



# CSE/STAT 416

## Introduction + Regression

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University of Washington  
June 24, 2019



**Machine Learning is  
changing the world.**



Sign in

● machine learning  
Search term

+ Compare

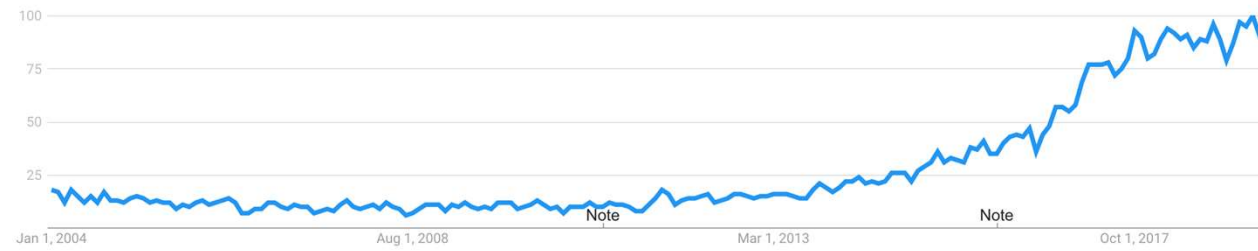
United States ▾

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Interest over time ?



● machine learning  
Search term

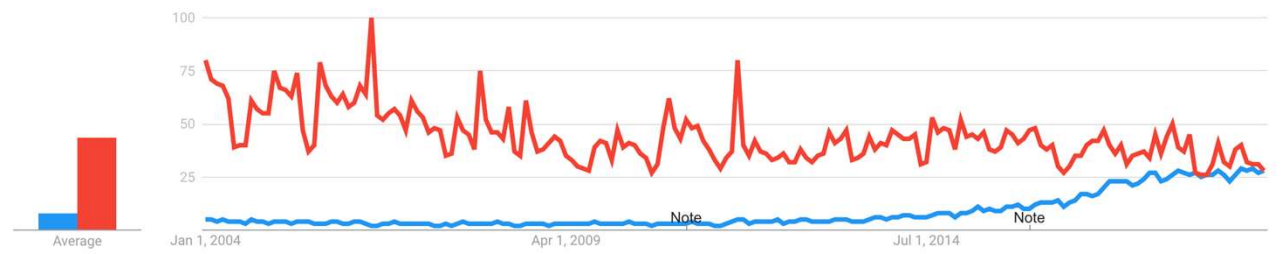
● bill gates  
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Interest over time ?

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It's Everywhere!

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**livingsocial.**  
Coupons

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Dating

**LinkedIn**  
Networking

**PANDORA**  
Music

**RelateIQ**  
CRM

**fitbit**  
Wearables

Disruptive companies  
differentiated by  
**INTELLIGENT  
APPLICATIONS**  
using  
**Machine Learning**

It's Everywhere...

### CREDIT SCORE



It's Everywhere...



**Eddy Dever**

@EddyDever

Follow



It's terrifying that both of these things are true at the same time in this world:

- computers drive cars around
- the state of the art test to check that you're not a computer is whether you can successfully identify stop signs in pictures

12:26 AM - 13 May 2018

5,644 Retweets 12,727 Likes



# What is Machine Learning?

Generically (and vaguely)

Machine Learning is the study of algorithms that improve their **performance** at some **task** with **experience**





# Course Overview

This course is broken up into 5 main case studies to explore ML in various contexts/applications.

1. Regression
  - Predicting housing prices
2. Classification
  - Positive/Negative reviews (Sentiment analysis)
3. Document Retrieval + Clustering
  - Find similar news articles
4. Recommender Systems
  - Given past purchases, what do we recommend to you?
5. Deep Learning
  - Recognizing objects in images

# Course Topics

## Models

- Linear regression, regularized approaches (ridge, LASSO)
- Linear classifiers: logistic regression
- Non-linear models: decision trees
- Nearest neighbors, clustering
- Recommender systems
- Deep learning

## Algorithms

- *Gradient descent*
- Boosting
- K-means

## Concepts

- Point estimation, MLE
- Loss functions, bias-variance tradeoff, cross-validation
- Sparsity, overfitting, model selection
- Decision boundaries

# ML Course Landscape

## CSE 446

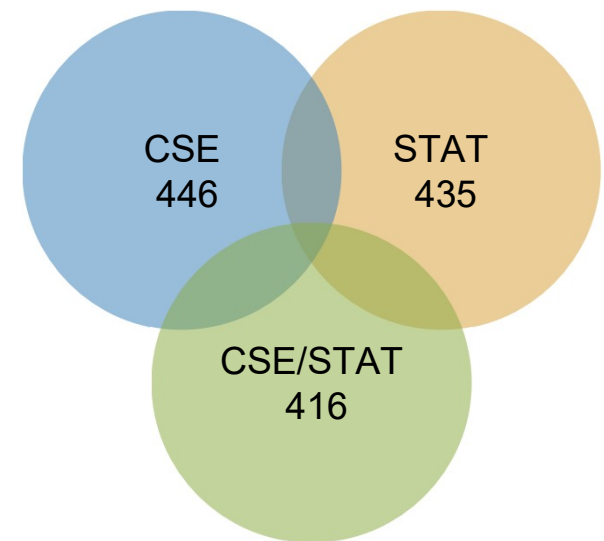
- CSE majors
- Very technical course

## STAT 435

- STAT majors
- Very technical course

## CSE/STAT 416

- Everyone else!
  - This is a super broad audience!
- Give everyone a strong foundational understanding of ML
  - More breadth than other courses, a little less depth



## Level of Course

### **Our Motto**

*Everyone should be able to learn machine learning, so our job is to make tough concepts intuitive and applicable.*

This means...

- Minimize pre-requisite knowledge
- Focus on important ideas, avoid getting bogged down by math
- Maximize ability to develop and deploy
- Use pre-written libraries to do many tasks
- Learn concepts in case studies

Does not mean course isn't fast paced! There are a lot of concepts to cover!

# Course Logistics

# Who am I?



- Hunter Schafer
  - Lecturer
  - Paul G. Allen School for Computer Science & Engineering (CSE)
- Office Hours
  - Time: 12:30 pm - 2:30 pm, Mondays
  - Location: CSE 444
- Contact
  - Personal Matters: [hschafer@cs.washington.edu](mailto:hschafer@cs.washington.edu)
  - Course Content + Logistics: [Piazza](#)

