

# Introduction to Database Systems

## CSE 414

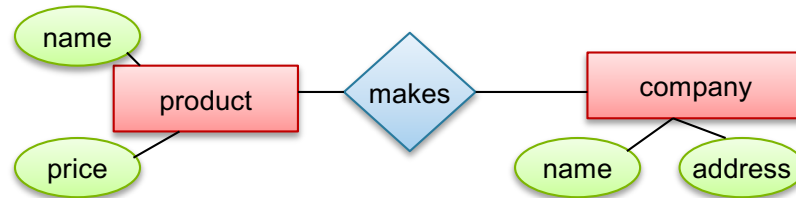
### Lecture 20: Design Theory

# Class Overview

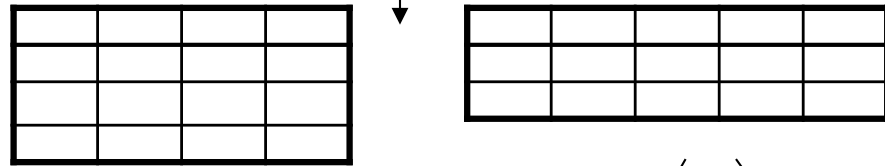
- Unit 1: Intro
- Unit 2: Relational Data Models and Query Languages
- Unit 3: Non-relational data
- Unit 4: RDMBS internals and query optimization
- Unit 5: Parallel query processing
- Unit 6: DBMS usability, conceptual design
  - E/R diagrams
  - Schema normalization
- Unit 7: Transactions

# Database Design Process

Conceptual Model:

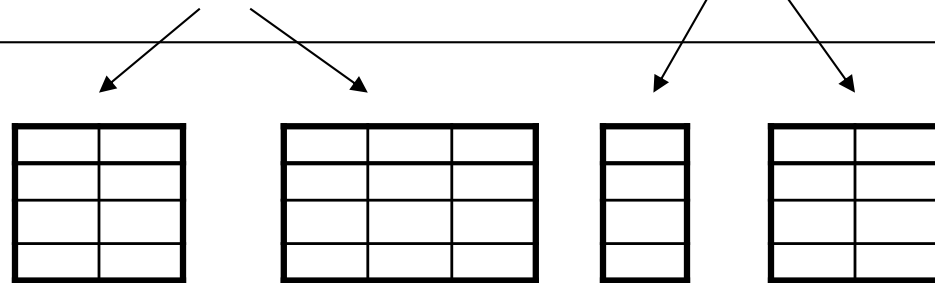


Relational Model:  
Tables + constraints  
And also functional dep.



