

Database Systems

CSE 414

Lectures 14: Relational Algebra
(part 2) and Query Evaluation
(Ch. 5.2 & 16.3 (skim 16.3.2))

Join Summary

- **Theta-join:** $R \bowtie_{\theta} S = \sigma_{\theta}(R \times S)$
 - Join of R and S with a join condition θ
 - Cross-product followed by selection θ
- **Equijoin:** $R \bowtie_{\theta} S = \sigma_{\theta}(R \times S)$
 - Join condition θ consists only of equalities
- **Natural join:** $R \bowtie S = \pi_A(\sigma_{\theta}(R \times S))$
 - Equijoin
 - Equality on **all** fields with same name in R and in S
 - Projection π_A drops all redundant attributes

So Which Join Is It ?

When we write $R \bowtie S$ we usually mean an equijoin, but we often omit the equality predicate when it is clear from the context

More Joins

- **Outer join**
 - Include tuples with no matches in the output
 - Use NULL values for missing attributes
 - Does not eliminate duplicate columns
- Variants
 - Left outer join
 - Right outer join
 - Full outer join

Outer Join Example

AnonPatient P

age	zip	disease
54	98125	heart
20	98120	flu
33	98120	lung

AnonJob J

job	age	zip
lawyer	54	98125
cashier	20	98120

P ⋈ J

P.age	P.zip	disease	job	J.age	J.zip
54	98125	heart	lawyer	54	98125
20	98120	flu	cashier	20	98120
33	98120	lung	null	null	null

More Examples

Supplier(sno, sname, scity, sstate)

Part(pno, pname, psize, pcolor)

Supply(sno, pno, qty, price)

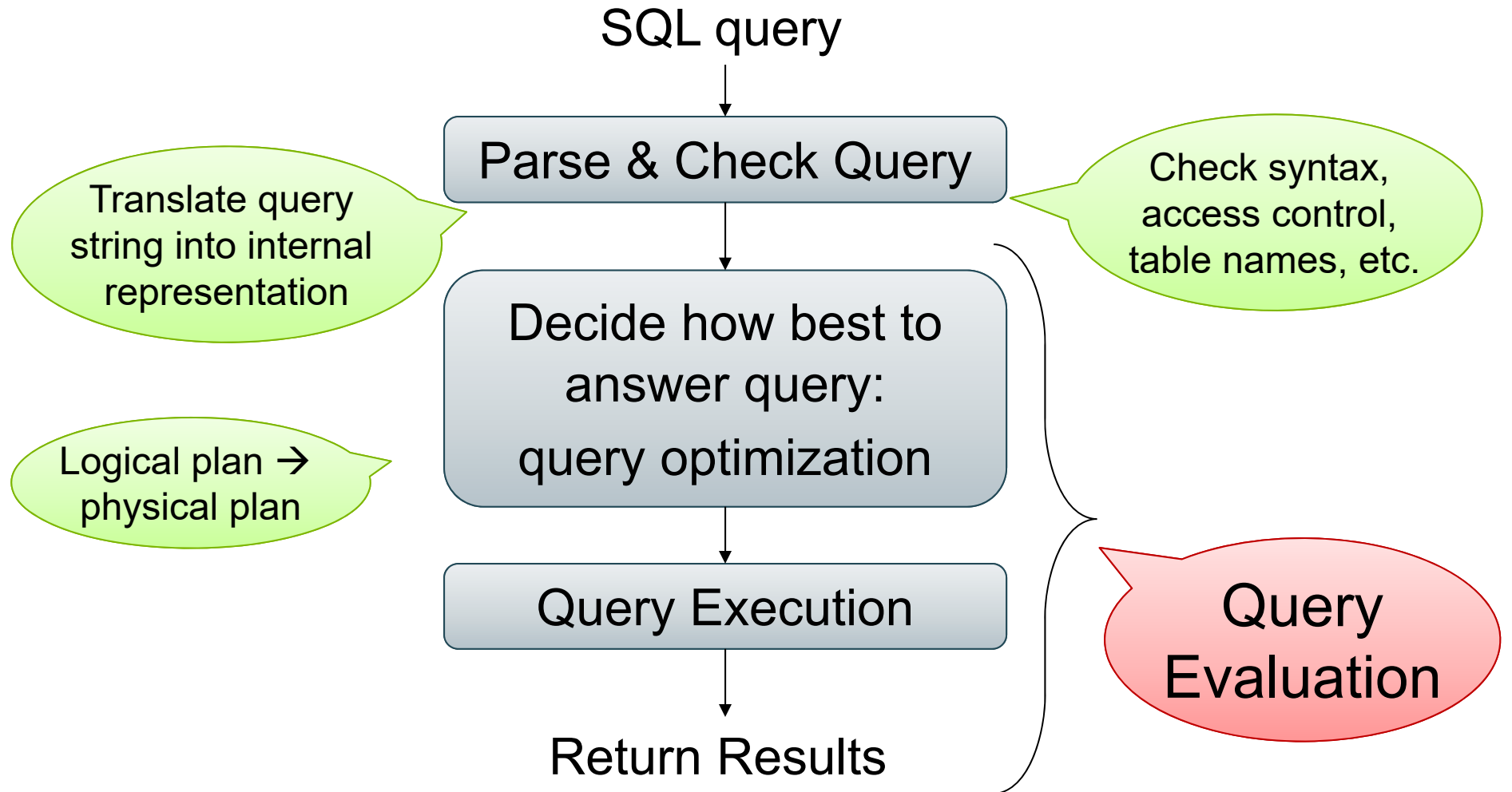
Name of supplier of parts with size greater than 10

