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| Introduction to Database Systems |
| CSE 414 |
| Lecture 20: Design Theory |
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## Class Overview

- Unit 1: Intro
- Unit 2: Relational Data Models and Query Languages
- Unit 3: Non-relational data
- Unit 4: RDMBS internals and query optimization
- Unit 5: Parallel query processing
- Unit 6: DBMS usability, conceptual design
- E/R diagrams
- Schema normalization
- Unit 7: Transactions



## Entity / Relationship Diagrams

- Entity set = a class
- An entity = an object

Product

- Attribute
- Relationship



## Arrows in Multiway Relationships

Q: What does the arrow mean?


A: Any person buys a given product from at most one store AND every store sells to every person at most one product CSE 414 - Spring 2018

## N-N Relationships to Relations




## Referential Integrity Constraints



Each product made by at most one company.
Some products made by no company
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## Constraints in SQL

Constraints in SQL:

- Keys, foreign keys
- Attribute-level constraints
- Tuple-level constraints
- Global constraints: assertions

- The more complex the constraint, the harder it is to check and to enforce


## Relational Schema Design

| Name | $\underline{\text { SSN }}$ | PhoneNumber | City |
| :--- | :--- | :--- | :--- |
| Fred | $123-45-6789$ | $206-555-1234$ | Seattle |
| Fred | $123-45-6789$ | $206-555-6543$ | Seattle |
| Joe | $987-65-4321$ | $908-555-2121$ | Westfield |

One person may have multiple phones, but lives in only one city
Primary key is thus (SSN, PhoneNumber)
What is the problem with this schema?

Relation Decomposition
Break the relation into two:

|  | Name | SSN | PhoneNumber | City |
| :---: | :---: | :---: | :---: | :---: |
|  | Fred | 123-45-6789 | 206-555-1234 | Seattle |
|  | Fred | 123-45-6789 | 206-555-6543 | Seattle |
|  | Joe | 987-65-4321 | 908-555-2121 | Westrield |
|  |  |  |  | $\checkmark$ |
| Name | SSN | City | SSN | PhoneNumber |
| Fred | 123-45-6789 | Seattle | 123-45-6789 | 206-555-1234 |
| Joe | 987-65-4321 | Westfield | 123-45-6789 | 206-555-6543 |
| Anomalies have gone: <br> - No more repeated data <br> - Easy to move Fred to "Bellevue" (how ?) <br> - Easy to delete all Joe's phone numbers (how ?) |  |  |  | 908-555-2121 |
|  |  |  |  |  |
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## Relational Schema Design (or Logical Design)

How do we do this systematically?

- Start with some relational schema
- Find out its functional dependencies (FDs)
- Use FDs to normalize the relational schema


## Functional Dependencies (FDs)

Definition $A_{1}, \ldots, A_{m} \rightarrow B_{1}, \ldots, B_{n}$ holds in $R$ if:

$\left(\mathrm{t} . \mathrm{A}_{1}=\mathrm{t}^{\prime} . \mathrm{A}_{1} \wedge . . \wedge \mathrm{n} . \mathrm{A}_{\mathrm{m}}=\mathrm{t}^{\prime} . \mathrm{A}_{\mathrm{m}} \rightarrow \mathrm{t} . \mathrm{B}_{1}=\mathrm{t}^{\prime} . \mathrm{B}_{1} \wedge \ldots \wedge \mathrm{t} . \mathrm{B}_{\mathrm{n}}=\mathrm{t}^{\prime} . \mathrm{B}_{\mathrm{n}}\right)$


## Example

| EmpID | Name | Phone | Position |
| :--- | :--- | :--- | :--- |
| E0045 | Smith | 1234 | Clerk |
| E3542 | Mike | $9876 \quad \leftarrow$ | Salesrep |
| E1111 | Smith | $9876 \leftarrow$ | Salesrep |
| E9999 | Mary | 1234 | Lawyer |

Position $\rightarrow$ Phone

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## Functional Dependencies (FDs)

## Definition

If two tuples agree on the attributes
$A_{1}, A_{2}, \ldots, A_{n}$
then they must also agree on the attributes

Formally
$\mathrm{B}_{1}, \mathrm{~B}_{2}, \ldots, \mathrm{~B}_{\mathrm{m}}$

$$
\mathrm{A}_{1}, \mathrm{~A}_{2}, \ldots, \mathrm{~A}_{\mathrm{n}} \rightarrow \mathrm{~B}_{1}, \mathrm{~B}_{2}, \ldots, \mathrm{~B}_{\mathrm{m}}
$$

## Example

An FD holds, or does not hold on an instance:

| EmpID | Name | Phone | Position |
| :--- | :--- | :--- | :--- |
| E0045 | Smith | 1234 | Clerk |
| E3542 | Mike | 9876 | Salesrep |
| E1111 | Smith | 9876 | Salesrep |
| E9999 | Mary | 1234 | Lawyer |

