## Database Systems CSE 414

## Lectures 11 - 12 : <br> Basics of Query Optimization and Cost Estimation

(Ch. 15.\{1,3,4.6,6\} \& 16.4-5)

## Announcements

- HW3 is due Tuesday
- WQ4 is due Thursday
- Midterm on Friday
- we'll talk more about it on Monday
- Husky Football spring game tomorrow


## Motivation

- To understand performance, need to understand a bit about how a DBMS works
- my database application is too slow... why?
- one of the queries is very slow... why?
- Under your direct control: index choice
- understand how that affects query performance


## Recap: Query Evaluation



## Query Optimizer Overview

- Input: Parsed \& checked SQL
- Output: A good physical query plan
- Basic query optimization algorithm:
- Enumerate alternative plans (logical and physical)
- Compute estimated cost of each plan
- Compute number of I/Os
- Optionally take into account other resources
- Choose plan with lowest cost
- This is called cost-based optimization


## Query Optimizer Overview

- There are exponentially many query plans
- exponential in the size of the query
- simple SFW with 3 joins has not too many
- Optimizer will consider many, many of them
- Worth substantial cost to avoid bad plans


## Rest of Today

- Cost of reading from disk
- Cost of single RA operators
- Cost of query plans


# Cost of Reading Data From Disk 

## Cost Parameters

- Cost = Disk I/O + CPU + Network I/O
- We will focus on Disk I/O
- Parameters:
$-B(R)=\#$ of blocks (i.e., pages) for relation $R$
$-T(R)=\#$ of tuples in relation $R$
$-\mathbf{V}(\mathbf{R}, \mathrm{A})=$ \# of distinct values of attribute a
- When $\mathbf{A}$ is a key, $V(R, A)=T(R)$
- When $\mathbf{A}$ is not a key, $\mathbf{V}(\mathbf{R}, \mathrm{A})$ can be anything $<T(R)$
- Where do these values come from?
- DBMS collects statistics about data on disk


## Selectivity Factors for Conditions

- $A=c \quad / * \sigma_{A=c}(R) * /$
- Selectivity $=1 / V(R, A)$
- $\mathrm{A}<\mathrm{C} \quad / * \sigma_{\mathrm{A}<\mathrm{c}}(\mathrm{R})^{*} /$
- Selectivity $=(c-\operatorname{Low}(R, A)) /(\operatorname{High}(R, A)-\operatorname{Low}(R, A))$
- $\mathrm{c} 1<\mathrm{A}<\mathrm{c} 2 \quad /{ }^{*} \sigma_{\mathrm{c} 1<\mathrm{A}<\mathrm{c} 2}(\mathrm{R})^{*} /$
- Selectivity $=(c 2-c 1) /(H i g h(R, A)-\operatorname{Low}(R, A))$


## Example: Selectivity of $\sigma_{A=c}(R)$

$$
\begin{aligned}
& T(R)=100,000 \\
& V(R, A)=20
\end{aligned}
$$

How many records are returned by $\sigma_{A=c}(R)=$ ?

Answer: $X$ * $T(R)$, where $X=$ selectivity...
$\ldots X=1 / V(R, A)=1 / 20$
Number of records returned $=100,000 / 20=5,000$

## Cost of Index-based Selection

- Sequential scan for relation $R$ costs $B(R)$
- Index-based selection
- Estimate selectivity factor $\mathbf{X}$ (see previous slide)
- Clustered index: $X^{*} B(R)$
- Unclustered index $X^{*} T(R)$

Note: we are ignoring I/O cost for index pages

## Example: Cost of $\sigma_{A=c}(R)$

- Example: | $B(R)=2000$ |
| :--- | :--- |
| $T(R)=100,000 \quad$ cost of $\sigma_{A=c}(R)=?$ |
- Table scan: $B(R)=2,000$ I/Os
- Index based selection:
- If index is clustered: $\quad B(R) / V(R, A)=1001 / O s$
- If index is unclustered: $\quad T(R) / V(R, A)=5,000 \mathrm{I} / \mathrm{Os}$

Lesson: Don't build unclustered indexes when $V(R, A)$ is small !