## Who are the TAs?



**Matthew Rockett**  
rockettm@cs

TA



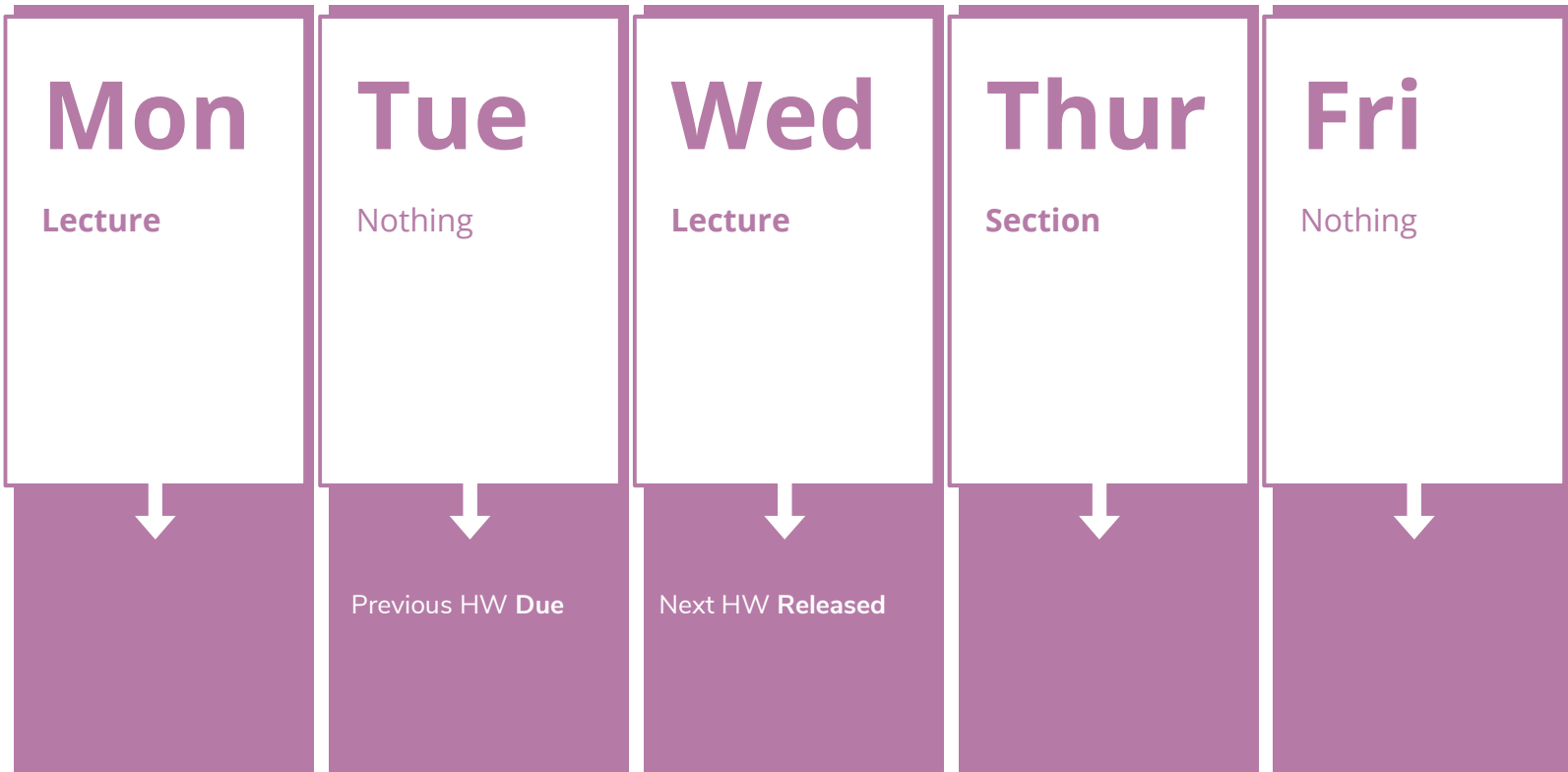
**Josh Ervin**  
joshue@cs

AA (9:40)  
AB (10:50)



**Rahul Biswas**  
rbiswas1@uw

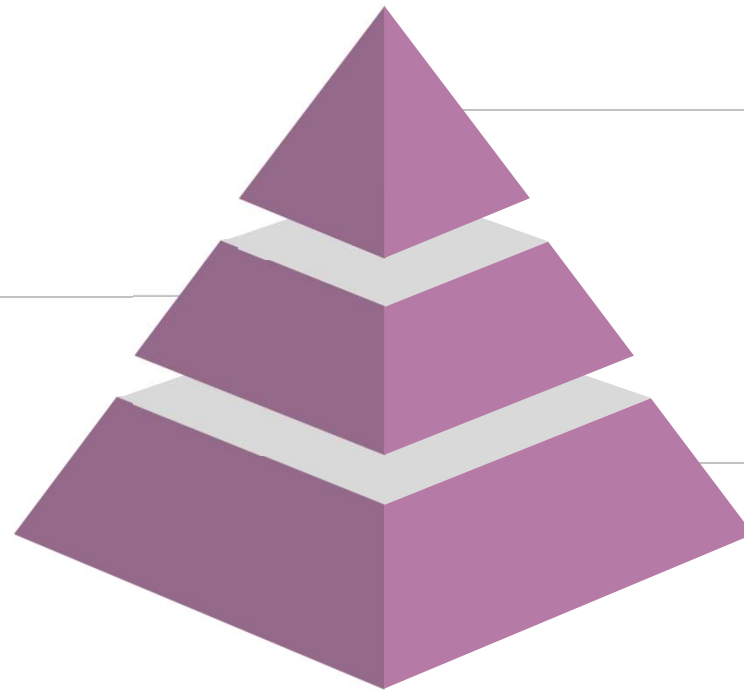
AC (12:00)



- We happen to not record attendance in lectures and section, but attending these sessions is expected
- Panopto for Lecture (on Canvas)







### Homework

With the scaffolding from **1 and 2**, you are probably now capable to tackle the homework. These will be complex and challenging, but you'll continue to **learn by doing**.

1

### Sections

Practice material covered in **1** in a context where a TA can help you.

The emphasis is still on you **learning by doing**.

2

### Lectures

Introduced to material for the first time. Mixed with activities and demos to give you a chance to **learn by doing**.

3

No where near mastery yet!

# Assessment

- **Weekly Homework Assignments**
  - **Weight:** 70%
  - **Number:** Approximately 8
  - Each Assignment has two parts that contribute to your grade separately:
    - Programming (55%)
    - Conceptual (15%)
- **Final Exam**
  - **Weight:** 30%
  - **Date:** Wednesday, August 21 from 9:40 am – 11:50 pm
  - **Location:** GWN 301

# Homework Logistics

- **Late Days**
  - 4 Free Late Days for the whole quarter.
  - Can use up to 2 Late Days on any assignment.
  - Each Late Day used after the 4 Free Late Days results in a -10% on that assignment
- **Collaboration**
  - You are encouraged to discuss assignments and concepts **at a high level**
    - If you have code in front of you in your discussion, probably **NOT** high level
    - Discuss process, not answers
  - All code and answers submitted must be your own
- **Turn In**
  - Everything completed and turned in on Gradescope
  - Multiple “assignments” on Gradescope per assignment

## Poll Everywhere

Pair 

2 minutes

[pollev.com/cse416](http://pollev.com/cse416)

### On your phone

If you could only have one pet, would you rather have a dog or cat?

### When you're done

Introduce yourself to your neighbor, and talk about what you did over summer "break"!



# Case Study 1

*Regression:  
Housing Prices*

# Fitting Data

**Goal:** Predict how much my house is worth

Have data from my neighborhood

*n data points*  
*(x<sub>i</sub>, y<sub>i</sub>)*

$$\left\{ \begin{array}{l} (x_1, y_1) = (2318 \text{ sq.ft.}, \$315k) \\ (x_2, y_2) = (1985 \text{ sq.ft.}, \$295k) \\ (x_3, y_3) = (2861 \text{ sq.ft.}, \$370k) \\ \vdots \\ (x_n, y_n) = (2055 \text{ sq.ft.}, \$320k) \end{array} \right.$$

**Assumption:**

There is a relationship between  $y \in \mathbb{R}$  and  $x \in \mathbb{R}^d$

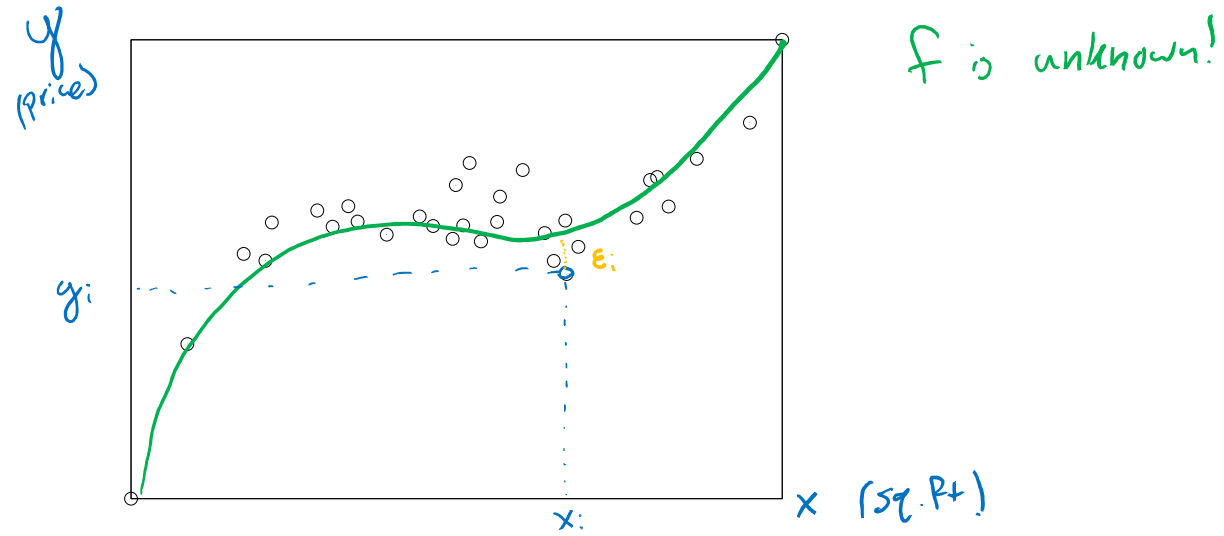
$$y \approx f(x)$$

$x$  is the **input data**. Can potentially have many inputs

$y$  is the **outcome/response/target/label/dependent variable**

# Model

A **model** is how we assume the world works



Regression model:

