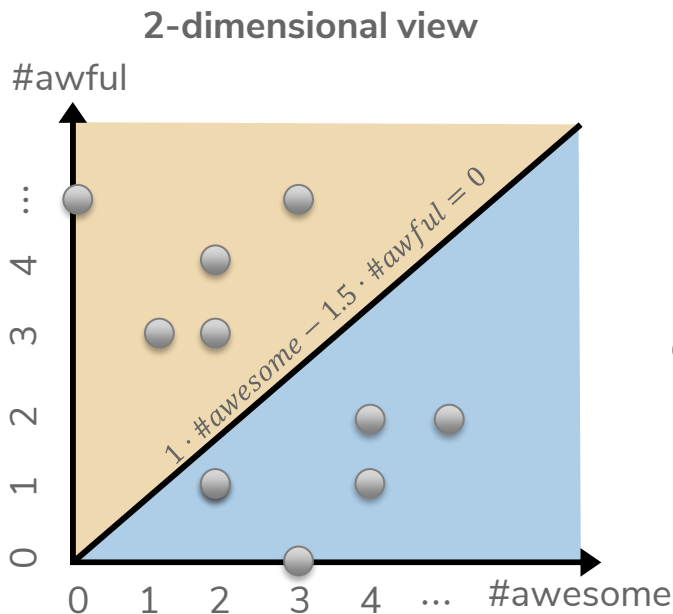
Word	Coefficient	Weight
	$w_0$	0.0
awesome	$w_1$	1.0
awful	$w_2$	-1.5

$$\hat{s} = 1 \cdot \#awesome - 1.5 \cdot \#awful$$



# Decision Boundary

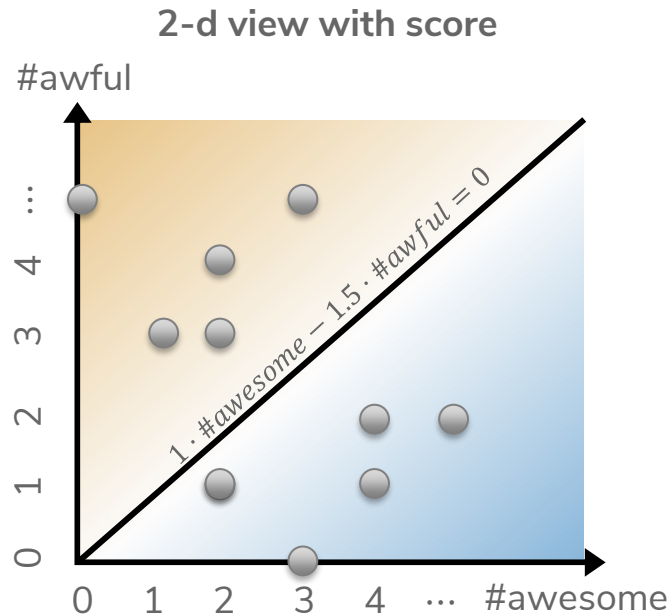
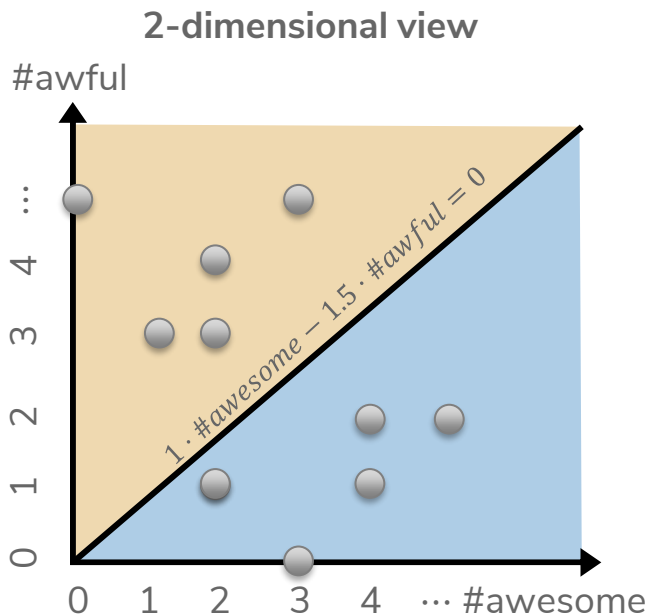
$$\text{Score}(x) = 1 \cdot \#awesome - 1.5 \cdot \#awful$$