## Cost of Executing Operators (Focus on Joins)

## Outline

- Join operator algorithms
- One-pass algorithms (Sec. 15.2 and 15.3)
- Index-based algorithms (Sec 15.6)
- Note about readings:
- In class, we discuss only algorithms for joins
- Other operators are easier: read the book


## Join Algorithms

- Hash join
- Nested loop join
- Sort-merge join


## Hash Join

Hash join: $R \bowtie S$

- Scan R, build buckets in main memory
- Then scan $S$ and join
- Cost: $B(R)+B(S)$
- One-pass algorithm when $B(R) \leq M$
- more disk access also when $B(R)>M$


## Hash Join Example

Patient(pid, name, address)
Insurance(pid, provider, policy_nb)
Patient $\bowtie$ Insurance

Two tuples per page

Patient

| 1 | 'Bob' | 'Seattle' |
| :--- | :--- | :--- |
| 2 | 'Ela' | 'Everett' |


| 3 | 'Jill' | 'Kent' |
| :--- | :--- | :--- |
| 4 | 'Joe' | 'Seattle' |

Insurance

| 2 | 'Blue' | 123 |
| :--- | :--- | :--- |
| 4 | 'Prem' | 432 |


| 4 | 'Prem' | 343 |
| :---: | :---: | :---: |
| 3 | 'GrpH' | 554 |

## Hash Join Example

Patient $\bowtie$ Insurance

## Large enough

Memory $\mathrm{M}=21$ pages


## Hash Join Example

Step 1: Scan Patient and build hash table in memory
Memory M = 21 pages
Hash h: pid \% 5


## Hash Join Example

Step 2: Scan Insurance and probe into hash table
Memory M = 21 pages

| Hash h: pid $\% 5$ |
| :--- |
| 5  1 6 2  3 8 |

Disk
Patient Insurance


| 2 | 4 |
| :--- | :--- |

Input buffer

Write to disk

## Hash Join Example

Step 2: Scan Insurance and probe into hash table
Memory M = 21 pages

| Hash h: pid $\% 5$ |
| :--- |
|           <br> 5  1 6 2  3 8 4 9 |

Disk
Patient Insurance

| 2 | 2 | 4 | 6 | 6 |
| :---: | :---: | :---: | :---: | :---: |
| 34 | 4 | 3 | 1 | 3 |
| 6 | 2 | 8 |  |  |
| 5 | 8 | 9 |  |  |

## Hash Join Example

Step 2: Scan Insurance and probe into hash table
Memory M = 21 pages
Hash h: pid \% 5

| 5 |  | 1 | 6 | 2 |  | 3 | 8 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Disk
Patient Insurance

| 1 | 2 |
| :--- | :--- |
| 3 | 4 |
| 9 | 6 |
| 8 | 5 |


| 2 | 4 |
| :--- | :--- |
| 4 | 3 |
| 2 | 8 |
| 8 | 9 |



| 4 | 3 |
| :--- | :--- |

Input buffer
Keep going until read all of Insurance

Cost: $B(R)+B(S)$

## Nested Loop Joins

- Tuple-based nested loop $R \bowtie S$
- $R$ is the outer relation, $S$ is the inner relation

```
for each tuple t in R do
    for each tuple t in in do
        if }\mp@subsup{t}{1}{}\mathrm{ and t join then output ( }\mp@subsup{t}{1}{},\mp@subsup{t}{2}{}
```

- Cost: $B(R)+T(R) B(S)$

What is the Cost?

- Multiple-pass since $S$ is read many times


## Block-at-a-time Refinement

for each block of tuples $r$ in $R$ do
for each block of tuples $s$ in $S$ do
for all pairs of tuples $t_{1}$ in $r, t_{2}$ in $s$
if $t_{1}$ and $t_{2}$ join then output $\left(t_{1}, t_{2}\right)$

- Cost: $B(R)+B(R) B(S)$

What is the Cost?