$$y_i = f(x_i) + \epsilon_i$$

$$E[\epsilon_i] = 0$$

*← expectation*

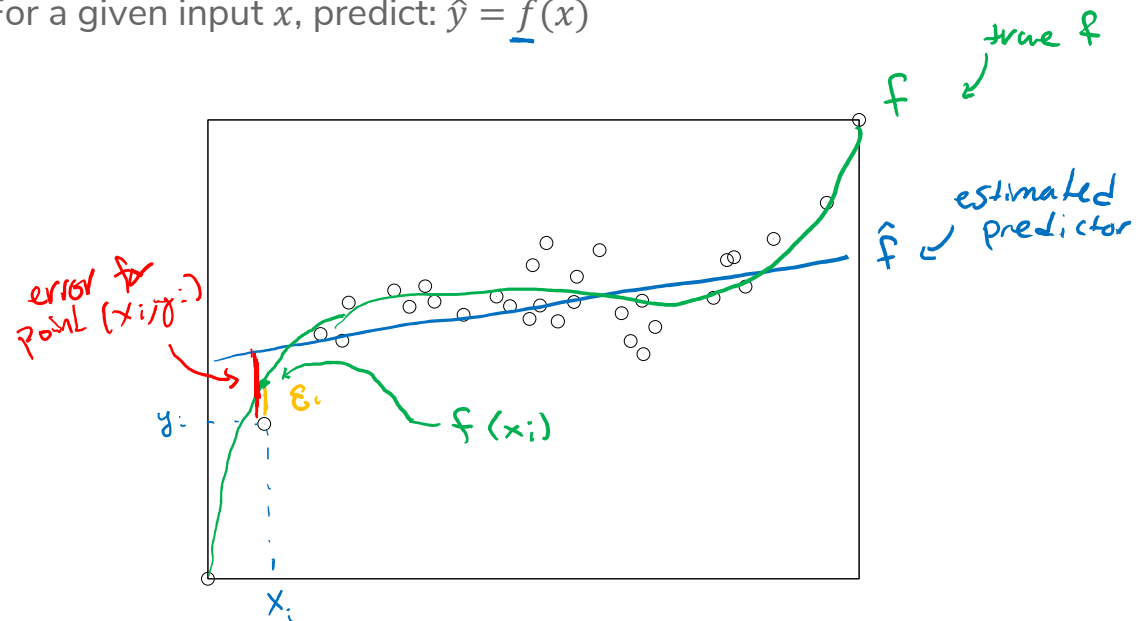
“Essentially, all models are wrong, but some are useful.”  
- George Box, 1987

# Predictor

We don't know  $f$ ! We need to learn it from the data!

Use machine learning to learn a predictor  $\hat{f}$  from the data

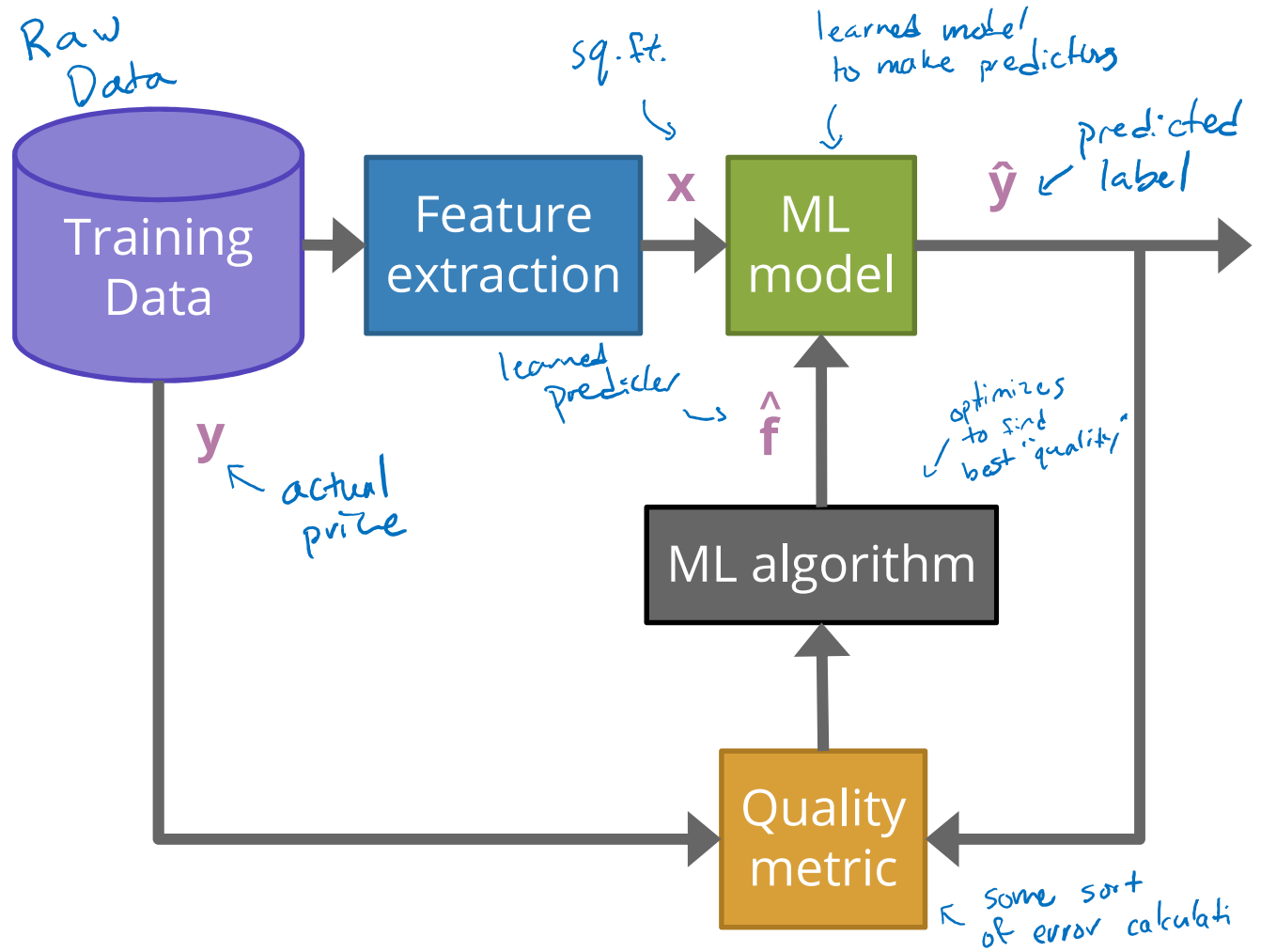
For a given input  $x$ , predict:  $\hat{y} = \hat{f}(x)$