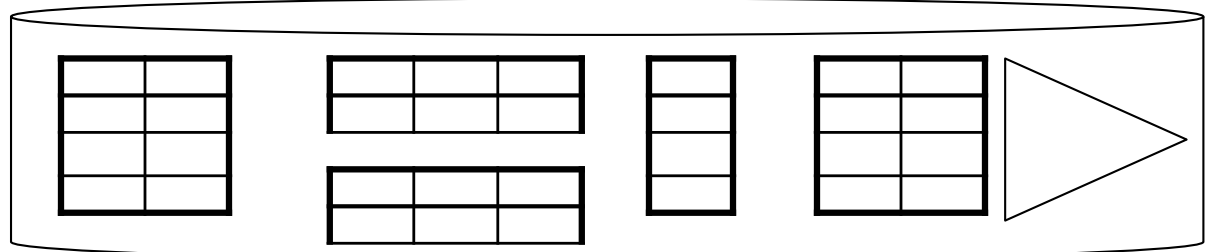
Normalization:  
Eliminates anomalies

Conceptual Schema



Physical storage details

Physical Schema



# Entity / Relationship Diagrams

- Entity set = a class
  - An entity = an object



Product

- Attribute



city

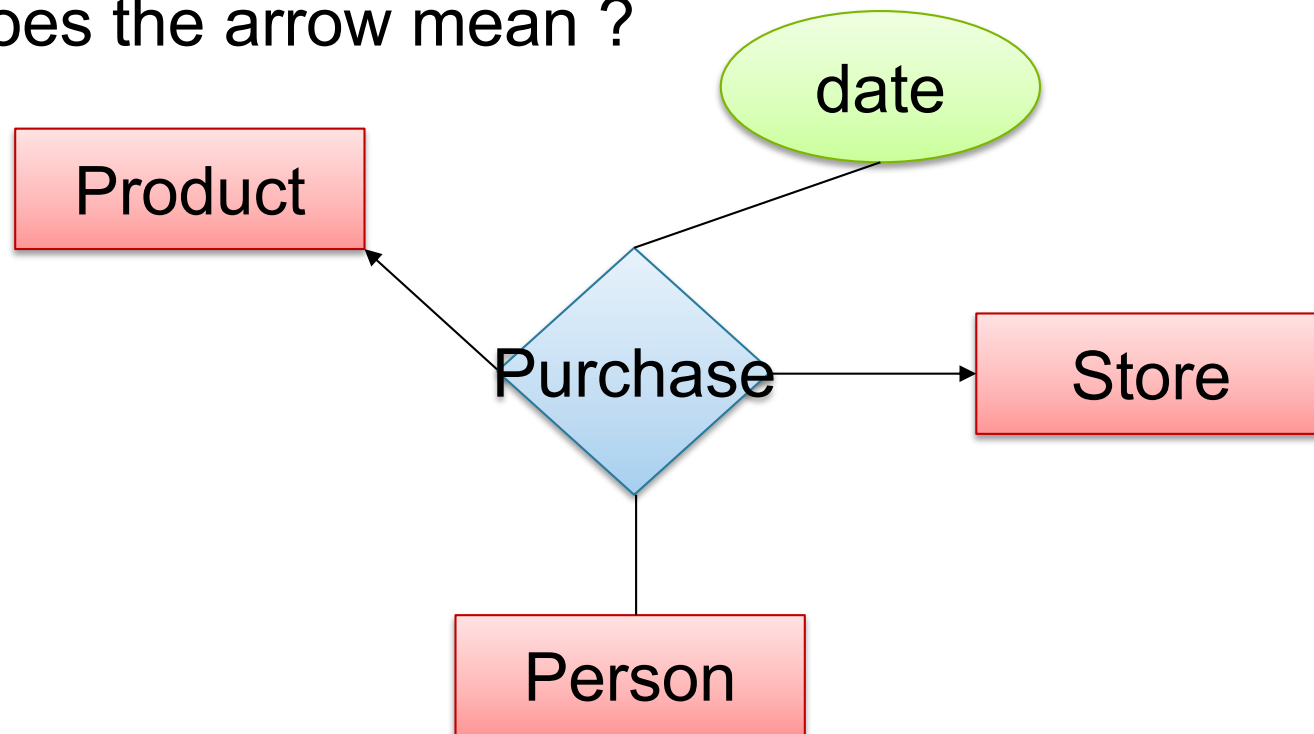
- Relationship



makes