Generally, with classification we don't use a plot like the 3d view since it's hard to visualize, instead use 2d plot with decision boundary

# Decision Boundary

$$\text{Score}(x) = 1 \cdot \#awesome - 1.5 \cdot \#awful$$





# Poll Everywhere

- **Goal:** Get you actively participating in your learning
- Typical Activity
  - Question is posed
  - **Think** (1 min): Think about the question on your own
  - **Pair** (2 min): Talk with your neighbor to discuss question
    - If you arrive at different conclusions, discuss your logic and figure out why you differ!
    - If you arrived at the same conclusion, discuss why the other answers might be wrong!
  - **Share** (1 min): We discuss the conclusions as a class
- During each of the **Think** and **Pair** stages, you will respond to the question via a Poll Everywhere poll
  - The poll will only be open for the last **15** seconds of each of the stage
  - Not worth any points, just here to help you learn!



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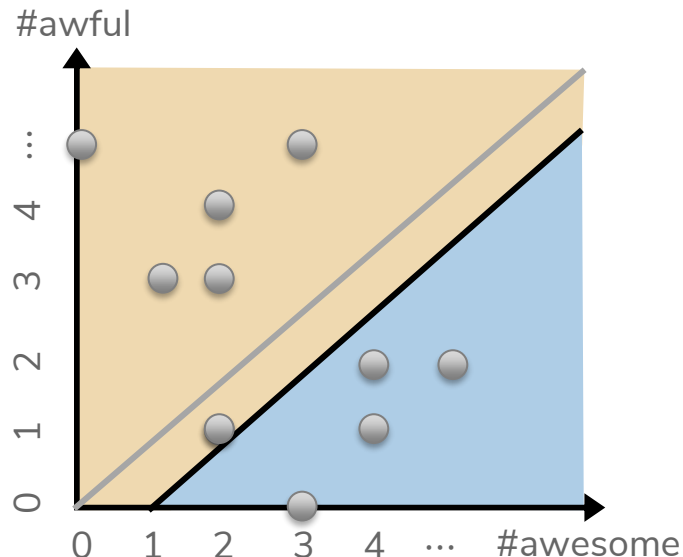
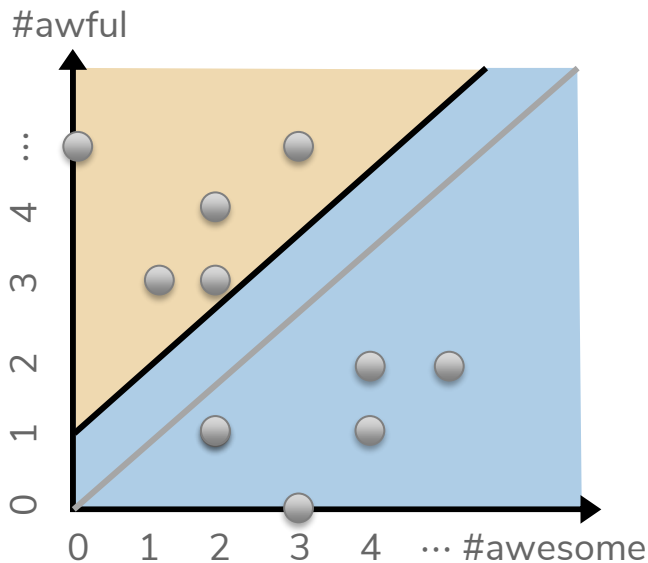


Think 

1 min

What happens to the decision boundary if we add an intercept?