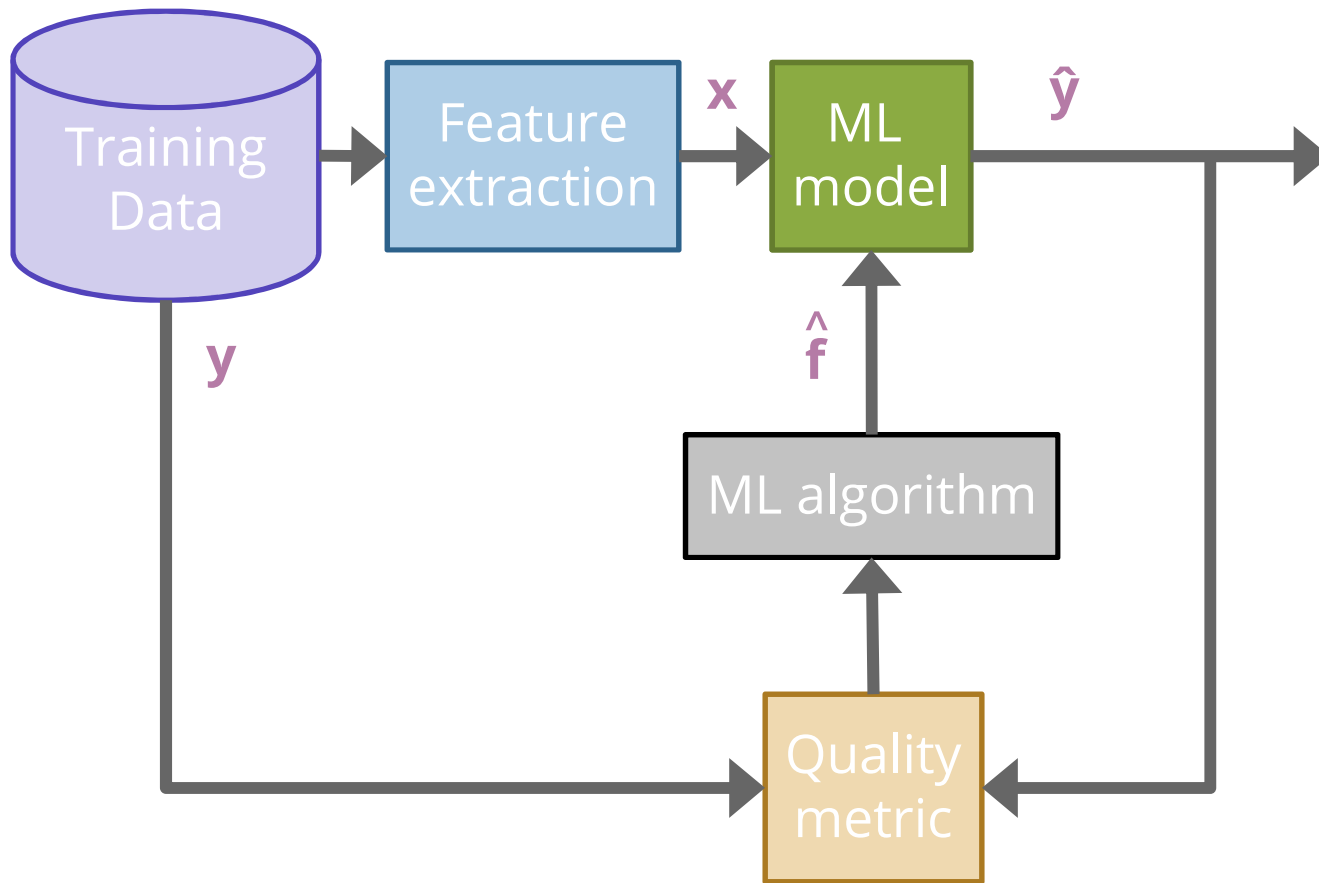
Small error on an example, means we had a good fit for that point



# ML Pipeline



# Linear Regression



# Linear Regression Model

Assume the data is produced by a line.

$$y_i = \underbrace{w_0 + w_1 x_i}_{f(x_i)} + \epsilon_i$$

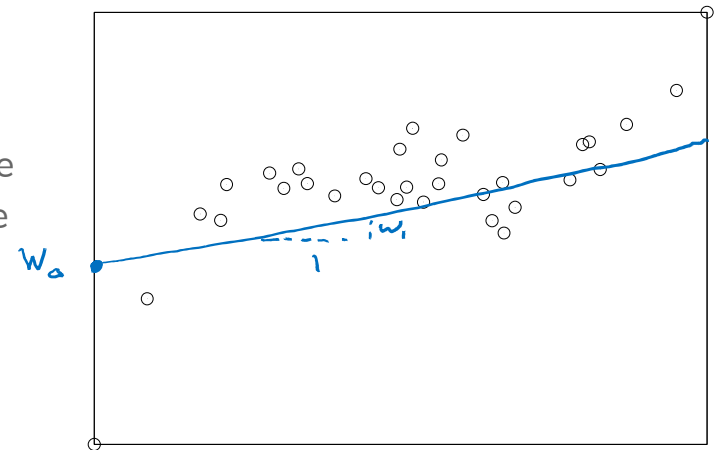
$w_0, w_1$  are the **parameters** of our model that need to be learned

- $w_0$  is the intercept (\$ of the land with no house)
- $w_1$  is the slope (\$ increase per increase in sq. ft)

Learn estimates of these parameters  $\hat{w}_0, \hat{w}_1$  and use them to predict new value for any input  $x$ !

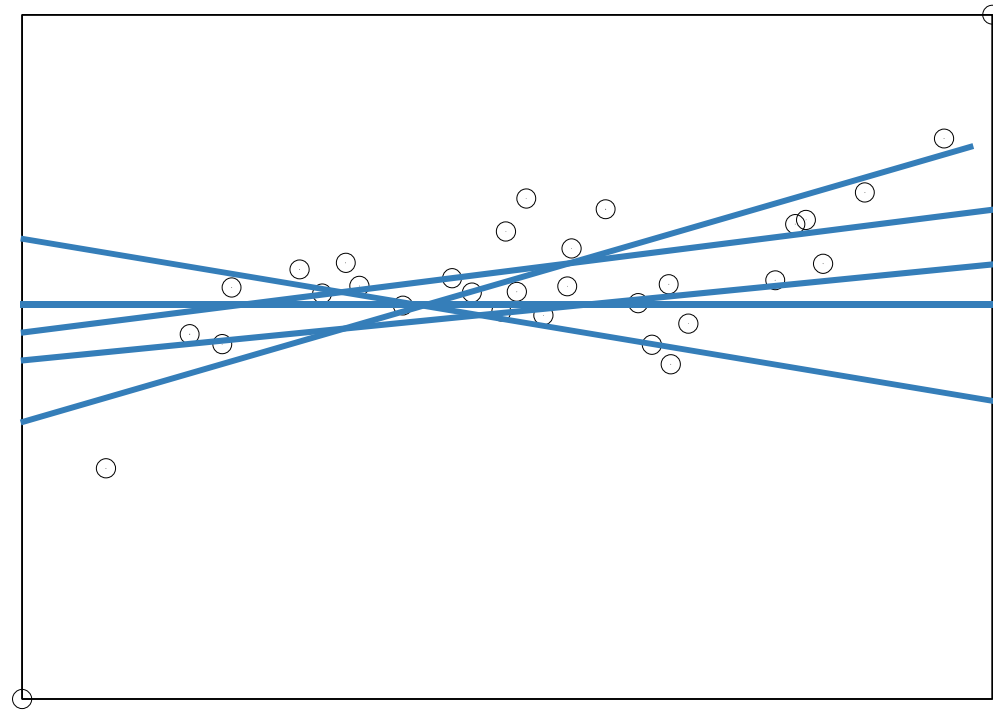
$$\hat{y} = \underbrace{\hat{w}_0 + \hat{w}_1 x}_{\hat{f}(x)}$$