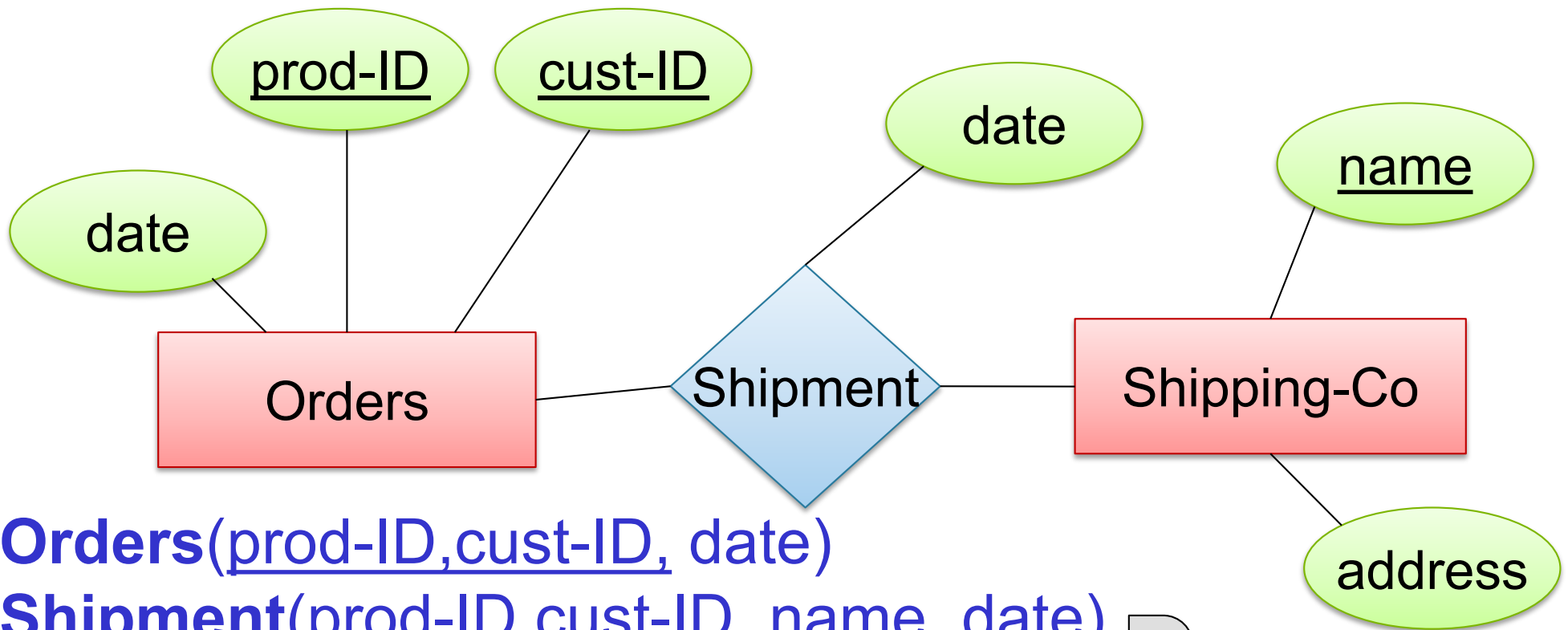
# Arrows in Multiway Relationships

**Q:** What does the arrow mean ?



**A:** Any person buys a given product from at most one store  
AND every store sells to every person at most one product

# N-N Relationships to Relations



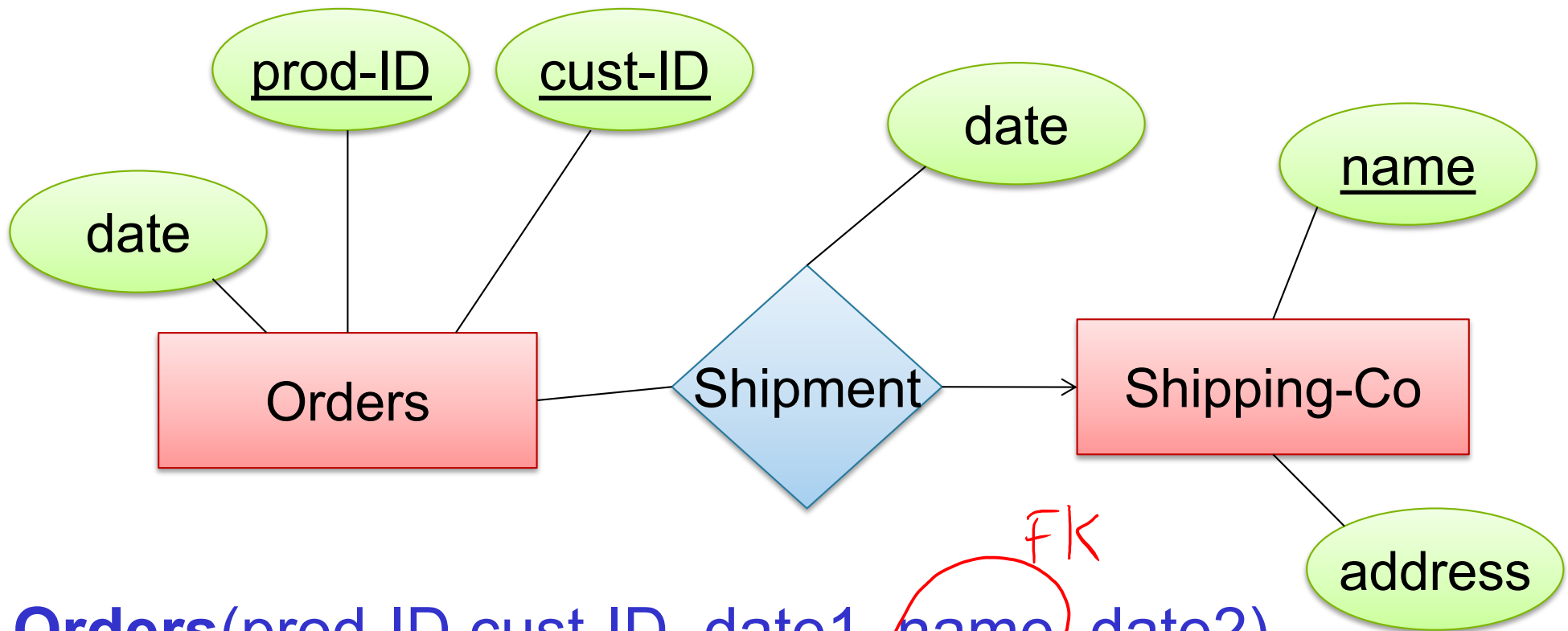
**Orders**(prod-ID, cust-ID, date)