## Block-at-a-time Refinement



## Block-at-a-time Refinement



## Page-at-a-time Refinement



## Block-at-a-time Refinement



## Block-Nested-Loop Refinement

for each group of $\mathrm{M}-1$ pages r in R do
for each page of tuples $s$ in $S$ do for all pairs of tuples $t_{1}$ in $r, t_{2}$ in $s$ if $t_{1}$ and $t_{2}$ join then output $\left(t_{1}, t_{2}\right)$

- Cost: $B(R)+B(R) B(S) /(M-1)$ What is the Cost?


## Sort-Merge Join

Sort-merge join: $R \bowtie S$

- Scan R and sort in main memory
- Scan S and sort in main memory
- Merge R and S
- Cost: $B(R)+B(S)$
- One pass algorithm when $B(S)+B(R)<=M$
- Typically, this is NOT a one pass algorithm


## Sort-Merge Join Example

Step 1: Scan Patient and sort in memory
Memory $\mathrm{M}=21$ pages

| 1 | 2 | 3 | 4 | 5 | 6 | 8 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Disk
Patient Insurance

| 2 | 2 | 4 | 6 | 6 |
| :---: | :---: | :---: | :---: | :---: |
| 4 | 4 | 3 | 1 | 3 |
| 96 | 2 | 8 |  |  |
| 8 | 8 | 9 |  |  |

## Sort-Merge Join Example

Step 2: Scan Insurance and sort in memory
Memory M = 21 pages

| 1 | 2 | 3 | 4 | 5 | 6 | 8 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| 1 | 2 | 2 | 3 | 3 | 4 | 4 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 6 | 8 | 8 | 9 |  |  |  |  |

## Sort-Merge Join Example

Step 3: Merge Patient and Insurance
Memory $M=21$ pages


## Sort-Merge Join Example

Step 3: Merge Patient and Insurance
Memory $M=21$ pages


## Sort-Merge Join Examr

 Step 3: Merge Patient and Insurance Using PK,so only one can match
Memory M = 21 page.


## Sort-Merge Join Example

Step 3: Merge Patient and Insurance
Memory $M=21$ pages


## Sort-Merge Join Example

Step 3: Merge Patient and Insurance
Memory $M=21$ pages


## Index Nested Loop Join

$R \bowtie S$

- Assume $S$ has an index on the join attribute
- Iterate over R, for each tuple fetch corresponding tuple(s) from S
- Cost:
- If index on $S$ is clustered: $B(R)+T(R) B(S) / V(S, A)$
- If index on $S$ is unclustered: $B(R)+T(R) T(S) / V(S, A)$


## Cost of Query Plans

## Physical Query Plan 1

(On the fly)

$$
\begin{array}{ll}
\pi \text { sname } & \text { Selection and project on-the-fly } \\
& ->\text { No additional cost. }
\end{array}
$$

(On the fly)


Total cost of plan is thus cost of join:
= B (Supplier)+B(Supplier)*B(Supply)
(Nested loop)

Supplier
(File scan)

$=100+100$ * 100
$=10,100 \mathrm{I} / \mathrm{s}$
(File scan)

## Physical Query Plan 2

(On the fly)


Total cost
$=100+100$ * $1 / 20$ * $1 / 10$ (a) $+100+100$ * $1 / 2500$ (b) +2 (c)
(Sort-merge join)

+0 (d)
Total cost $\approx 204$ I/Os
(Scan write to T1)
(a) $\sigma_{\text {scity }}=$ 'Seattle' $\wedge$ sstate $=$ 'WA'

Supplier
(File scan)


Supply
(File scan)

## Physical Query Plan 3

(On the fly) (d) $\pi_{\text {sname }}$
(On the fly)
(c) $\sigma_{\text {scity='Seattle' } \wedge s s t a t e=' W A ' ~}^{\text {' }}$

Total cost
$=1$ (a)
+4 (b)
+0 (c)
+0 (d)
Total cost $\approx 5 \mathrm{I} / \mathrm{Os}$
(b) $\underset{\text { sno sno }}{\text { (Index nested loop) }}$
(Use hash index) 4 tuples
(a) $\sigma_{\mathrm{pno}=2}$

Supply
(Index on pno )
Assume: clustered

Supplier
(Index on sno)
Clustering does not matter