$$\text{Score}(x) = 1.0 + 1 \cdot \#awesome - 1.5 \cdot \#awful$$

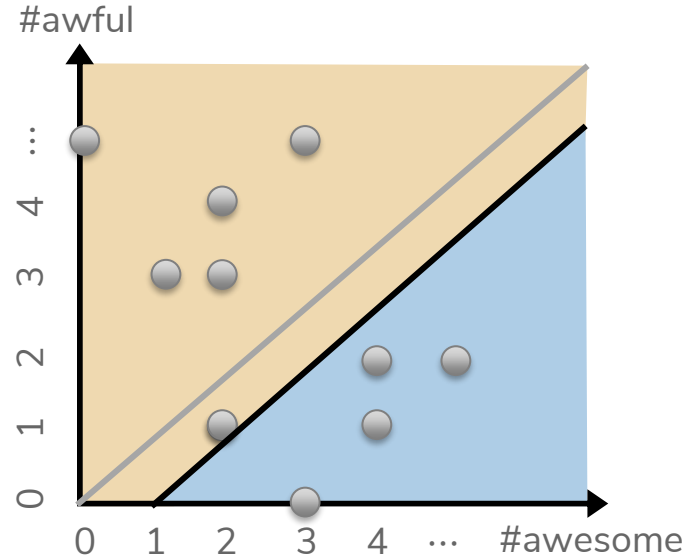
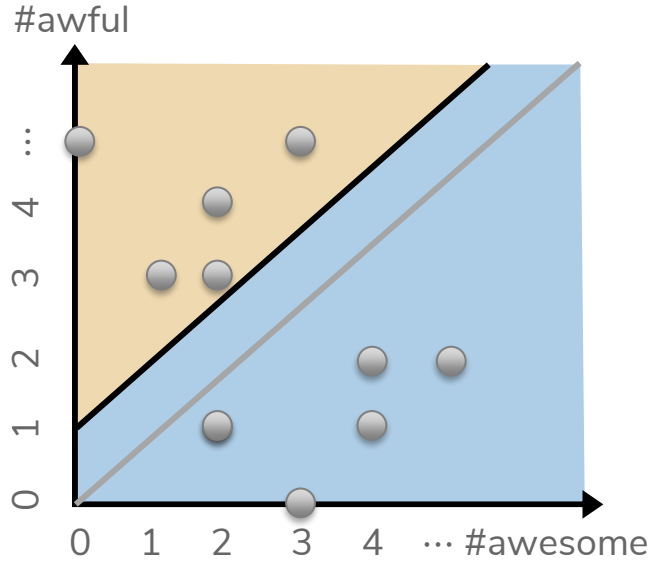


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What happens to the decision boundary if we add an intercept?

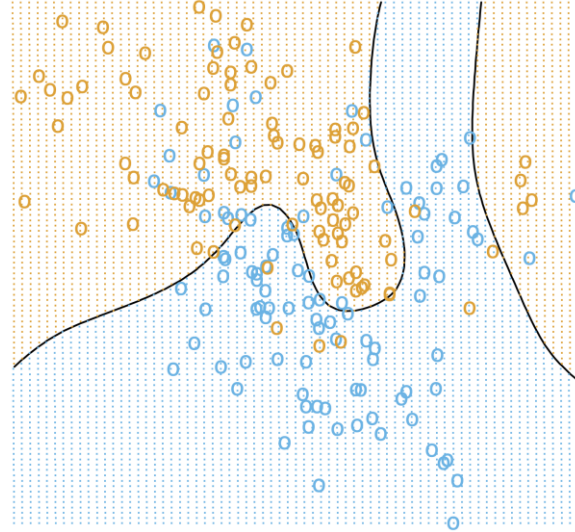
$$\text{Score}(x) = 1.0 + 1 \cdot \#awesome - 1.5 \cdot \#awful$$



# Complex Decision Boundaries?

What if we want to use a more complex decision boundary?

- Need more complex model/features!
- Covered next lecture!