**Shipment**(prod-ID, cust-ID, name, date)

**Shipping-Co**(name, address)

<u>prod-ID</u>	<u>cust-ID</u>	<u>name</u>	date
Gizmo55	Joe12	UPS	4/10/2011
Gizmo55	Joe12	FEDEX	4/9/2011

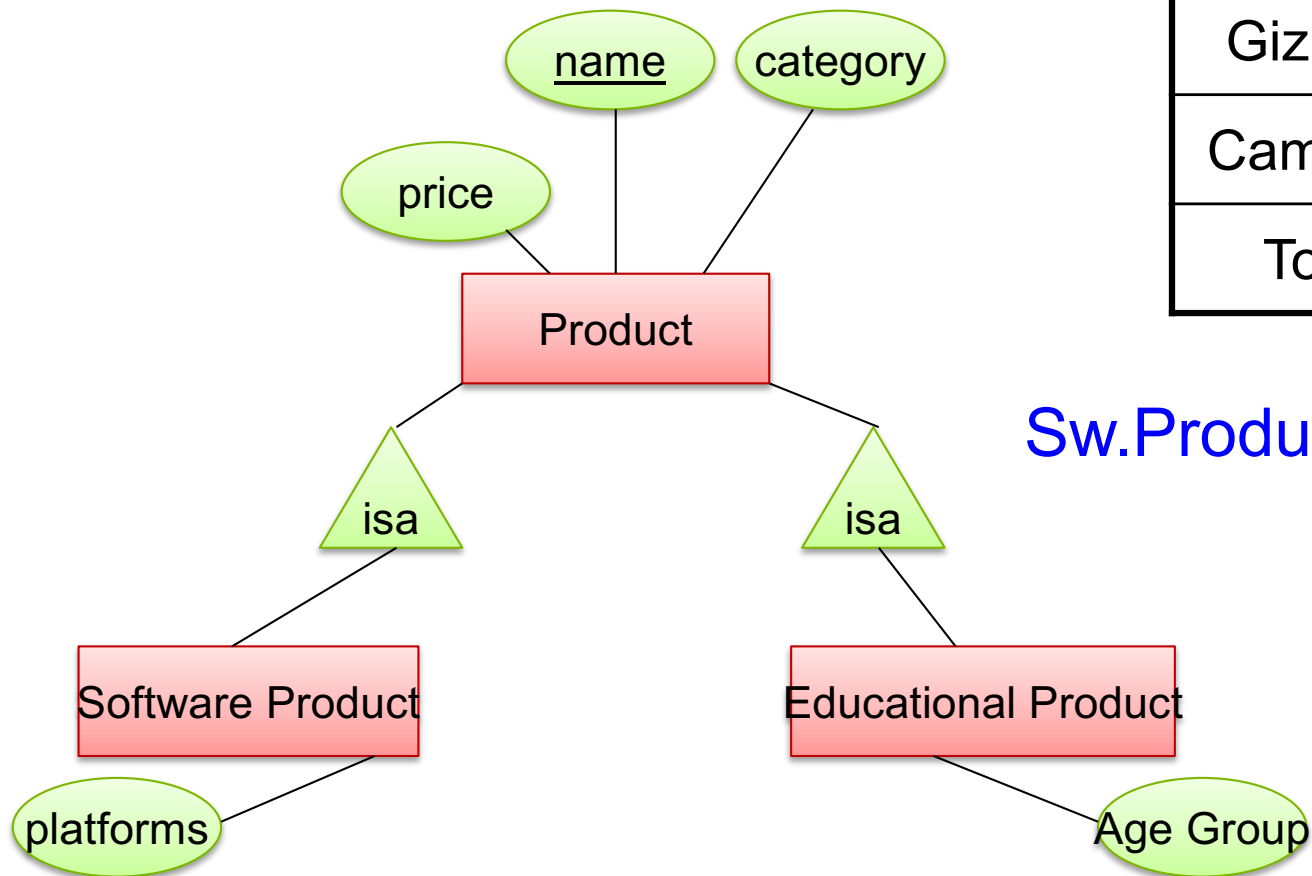
# N-1 Relationships to Relations



**Orders**(prod-ID, cust-ID, date1, name, date2)  
**Shipping-Co**(name, address)

Remember: no separate relations for many-one relationship

# Subclasses to Relations



Product

<u>Name</u>	Price	Category
Gizmo	99	gadget
Camera	49	photo
Toy	39	gadget

Sw.Product

<u>Name</u>	platforms
Gizmo	unix

Ed.Product

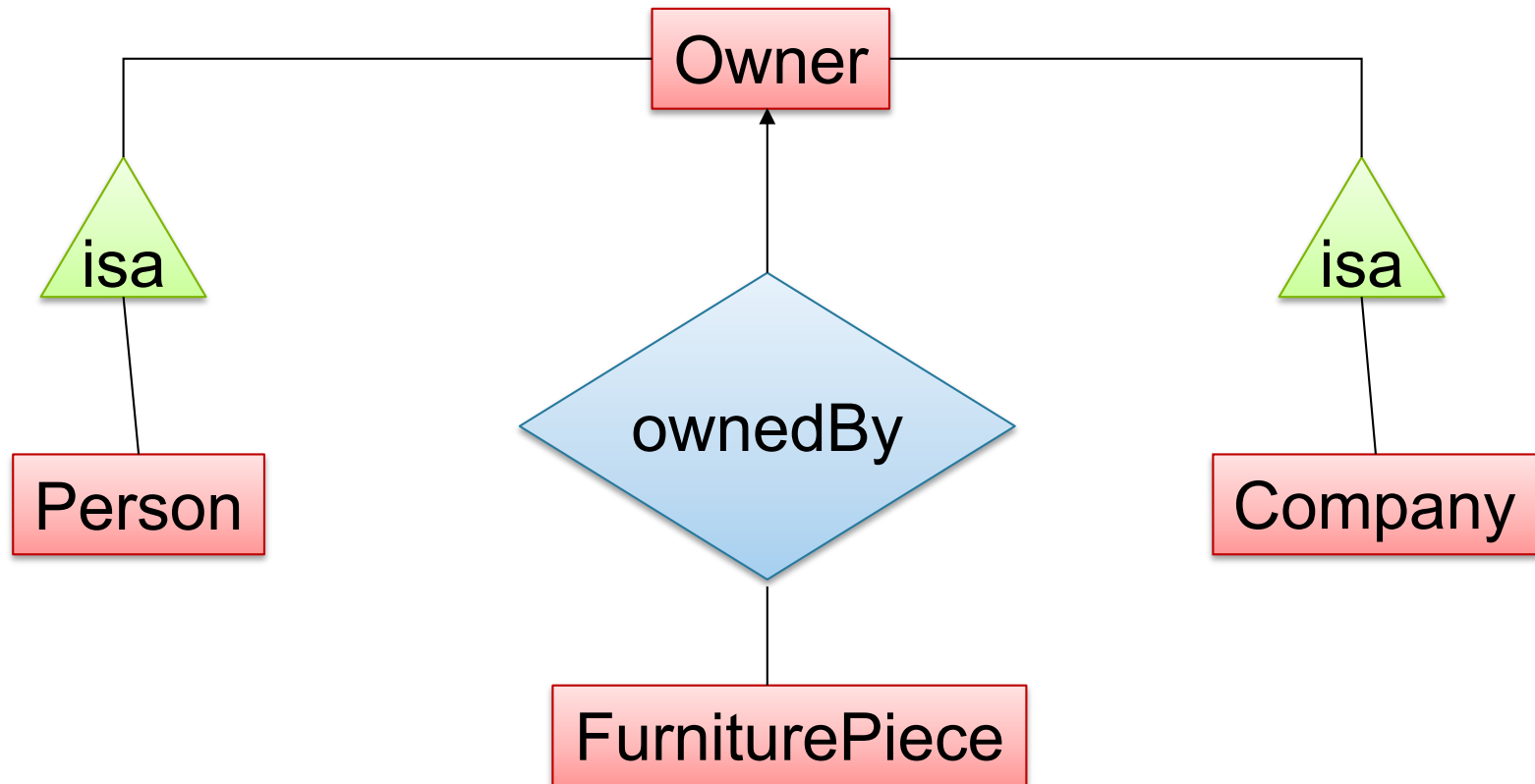
<u>Name</u>	Age Group
Gizmo	toddler
Toy	retired