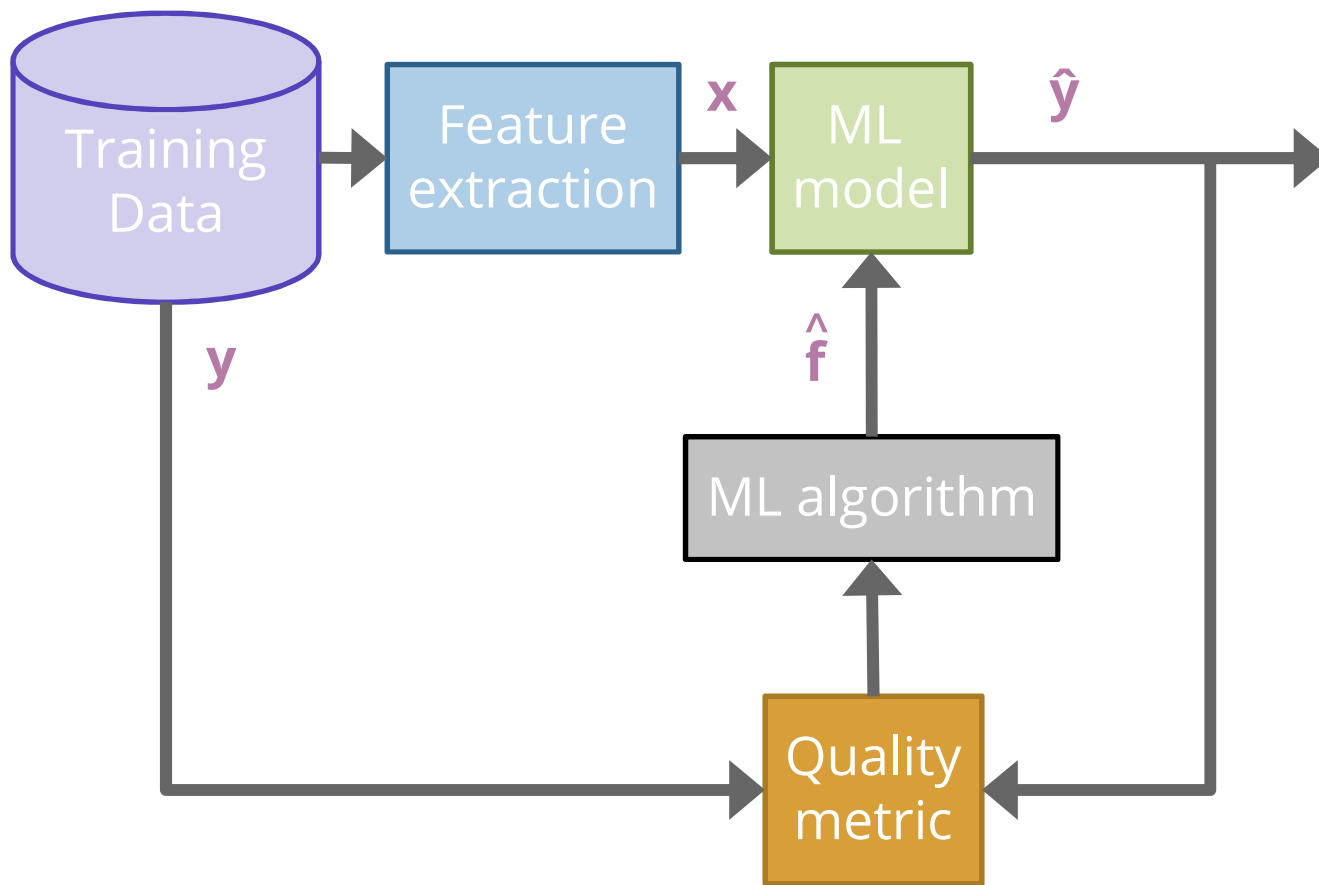
Why don't we add  $\epsilon$ ?



# Basic Idea

Try a bunch of different lines and see which one is best!  
What does best even mean here?





## “Cost” of predictor

Define a “cost” for a particular setting of parameters

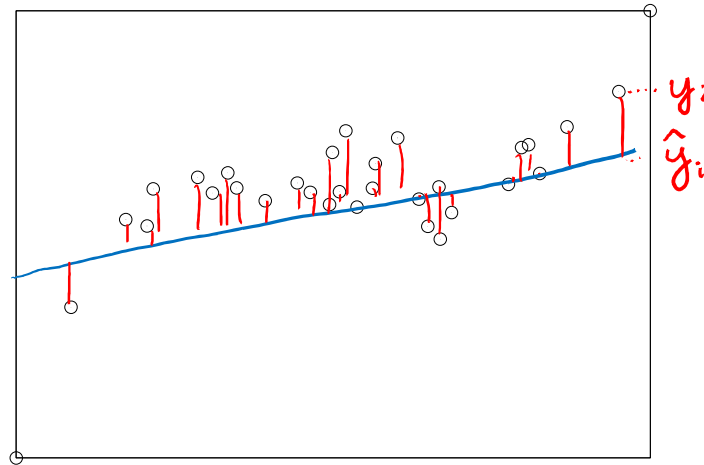
- Low cost → Better fit
- Find settings that minimize the cost
- For regression, we will use the error as the cost.
  - Low error = Low cost = Better ~~model~~ (hopefully)  
*predictor*

Note: There are other ways we can define cost which will result in different “best” predictors. We will see what these other costs are and how they affect the result.

## Residual Sum of Squares (RSS)

How to define error? **Residual sum of squares (RSS)**

$$\begin{aligned} \text{RSS}(w_0, w_1) &= (y_1 - \hat{y}_1)^2 + (y_2 - \hat{y}_2)^2 + \dots + (y_n - \hat{y}_n)^2 \\ &= \sum_{i=1}^n (y_i - \hat{y}_i)^2 \\ &= \sum_{i=1}^n (y_i - (w_0 + w_1 x_i))^2 \end{aligned}$$



Note

Many people use  
mean-square error (MSE)

$$\text{MSE}(w_0, w_1) = \frac{1}{n} \text{RSS}(w_0, w_1)$$





## Poll Everywhere

[pollev.com/cse416](https://pollev.com/cse416)

- **Goal:** Get you actively participating in your learning
- Typical Activity
  - Question is posed
  - **Think** (1 min): Think about the question on your own
  - **Pair** (2 min): Talk with your neighbor to discuss question
    - If you arrive at different conclusions, discuss your logic and figure out why you differ!
    - If you arrived at the same conclusion, discuss why the other answers might be wrong!
  - **Share** (1 min): We discuss the conclusions as a class
- During each of the **Think** and **Pair** stages, you will respond to the question via a Poll Everywhere poll
  - The poll will only be open for the last **15** seconds of each of the stage
  - Not worth any points, just here to help you learn!

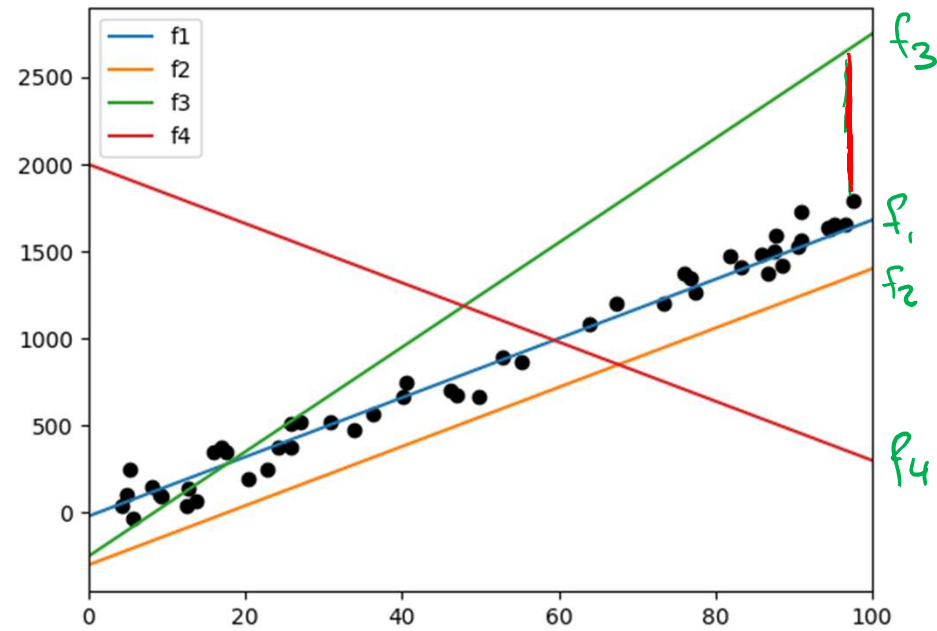
# Poll Everywhere

Think 

1 min

[pollev.com/cse416](http://pollev.com/cse416)