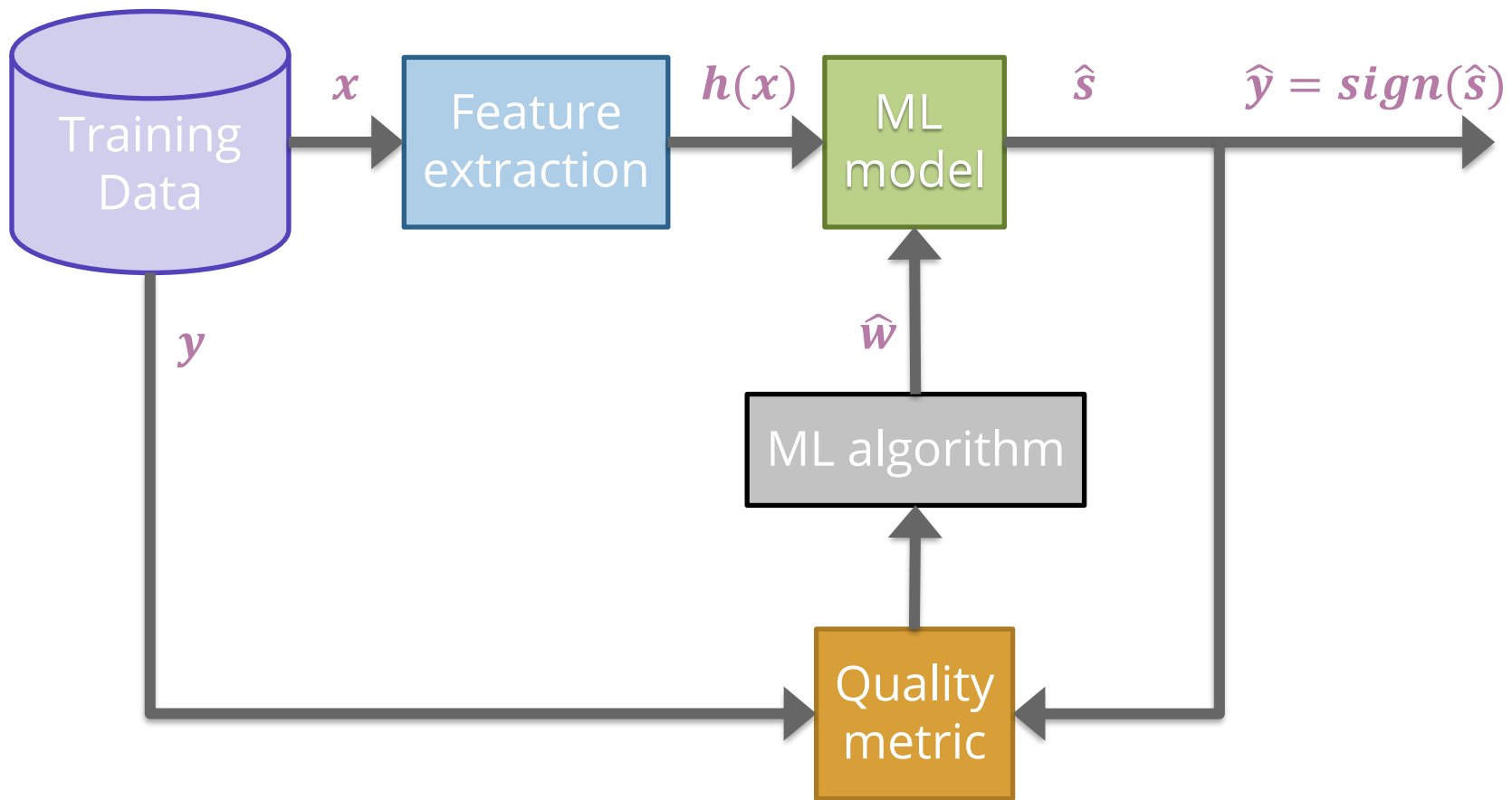




# Brain Break



# Evaluating Classifiers



# Classification Error

Ratio of examples where there was a mistaken prediction

What's a mistake?

- If the true label was positive ( $y = +1$ ), but we predicted negative ( $\hat{y} = -1$ )
- If the true label was negative ( $y = -1$ ), but we predicted positive ( $\hat{y} = +1$ )

**Classification Error**

**Classification Accuracy**

# What's a good accuracy?

For binary classification:

- Should at least beat random guessing...
- Accuracy should be at least 0.5

For multi-class classification ( $k$  classes):

- Should still beat random guessing
- Accuracy should be at least  $1/k$ 
  - 3-class: 0.33
  - 4-class: 0.25
  - ...

**Besides that, higher accuracy means better, right?**



# Detecting Spam

Imagine I made a “Dummy Classifier” for detecting spam

- The classifier ignores the input, and always predicts spam.
- This actually results in 90% accuracy! Why?
  - Most emails are spam...

This is called the **majority class classifier**.

A classifier as simple as the majority class classifier can have a high accuracy if there is a **class imbalance**.

- A class imbalance is when one class appears much more frequently than another in the dataset

This might suggest that accuracy isn't enough to tell us if a model is a good model.

# Assessing Accuracy

Always digging in and ask critical questions of your accuracy.

- Is there a **class imbalance**?
- How does it compare to a baseline approach?
  - Random guessing
  - Majority class
  - ...
- Most important: **What does my application need?**
  - What's good enough for user experience?
  - What is the impact of a mistake we make?