Other ways to convert are possible



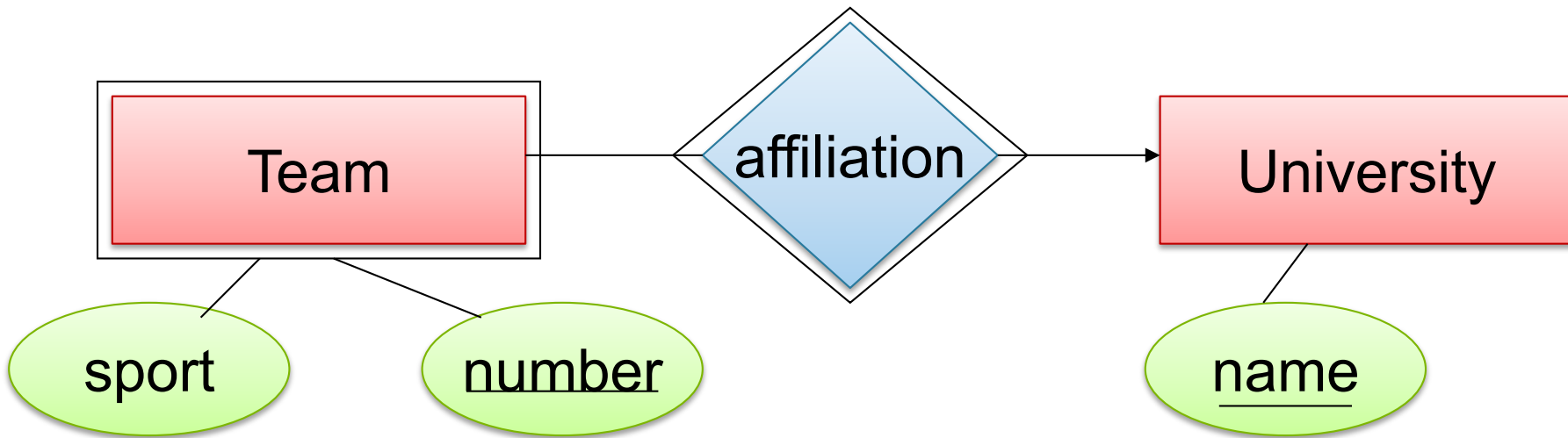
# Modeling Union Types with Subclasses

Solution 2: better, more laborious



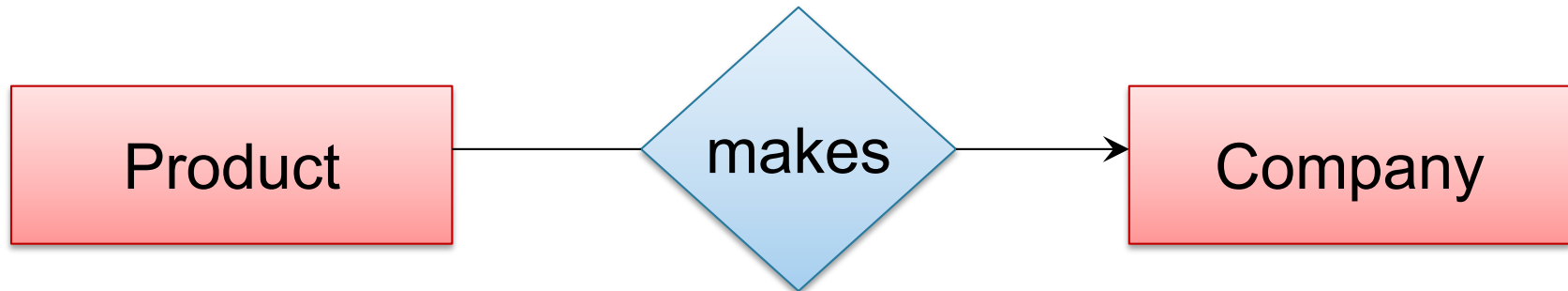
# Weak Entity Sets

Entity sets are weak as their key comes from other classes to which they are related.

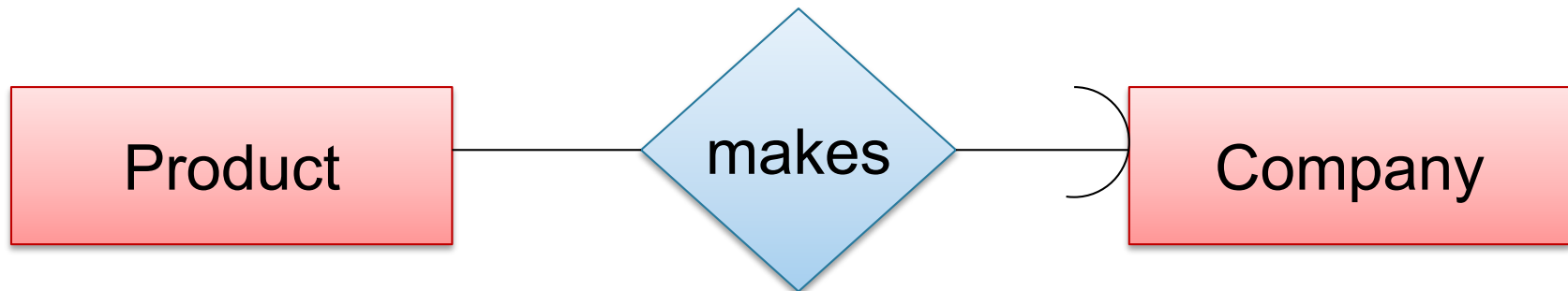


Team(sport, number, universityName)  
University(name)

# Referential Integrity Constraints

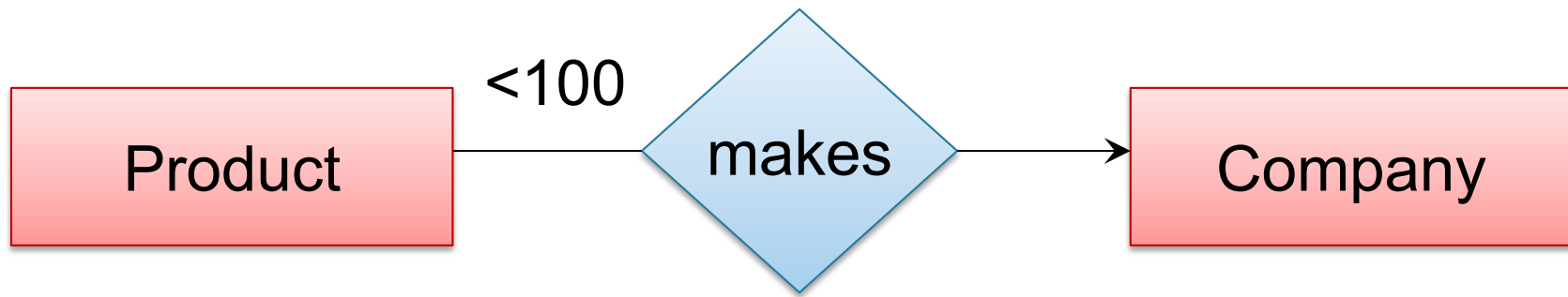


Each product made by at most one company.  
Some products made by no company



Each product made by exactly one company.

# Other Constraints



Q: What does this mean ?

A: A Company entity cannot be connected by relationship to more than 99 Product entities

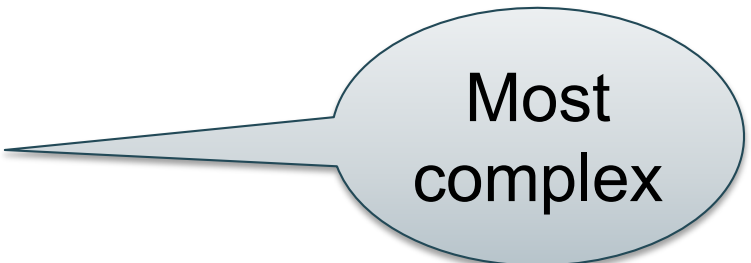
# Constraints in SQL

Constraints in SQL:

- **Keys, foreign keys**
- **Attribute-level** constraints
- **Tuple-level** constraints
- **Global** constraints: assertions



simplest



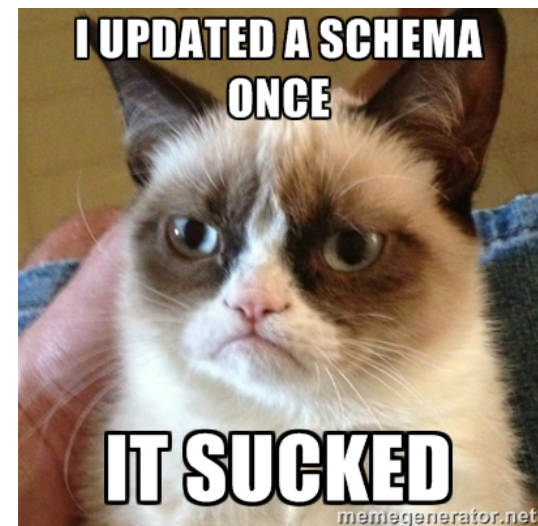
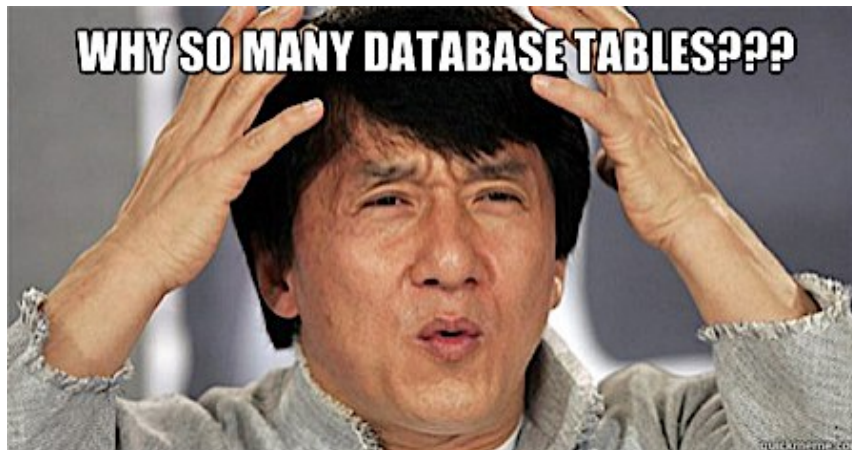
Most  
complex

- The more complex the constraint, the harder it is to check and to enforce

# What happens when data changes?

- SQL has three policies for maintaining referential integrity:
- NO ACTION reject violating modifications (default)
- CASCADE after delete/update do delete/update
- SET NULL set foreign-key field to NULL
- SET DEFAULT set foreign-key field to default value
  - need to be declared with column, e.g.,  
`CREATE TABLE Product (pid INT DEFAULT 42)`

# What makes good schemas?



# Relational Schema Design

Name	<u>SSN</u>	<u>PhoneNumber</u>	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

One person may have multiple phones, but lives in only one city

Primary key is thus (SSN, PhoneNumber)

What is the problem with this schema?



# Relational Schema Design

Name	<u>SSN</u>	<u>PhoneNumber</u>	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
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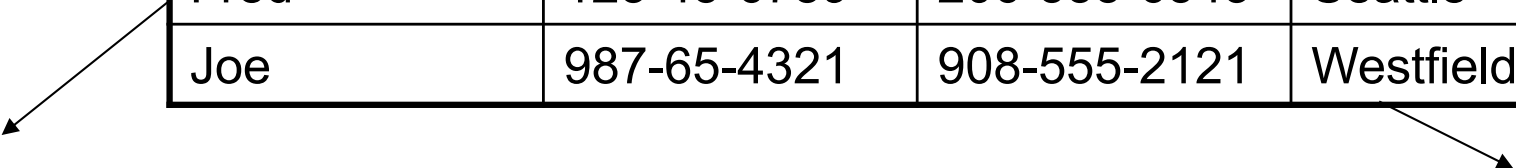
## Anomalies:

- Redundancy = repeat data
- Update anomalies = what if Fred moves to “Bellevue”?
- Deletion anomalies = what if Joe deletes his phone number?

# Relation Decomposition

**Break the relation into two:**

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield



Name	<u>SSN</u>	City
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield

<u>SSN</u>	<u>PhoneNumber</u>
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121

**Anomalies have gone:**

- No more repeated data
- Easy to move Fred to “Bellevue” (how ?)
- Easy to delete all Joe’s phone numbers (how ?)

# Relational Schema Design (or Logical Design)

How do we do this systematically?

- Start with some relational schema
- Find out its **functional dependencies** (FDs)
- Use FDs to **normalize** the relational schema

# Functional Dependencies (FDs)

## Definition

If two tuples agree on the attributes

$A_1, A_2, \dots, A_n$

then they must also agree on the attributes

$B_1, B_2, \dots, B_m$

Formally:

$A_1 \dots A_n$  **determines**  $B_1 \dots B_m$

$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$

# Functional Dependencies (FDs)

**Definition**  $A_1, \dots, A_m \rightarrow B_1, \dots, B_n$  holds in R if:

for all  $\forall t, t' \in R$ ,  
 (  $t.A_1 = t'.A_1 \wedge \dots \wedge t.A_m = t'.A_m \rightarrow t.B_1 = t'.B_1 \wedge \dots \wedge t.B_n = t'.B_n$  )

R	$A_1$	...	$A_m$		$B_1$	...	$B_n$		
t									
t'									

if  $t, t'$  agree here then  $t, t'$  agree here

# Example

An FD holds, or does not hold on an instance:

<b>EmpID</b>	<b>Name</b>	<b>Phone</b>	<b>Position</b>
E0045	Smith	1234	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234	Lawyer

EmpID → Name, Phone, Position

Position → Phone

but not Phone → Position

# Example

EmpID	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876 ←	Salesrep
E1111	Smith	9876 ←	Salesrep
E9999	Mary	1234	Lawyer

Position → Phone

# Example

EmpID	Name	Phone	Position
E0045	Smith	1234 →	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234 →	Lawyer

But not Phone → Position



# Example

name  $\rightarrow$  color  
category  $\rightarrow$  department  
color, category  $\rightarrow$  price

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Green	Toys	99

Do all the FDs hold on this instance?