Sort the following lines by their RSS on the data, from smallest to largest. (estimate, don't actually compute)



$f_1 < f_2 < f_3 < f_4$

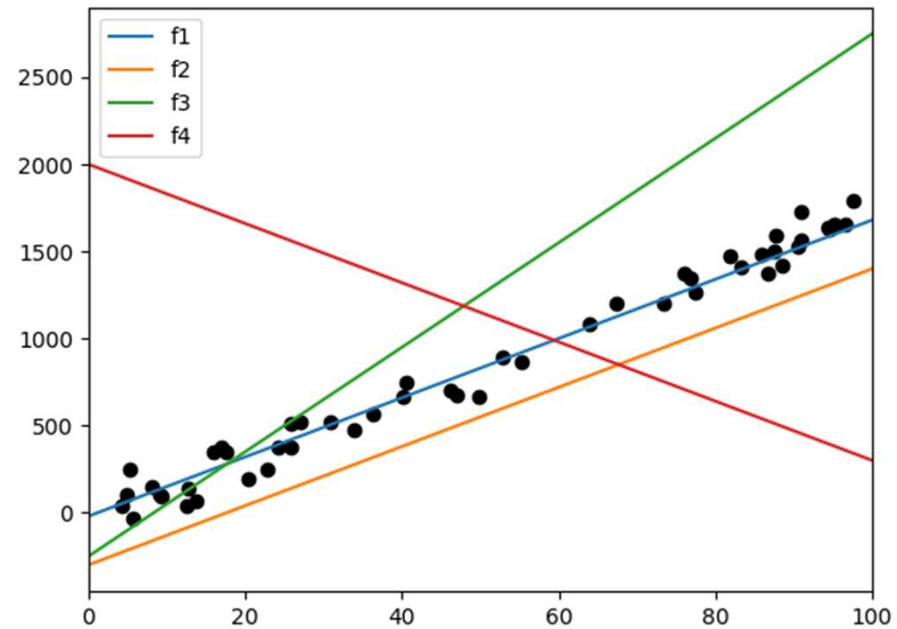
# Poll Everywhere

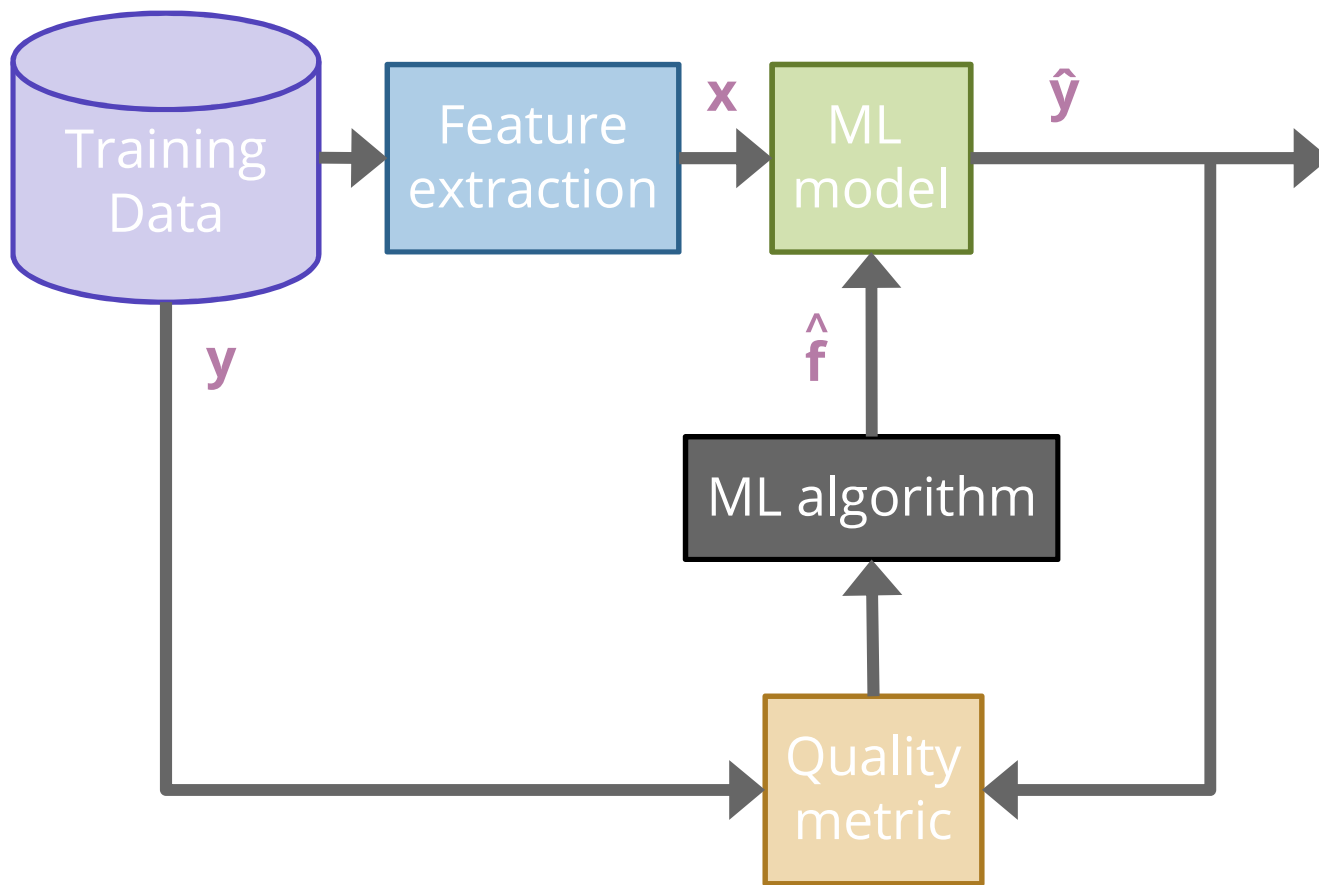
Pair 

2 min

[pollev.com/cse416](http://pollev.com/cse416)

Sort the following lines by their RSS on the data, from smallest to largest. (estimate, don't actually compute)

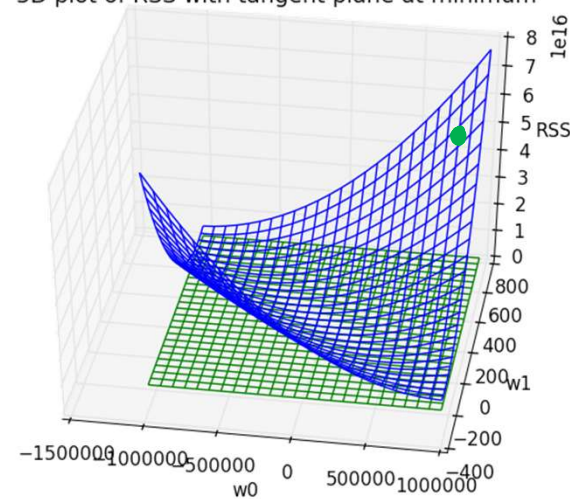




# Minimizing Cost

RSS is a function with inputs  $w_0, w_1$ , different settings have different RSS for a dataset