# Confusion Matrix

For binary classification, there are only two types of mistakes

- $\hat{y} = +1, y = -1$
- $\hat{y} = -1, y = +1$

Generally we make a **confusion matrix** to understand mistakes.

		Predicted Label	
		+	-
True Label	+	True Positive (TP)	False Negative (FN)
	-	False Positive (FP)	True Negative (TN)

# Confusion Matrix Example

		Predicted Label	
		+	-
True Label	+	True Positive (TP)	False Negative (FN)
	-	False Positive (FP)	True Negative (TN)

# Which is Worse?

## What's worse, a false negative or a false positive?

- It entirely depends on your application!

### Detecting Spam

False Negative: Annoying

False Positive: Email lost

### Medical Diagnosis

False Negative: Disease not treated

False Positive: Wasteful treatment

In almost every case, how treat errors depends on your context.

# Binary Classification Measures

## Notation

- $C_{TP} = \#TP$ ,  $C_{FP} = \#FP$ ,  $C_{TN} = \#TN$ ,  $C_{FN} = \#FN$
- $N = C_{TP} + C_{FP} + C_{TN} + C_{FN}$
- $N_P = C_{TP} + C_{FP}$ ,  $N_N = C_{FP} + C_{TN}$

## Error Rate

$$\frac{C_{FP} + C_{FN}}{N}$$

## Accuracy Rate

$$\frac{C_{TP} + C_{TN}}{N}$$

## False Positive rate (FPR)

$$\frac{C_{FP}}{N_N}$$

## False Negative Rate (FNR)

$$\frac{C_{FN}}{N_P}$$

## True Positive Rate or Recall

$$\frac{T_P}{N_P}$$

## Precision

$$\frac{T_P}{C_{TP} + C_{FP}}$$

## F1-Score

$$2 \frac{\text{Precision} \cdot \text{Recall}}{\text{Precision} + \text{Recall}}$$

[See more!](#)

# Multiclass Confusion Matrix

Consider predicting (Healthy, Cold, Flu)

		Predicted Label		
		Healthy	Cold	Flu
True Label	Healthy	60	8	2
	Cold	4	12	4
	Flu	0	2	8

Think 

1 min

Suppose we trained a classifier and computed its confusion matrix on the training dataset. **Is there a class imbalance in the dataset and if so, which class has the highest representation?**

		Predicted Label		
		Pupper	Doggo	Woofers
True Label	Pupper	2	27	4
	Doggo	4	25	4
	Woofers	1	30	2

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# Poll Everywhere

Pair 

2 min

Suppose we trained a classifier and computed its confusion matrix on the training dataset. **Is there a class imbalance in the dataset and if so, which class has the highest representation?**

		Predicted Label		
		Pupper	Doggo	Woofers
True Label	Pupper	2	27	4
	Doggo	4	25	4
	Woofers	1	30	2

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# Learning Theory

# How much data?

The more the merrier

- But data quality is also an extremely important factor

Theoretical techniques can bound how much data is needed

- Typically too loose for practical applications
- But does provide some theoretical guarantee