# Example

name → color  
category → department  
color, category → price

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Green	Toys	49
Gizmo	Stationary	Green	Office-suppl.	59

What about this one ?

# Buzzwords

- FD **holds** or **does not hold** on an instance
- If we can be sure that *every instance of  $R$*  will be one in which a given FD is true, then we say that  **$R$  satisfies the FD**
- If we say that  $R$  satisfies an FD, we are **stating a constraint on  $R$**

# Why bother with FDs?

Name	<u>SSN</u>	<u>PhoneNumber</u>	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

## Anomalies:

- Redundancy = repeat data
- Update anomalies = what if Fred moves to “Bellevue”?
- Deletion anomalies = what if Joe deletes his phone number?

# An Interesting Observation

If all these FDs are true:

name  $\rightarrow$  color  
category  $\rightarrow$  department  
color, category  $\rightarrow$  price

Then this FD also holds:

name, category  $\rightarrow$  price

If we find out from application domain that a relation satisfies some FDs, it doesn't mean that we found all the FDs that it satisfies!  
There could be more FDs implied by the ones we have.

# Closure of a set of Attributes

**Given** a set of attributes  $A_1, \dots, A_n$

The **closure** is the set of attributes  $B$ , notated  $\{A_1, \dots, A_n\}^+$ ,  
s.t.  $A_1, \dots, A_n \rightarrow B$

Example:

1.  $\text{name} \rightarrow \text{color}$
2.  $\text{category} \rightarrow \text{department}$
3.  $\text{color, category} \rightarrow \text{price}$

Closures:

$\text{name}^+ = \{\text{name, color}\}$

$\{\text{name, category}\}^+ = \{\text{name, category, color, department, price}\}$

$\text{color}^+ = \{\text{color}\}$

# Closure Algorithm

$X = \{A_1, \dots, A_n\}$ .

**Repeat until**  $X$  doesn't change **do:**  
  **if**  $B_1, \dots, B_n \rightarrow C$  is a FD **and**  
     $B_1, \dots, B_n$  are all in  $X$   
  **then** add  $C$  to  $X$ .

Example:

1.  $\text{name} \rightarrow \text{color}$
2.  $\text{category} \rightarrow \text{department}$
3.  $\text{color}, \text{category} \rightarrow \text{price}$

$\{\text{name}, \text{category}\}^+ =$   
   $\{ \text{name}, \text{category}, \text{color}, \text{department}, \text{price} \}$

Hence:  $\text{name}, \text{category} \rightarrow \text{color}, \text{department}, \text{price}$

# Example

## In class:

R(A,B,C,D,E,F)

A, B	→	C
A, D	→	E
B	→	D
A, F	→	B

Compute  $\{A, B\}^+$       $X = \{A, B, \quad \quad \quad \}$

Compute  $\{A, F\}^+$   $X = \{A, F,$



# Example

In class:

$R(A, B, C, D, E, F)$

A, B	→	C
A, D	→	E
B	→	D
A, F	→	B

Compute  $\{A, B\}^+$      $X = \{A, B, C, D, E\}$

Compute  $\{A, F\}^+$      $X = \{A, F,$      $\}$

# Example

In class:

$R(A, B, C, D, E, F)$

A, B	→	C
A, D	→	E
B	→	D
A, F	→	B

Compute  $\{A, B\}^+$      $X = \{A, B, C, D, E\}$

Compute  $\{A, F\}^+$      $X = \{A, F, B, C, D, E\}$

# Example

In class:

$R(A, B, C, D, E, F)$

$A, B \rightarrow C$
$A, D \rightarrow E$
$B \rightarrow D$
$A, F \rightarrow B$

Compute  $\{A, B\}^+$      $X = \{A, B, C, D, E\}$

Compute  $\{A, F\}^+$      $X = \{A, F, B, C, D, E\}$

# Practice at Home

Find all FD's implied by:

$A, B \rightarrow C$
$A, D \rightarrow B$
$B \rightarrow D$

Step 1: Compute  $X^+$ , for every  $X$ :

$A^+ = A, B^+ = BD, C^+ = C, D^+ = D$

$AB^+ = ABCD, AC^+ = AC, AD^+ = ABCD,$

$BC^+ = BCD, BD^+ = BD, CD^+ = CD$

$ABC^+ = ABD^+ = ACD^+ = ABCD$  (no need to compute— why ?)

$BCD^+ = BCD, ABCD^+ = ABCD$

Step 2: Enumerate all FD's  $X \rightarrow Y$ , s.t.  $Y \subseteq X^+$  and  $X \cap Y = \emptyset$  :

$AB \rightarrow CD, AD \rightarrow BC, ABC \rightarrow D, ABD \rightarrow C, ACD \rightarrow B$

# Keys

$R(A_1, \dots, A_n, B)$

- A **superkey** is a set of attributes  $A_1, \dots, A_n$  s.t. for any other attribute  $B$ , we have  $A_1, \dots, A_n \rightarrow B$
- A **key** is a minimal superkey
  - A superkey and for which no subset is a superkey

# Computing (Super)Keys

- For all sets  $X$ , compute  $X^+$
- If  $X^+ = [\text{all attributes}]$ , then  $X$  is a superkey
- Try reducing to the minimal  $X$ 's to get the key

# Example

Product(name, price, category, color)

name, category → price  
category → color

What is the key ?

# Example

Product(name, price, category, color)

name, category  $\rightarrow$  price  
category  $\rightarrow$  color

What is the key ?

$(\text{name, category}) + = \{ \text{name, category, price, color} \}$

Hence (name, category) is a key



# Key or Keys ?

Can we have more than one key ?

Given  $R(A,B,C)$  define FD's s.t. there are two or more distinct keys

# Key or Keys ?

Can we have more than one key ?

Given  $R(A,B,C)$  define FD's s.t. there are two or more distinct keys

$A \rightarrow B$
$B \rightarrow C$
$C \rightarrow A$

or

$AB \rightarrow C$
$BC \rightarrow A$

or

$A \rightarrow BC$
$B \rightarrow AC$

what are the keys here ?

# Eliminating Anomalies

Main idea:

- $X \rightarrow A$  is OK if  $X$  is a (super)key
- $X \rightarrow A$  is not OK otherwise
  - Need to decompose the table, but how?