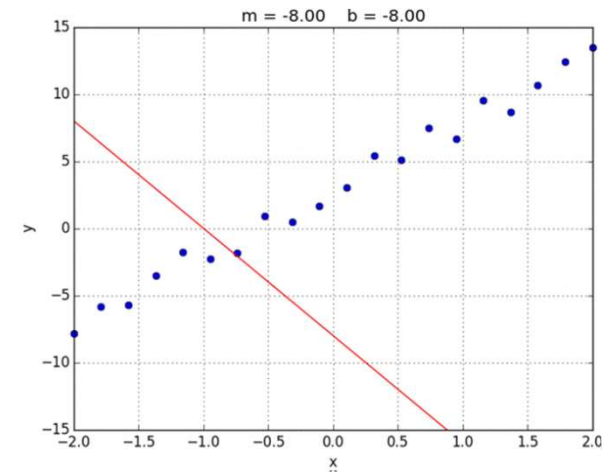
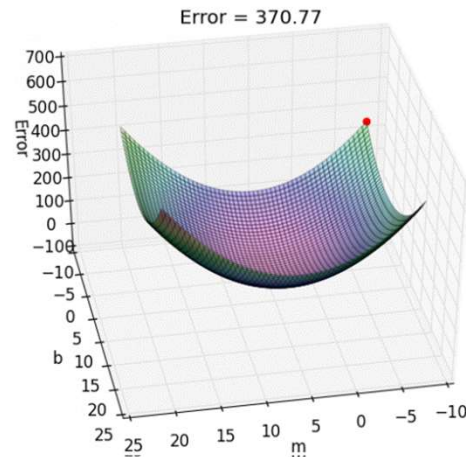
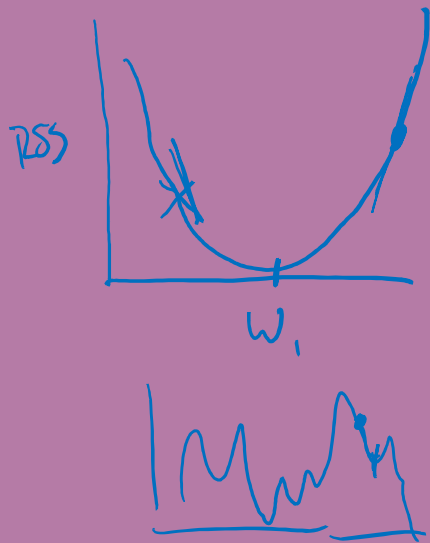
3D plot of RSS with tangent plane at minimum



$$\begin{aligned}\hat{w}_0, \hat{w}_1 &= \min_{w_0, w_1} \text{RSS}(w_0, w_1) \\ &= \min_{w_0, w_1} \sum_{i=1}^n (y_i - (w_0 + w_1 x_i))^2\end{aligned}$$

Unfortunately, we can't try it out on all possible settings ☹️

# Gradient Descent



Instead of computing all possible points to find the minimum, just start at one point and “roll” down the hill. Use the gradient (slope) to determine which direction is down.

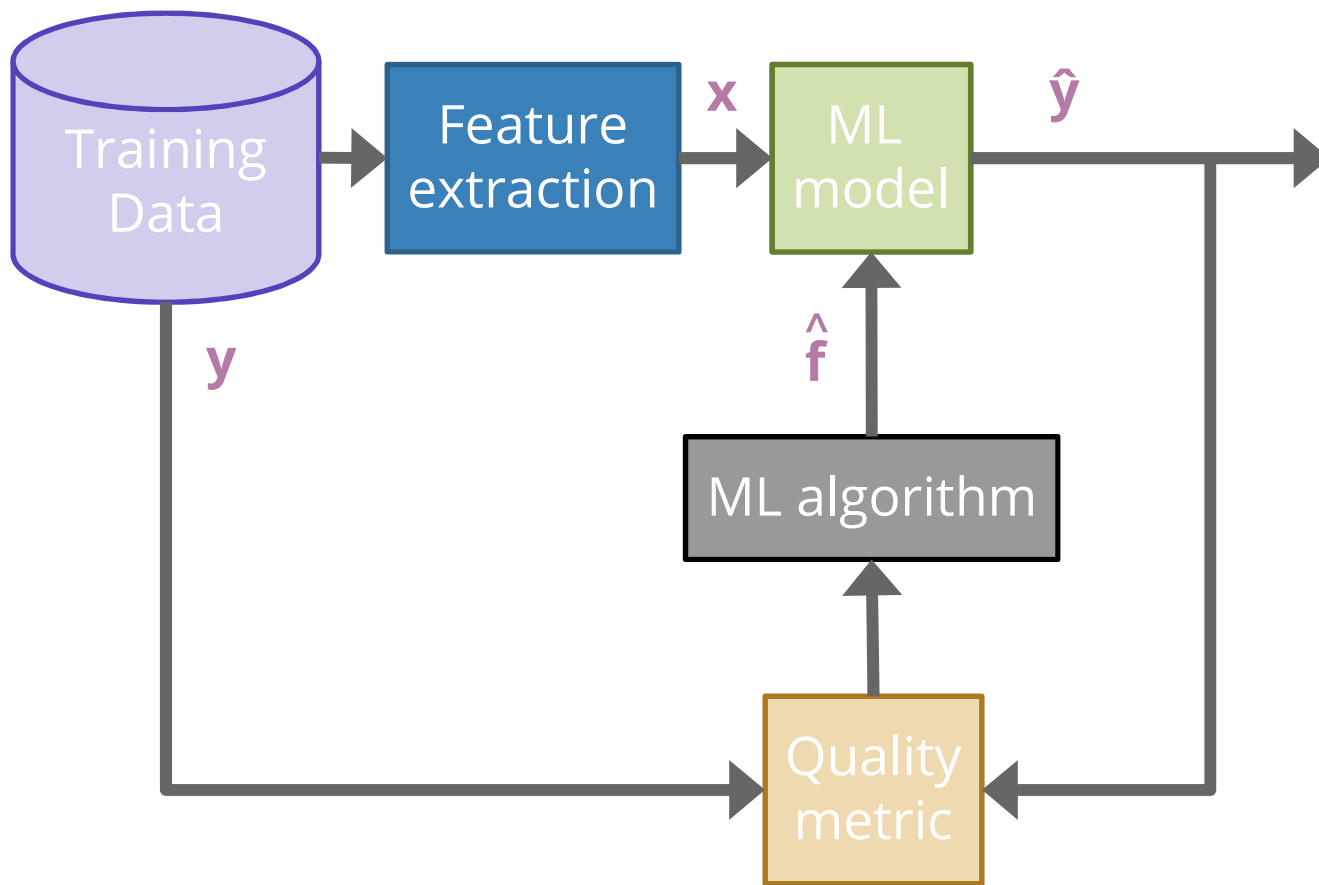
start at some (random) point  $w^{(0)}$  when  $t = 0$   
while we haven't converged:

$$w^{(t+1)} = w^{(t)} - \eta \nabla R_{SS}(w^{(t)})$$



Brain Break







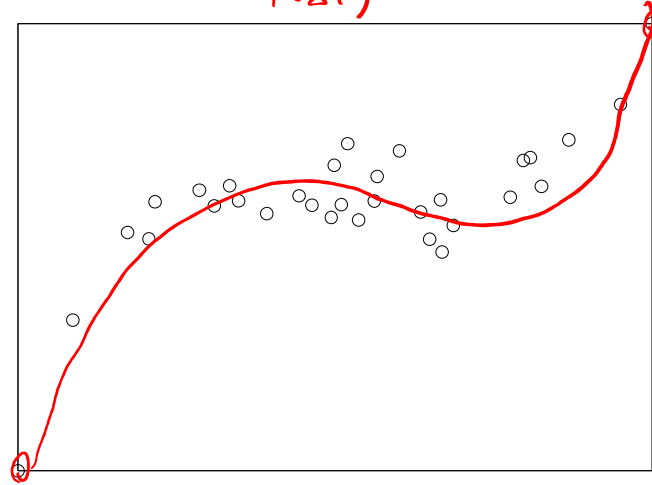
# Higher Order Features

This data doesn't look exactly linear, why are we fitting a line instead of some higher-degree polynomial?