EmpID $\rightarrow$ Name, Phone, Position
Position $\rightarrow$ Phone
but not Phone $\rightarrow$ Position

## Example

| EmpID | Name | Phone | Position |
| :--- | :--- | :--- | :--- |
| E0045 | Smith | $1234 \rightarrow$ | Clerk |
| E3542 | Mike | 9876 | Salesrep |
| E1111 | Smith | 9876 | Salesrep |
| E9999 | Mary | $1234 \rightarrow$ | Lawyer |

But not Phone $\rightarrow$ Position


## Buzzwords

- FD holds or does not hold on an instance
- If we can be sure that every instance of $R$ will be one in which a given FD is true, then we say that $R$ satisfies the FD
- If we say that $R$ satisfies an FD, we are stating a constraint on $R$


## An Interesting Observation

| $\qquad$If all these FDs are true: name $\rightarrow$ color <br> category $\rightarrow$ department <br> color, category $\rightarrow$ price <br> Then this FD also holds: name, category $\rightarrow$ price |
| :--- |
| If we find out from application domain that a relation satisfies some FDs, <br> it doesn't mean that we found all the FDs that it satisfies! <br> There could be more FDs implied by the ones we have. |


| Example $\begin{aligned} & \text { name } \rightarrow \text { color } \\ & \text { category } \rightarrow \text { department } \\ & \text { color, category } \rightarrow \text { price }\end{aligned}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| name | category | color | department | price |
| Gizmo | Gadget | Green | Toys | 49 |
| Tweaker | Gadget | Green | Toys | 49 |
| Gizmo | Stationary | Green | Office-supp. | 59 |
| What about this one ? |  | CSE 414 - Sping 2018 |  | 26 |

## Why bother with FDs?

| Name | $\underline{\text { SSN }}$ | PhoneNumber | City |
| :--- | :--- | :--- | :--- |
| Fred | $123-45-6789$ | $206-555-1234$ | Seattle |
| Fred | $123-45-6789$ | $206-555-6543$ | Seattle |
| Joe | $987-65-4321$ | $908-555-2121$ | Westfield |

Anomalies:

- Redundancy
= repeat data
- Update anomalies = what if Fred moves to "Bellevue"?
- Deletion anomalies = what if Joe deletes his phone number?


## Closure of a set of Attributes

Given a set of attributes $\mathrm{A}_{1}, \ldots, \mathrm{~A}_{\mathrm{n}}$
The closure is the set of attributes B , notated $\left.\left\{\mathrm{A}_{1}, \ldots, \mathrm{~A}_{n}\right\}^{+}\right)$, s.t. $A_{1}, \ldots, A_{n} \rightarrow B$

Example

1. name $\rightarrow$ color
2. category $\rightarrow$ department
3. color, category $\rightarrow$ price

Closures:
3. color, category $\rightarrow$ price
name $^{+}=\{$name, color $\}$
\{name, category\} ${ }^{+}=$\{name, category, color, department, price\} color $^{+}=\{$color $\}$


## Example

In class:
$R(A, B, C, D, E, F)$

$$
\begin{array}{|lll|}
\hline \mathrm{A}, \mathrm{~B} & \rightarrow & \mathrm{C} \\
\mathrm{~A}, \mathrm{D} & \rightarrow & \mathrm{E} \\
\mathrm{~B} & & \rightarrow \\
\mathrm{D} \\
\mathrm{~A}, \mathrm{~F} & \rightarrow & \mathrm{~B} \\
\hline
\end{array}
$$

Compute $\{A, B\}^{+} \quad X=\{A, B, C, D, E\}$
Compute $\{A, F\}^{+} \quad X=\{A, F, B, C, D, E\}$
What is the key of $R$ ?


## Example

In class:
$R(A, B, C, D, E, F)$

$$
\begin{array}{|lll|}
\hline \mathrm{A}, \mathrm{~B} & \rightarrow & \mathrm{C} \\
\mathrm{~A}, \mathrm{D} & \rightarrow & \mathrm{E} \\
\mathrm{~B} & \rightarrow & \mathrm{D} \\
\mathrm{~A}, \mathrm{~F} & \rightarrow & \mathrm{~B} \\
\hline
\end{array}
$$

Compute $\{A, B\}^{+} \quad X=\{A, B, \quad\}$
Compute $\{A, F\}^{+} \quad X=\{A, F, \quad\}$