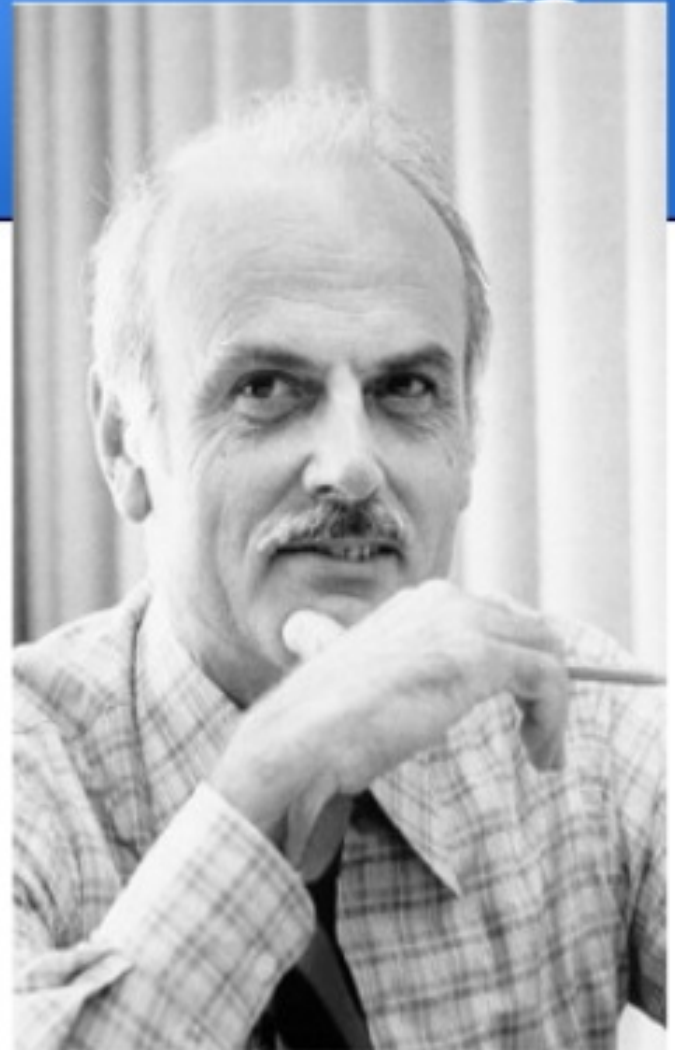
## Boyce-Codd Normal Form

# Boyce-Codd Normal Form

Dr. Raymond F. Boyce

Edgar Frank “Ted” Codd

"A Relational Model of Data for  
Large Shared Data Banks"



# Boyce-Codd Normal Form

There are no  
“bad” FDs:

**Definition.** A relation  $R$  is in BCNF if:

Whenever  $X \rightarrow B$  is a non-trivial dependency,  
then  $X$  is a superkey.

Equivalently:

**Definition.** A relation  $R$  is in BCNF if:

$\forall X$ , either  $X^+ = X$  or  $X^+ = [\text{all attributes}]$

# BCNF Decomposition Algorithm

Normalize(R)

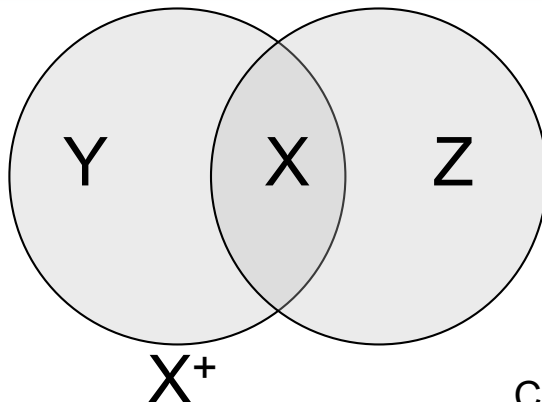
find  $X$  s.t.:  $X \neq X^+$  and  $X^+ \neq [\text{all attributes}]$

**if** (not found) **then** “R is in BCNF”

**let**  $Y = X^+ - X$ ;  $Z = [\text{all attributes}] - X^+$

decompose R into  $R_1(X \cup Y)$  and  $R_2(X \cup Z)$

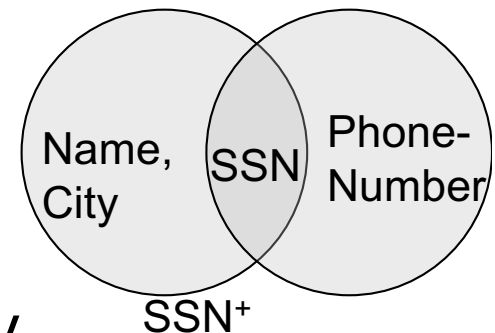
Normalize( $R_1$ ); Normalize( $R_2$ );



# Example

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

$SSN \rightarrow Name, City$



The only key is:  $\{SSN, PhoneNumber\}$

Hence  $SSN \rightarrow Name, City$  is a “bad” dependency

In other words:

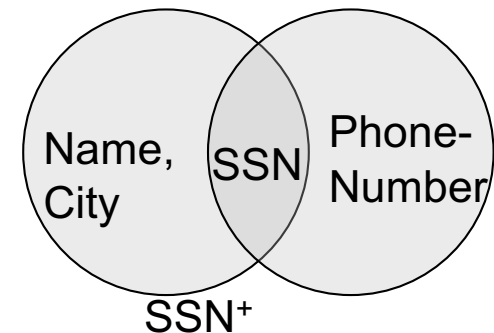
$SSN^+ = SSN, Name, City$  and is neither  $SSN$  nor  $All\ Attributes$



# Example BCNF Decomposition

<b>Name</b>	<b><u>SSN</u></b>	<b>City</b>
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield

$SSN \rightarrow Name, City$



<b><u>SSN</u></b>	<b><u>PhoneNumber</u></b>
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121
987-65-4321	908-555-1234

**Let's check anomalies:**

- Redundancy ?
- Update ?
- Delete ?