We can! We just have to use a slightly different model!

$$y_i = w_0 + w_1x_i + w_2x_i^2 + w_3x_i^3 + \epsilon_i$$

$f(x_i)$



# Polynomial Regression

## Model

$$y_i = w_0 + w_1x_i + w_2x_i^2 + \dots + w_px_i^p + \epsilon_i$$

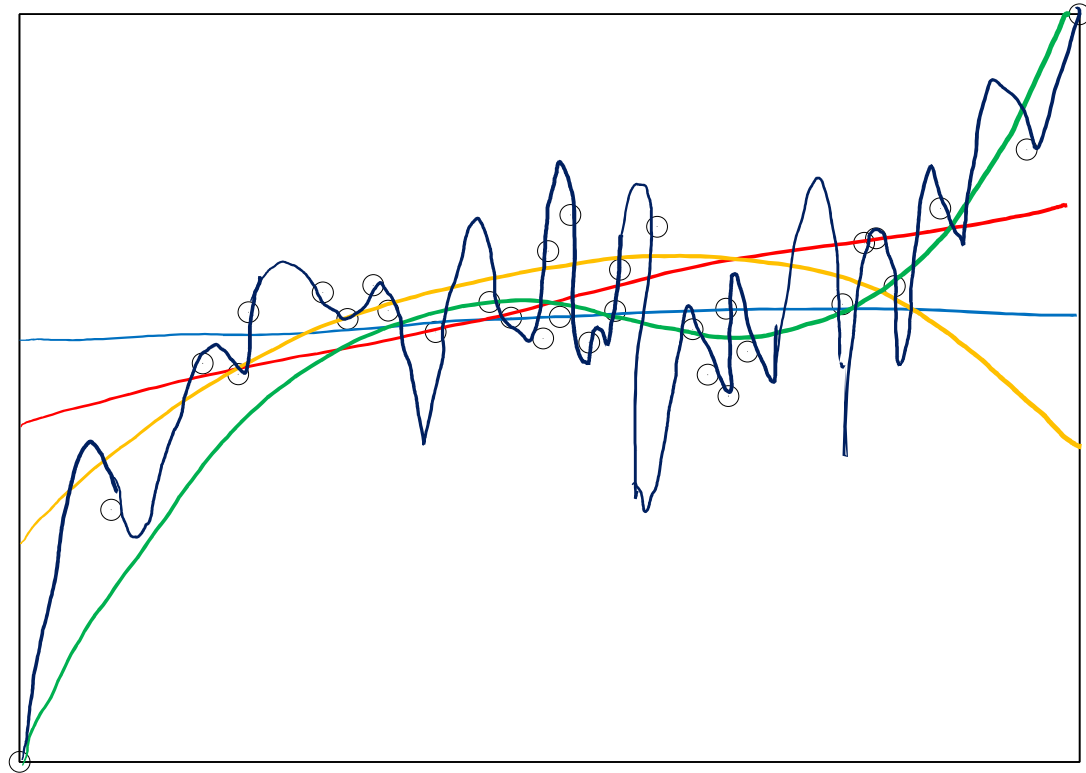
Just like linear regression, but uses more features!

Feature	Value	Parameter
0	1 (constant)	$w_0$
1	$x$	$w_1$
2	$x^2$	$w_2$
...	...	...
p	$x^p$	$w_p$

How do you train it? Gradient descent (with more parameters)

# Polynomial Regression

$p: 0 \quad 1 \quad 2 \quad 3 \quad \dots \quad 32$



How to decide what the right degree? Come back Wednesday!

# Features

**Features** are the values we select or compute from the data inputs to put into our model. **Feature extraction** is the process of turning the data into features.

## Model

$$y_i = w_0 h_0(x_i) + w_1 h_1(x_i) + \dots + w_D h_D(x_i) + \epsilon_i$$
$$= \sum_{j=0}^D w_j h_j(x_i) + \epsilon_i$$

Feature	Value	Parameter
0	$h_0(x)$ often 1 (constant)	$w_0$
1	$h_1(x)$ $x^2 + x$	$w_1$
2	$h_2(x)$ $e^x$	$w_2$
...	...	...
D	$h_D(x)$ $\log(x)$	$w_D$

## Adding Other Inputs

Generally we are given a data table of values we might look at that include more than one value per house.

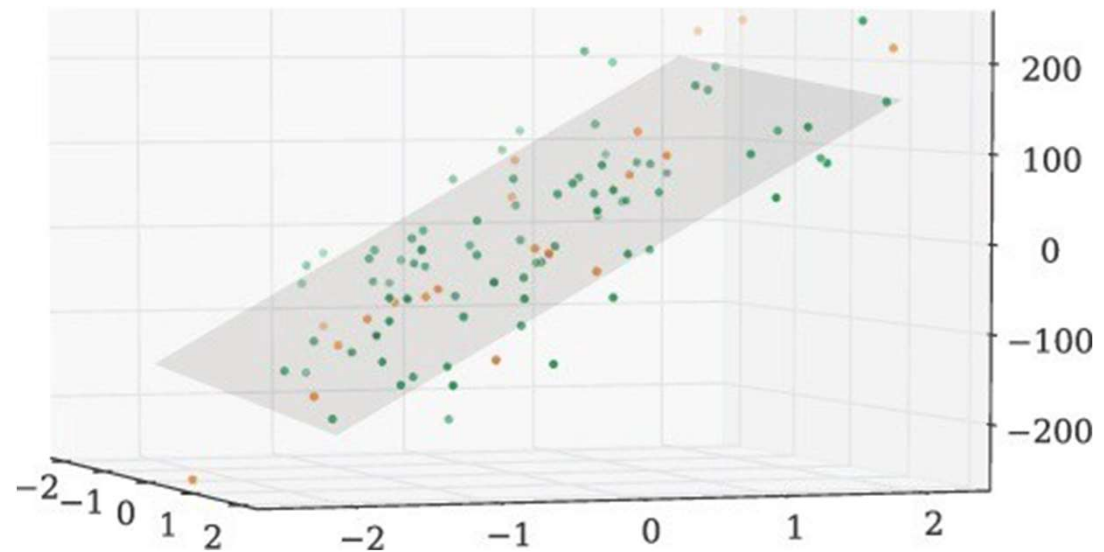
- Each row is a single house.
- Each column (except Value) is a data input.

sq. ft.	# bathrooms	owner's age	...	value
1400	3	47	...	70,800
700	3	19	...	65,000
...	...	...	...	...
1250	2	36	...	100,000

## More Inputs - Visually

Adding more features to the model allows for more complex relationships to be learned

$$y_i = w_0 + w_1(\text{sq. ft.}) + w_2(\text{\# bathrooms}) + \epsilon_i$$



Coefficients tell us the rate of change if all other features are constant

# Notation

**Important:** Distinction is the difference between a *data input* and a *feature*.

- Data inputs are columns of the raw data
- Features are the values (possibly transformed) for the model (done after our feature extraction  $h(x)$ )

Data Input:  $x_i = (x_i[1], x_i[2], \dots, x_i[d])$

Output:  $y_i$

- $x_i$  is the  $i^{th}$  row
- $x_i[j]$  is the  $i^{th}$  row's  $j^{th}$  data input
- $h_j(x_i)$  is the  $j^{th}$  feature of the  $i^{th}$  row

# Features

You can use anything you want as features and include as many of them as you want!

Generally, more features means a more complex model. This might not always be a good thing!

Choosing good features is a bit of an art.

Feature	Value	Parameter
0	1 (constant)	$w_0$
1	$h_1(x) \dots x[1] = \text{sq. ft.}$	$w_1$
2	$h_2(x) \dots x[2] = \# \text{ bath}$	$w_2$
...	...	...
D	$h_D(x) \dots \text{like } \log(x[7]) * x[2]$	$w_D$



# Linear Regression Recap

## Dataset

$\{(x_i, y_i)\}_{i=1}^n$  where  $x \in \mathbb{R}^d$ ,  $y \in \mathbb{R}$

## Feature Extraction

$h(x): \mathbb{R}^d \rightarrow \mathbb{R}^D$

$h(x) = (h_0(x), h_1(x), \dots, h_D(x))$

## Regression Model

$y = f(x) + \epsilon$

$$\begin{aligned} &= \sum_{j=0}^D w_j h_j(x) + \epsilon \\ &= w^T h(x) + \epsilon \end{aligned}$$

## Quality Metric

$$RSS(w) = \sum_{i=1}^n (y_i - w^T x_i)^2$$

## Predictor

$$\hat{w} = \min_w RSS(w)$$

## ML Algorithm

Optimized using Gradient Descent

## Prediction

$$\hat{y} = \hat{w}^T h(x)$$