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## Example

In class:
$R(A, B, C, D, E, F)$

$$
\begin{array}{|lll|}
\hline \mathrm{A}, \mathrm{~B} & \rightarrow & \mathrm{C} \\
\mathrm{~A}, \mathrm{D} & \rightarrow & \mathrm{E} \\
\mathrm{~B} & & \rightarrow \\
\mathrm{D} \\
\mathrm{~A}, \mathrm{~F} & \rightarrow & \mathrm{~B} \\
\hline
\end{array}
$$

Compute $\{A, B\}^{+} \quad X=\{A, B, C, D, E\}$
Compute $\{\mathrm{A}, \mathrm{F}\}^{+} \quad \mathrm{X}=\{\mathrm{A}, \mathrm{F}, \mathrm{B}, \mathrm{C}, \mathrm{D}, \mathrm{E}\}$

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## Practice at Home

Find all FD's implied by:

$$
\begin{array}{|lll|}
\hline \mathrm{A}, \mathrm{~B} & \rightarrow & \mathrm{C} \\
\mathrm{~A}, \mathrm{D} & \rightarrow & \mathrm{~B} \\
\mathrm{~B} & \rightarrow & \mathrm{D} \\
\hline
\end{array}
$$

Step 1: Compute $\mathrm{X}^{+}$, for every X :
$\mathrm{A}^{+}=\mathrm{A}, \quad \mathrm{B}^{+}=\mathrm{BD}, \quad \mathrm{C}^{+}=\mathrm{C}, \quad \mathrm{D}^{+}=\mathrm{D}$
$A B^{+}=A B C D, A C^{+}=A C, A D^{+}=A B C D$,
$\mathrm{BC}^{+}=\mathrm{BCD}, \mathrm{BD}^{+}=\mathrm{BD}, \mathrm{CD}^{+}=\mathrm{CD}$
$\mathrm{ABC}^{+}=\mathrm{ABD}^{+}=\mathrm{ACD}^{+}=\mathrm{ABCD}$ (no need to compute- why ?)
$\mathrm{BCD}^{+}=\mathrm{BCD}, \quad \mathrm{ABCD}^{+}=\mathrm{ABCD}$
Step 2: Enumerate all FD's $X \rightarrow Y$, s.t. $Y \subseteq X^{+}$and $X \cap Y=\emptyset$ :
$\mathrm{AB} \rightarrow \mathrm{CD}, \mathrm{AD} \rightarrow \mathrm{BC}, \mathrm{ABC} \rightarrow \mathrm{D}, \mathrm{ABD} \rightarrow \mathrm{C}, \mathrm{ACD} \rightarrow \mathrm{B} \quad{ }^{36}$

$$
\text { Keys } \quad R\left(A, \ldots A_{n}, B\right)
$$

- A superkey is a set of attributes $A_{1}, \ldots, A_{n}$ s.t. for any other attribute $B$, we have $A_{1}, \ldots, A_{n} \rightarrow B$
- A key is a minimal superkey
- A superkey and for which no subset is a superkey


## Example

Product(name, price, category, color)
name, category $\rightarrow$ price category $\rightarrow$ color

What is the key?

## Key or Keys ?

Can we have more than one key ?

Given $R(A, B, C)$ define FD's s.t. there are two or more distinct keys

Computing (Super)Keys

- For all sets X , compute $\mathrm{X}^{+}$
- If $\mathrm{X}^{+}=$[all attributes], then X is a superkey
- Try reducing to the minimal X's to get the key


## Example

Product(name, price, category, color)
name, category $\rightarrow$ price
category $\rightarrow$ color

What is the key?
(name, category) $+=$ \{ name, category, price, color $\}$
Hence (name, category) is a key

## Key or Keys ?

Can we have more than one key ?

Given $R(A, B, C)$ define FD's s.t. there are two or more distinct keys


## Eliminating Anomalies

## Main idea:

- $X \rightarrow A$ is OK if $X$ is a (super)key
- $X \rightarrow A$ is not OK otherwise
- Need to decompose the table, but how?


## Boyce-Codd Normal Form

There are no
"bad" FDs:

Equivalently:
Definition. A relation R is in BCNF if: $\forall \mathrm{X}$, either $\mathrm{X}^{+}=\mathrm{X}$ or $\mathrm{X}^{+}=$[all attributes $]$

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## Example

| Name | SSN | PhoneNumber | City |
| :--- | :--- | :--- | :--- |
| Fred | $123-45-6789$ | $206-555-1234$ | Seattle |
| Fred | $123-45-6789$ | $206-555-6543$ | Seattle |
| Joe | $987-65-4321$ | $908-555-2121$ | Westfield |
| Joe | $987-65-4321$ | $908-555-1234$ | Westfield |



The only key is: \{SSN, PhoneNumber\}
Hence SSN $\rightarrow$ Name, City is a "bad" dependency
In other words:
SSN+ = SSN, Name, City and is neither SSN nor All Attributes