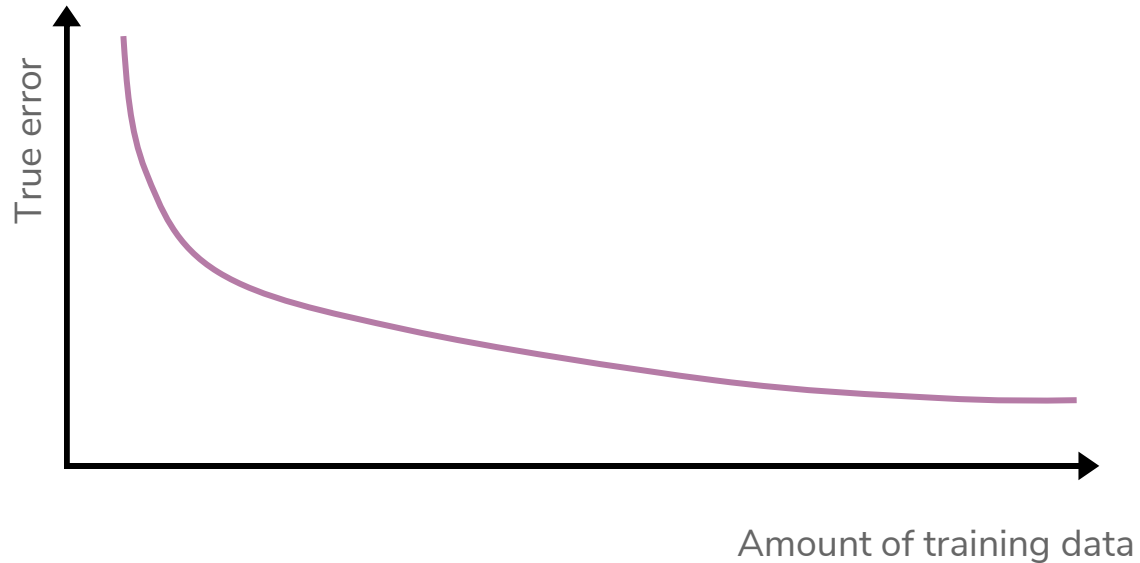
In practice

- More complex models need more data

# Learning Curve

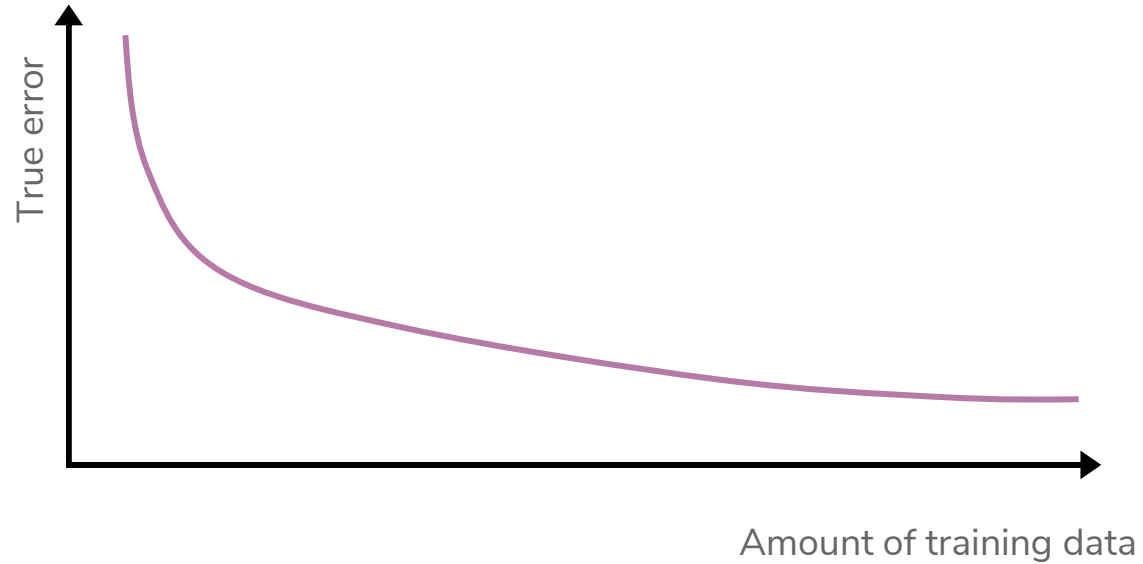
How does the true error of a model relate to the amount of training data we give it?

- Hint: We've seen this picture before



# Learning Curve

What if we use a more complex model?



# Change Threshold

What if I never want to make a false positive prediction?

What if I never want to make a false negative prediction?

One way to control for our application is to change the scoring threshold. (Could also change intercept!)

- If  $Score(x) \geq \alpha$ :
  - Predict  $\hat{y} = +1$
- Else:
  - Predict  $\hat{y} = -1$

# ROC Curve

What happens to our TPR and FPR as we increase the threshold?



## Next Time

We will talk about learning classifiers that model the probability of seeing a particular class at a given input.

$$P(y|x)$$

Normally assume some structure on the probability (e.g. linear)

$$P(y|x, w) \approx w^T x$$

Use machine learning algorithm to learn approximate  $\hat{w}$  such that

$$\hat{P}(y|x) = P(y|x, \hat{w})$$

And  $P(y|x)$  and  $\hat{P}(y|x)$  are close.



# Recap

**Theme:** Describe high level idea and metrics for classification

**Ideas:**

- Applications of classification
- Linear classifier
- Decision boundaries
- Classification error / Classification accuracy
- Class imbalance
- Confusion matrix
- Learning theory
- ROC Curve