$\pi_{\text{sname}}(\text{Supplier} \bowtie \text{Supply} \bowtie (\sigma_{\text{psize} > 10}(\text{Part})))$

Name of supplier of red parts or parts with size greater than 10

$\pi_{\text{sname}}(\text{Supplier} \bowtie \text{Supply} \bowtie (\sigma_{\text{psize} > 10}(\text{Part}) \cup \sigma_{\text{pcolor} = \text{'red'}}(\text{Part})))$

Query Evaluation Steps



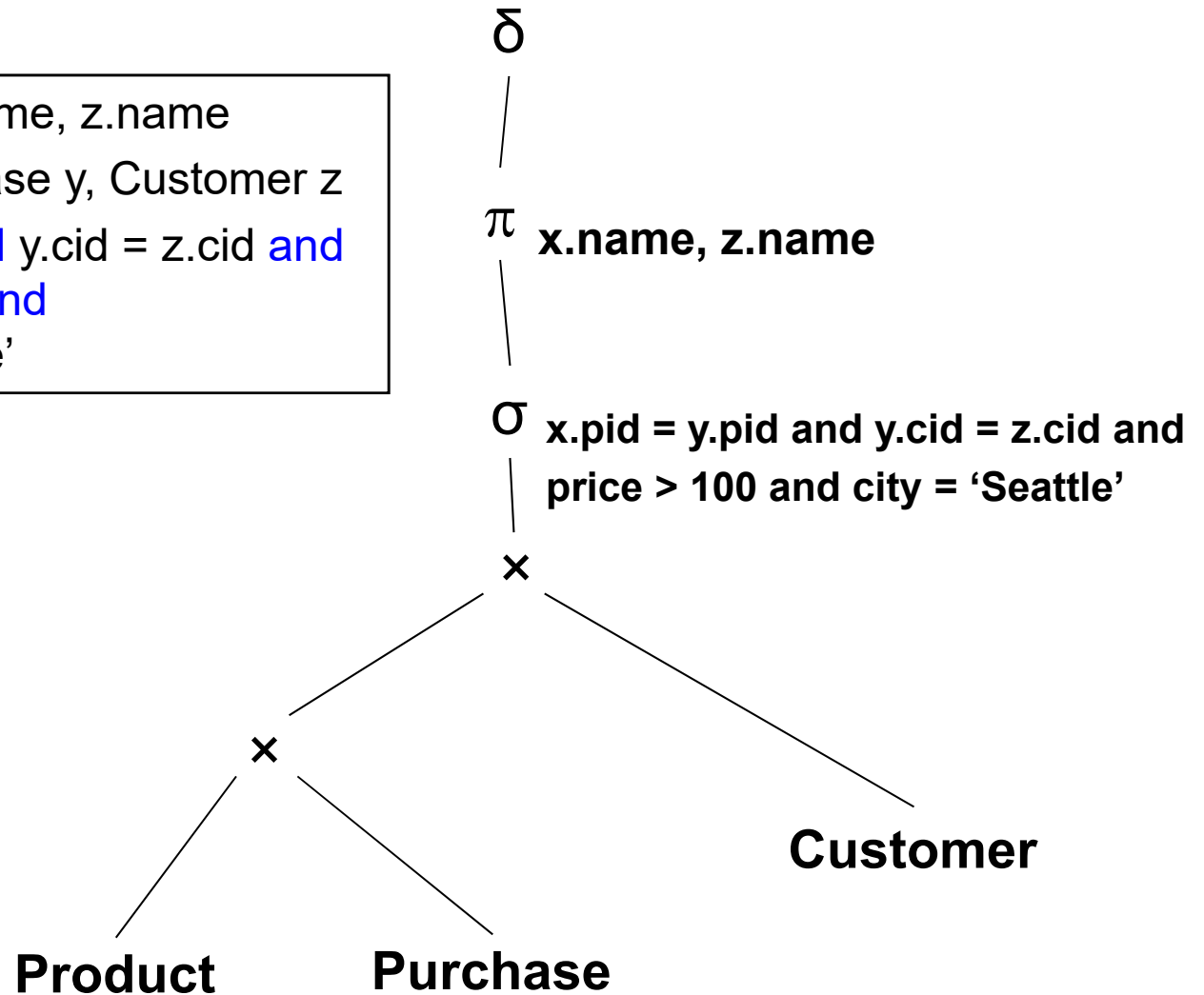
Product(pid, name, price)

Purchase(pid, cid, store)

Customer(cid, name, city)

From SQL to RA

```
SELECT DISTINCT x.name, z.name
FROM Product x, Purchase y, Customer z
WHERE x.pid = y.pid and y.cid = z.cid and
      x.price > 100 and
      z.city = 'Seattle'
```



Product(pid, name, price)

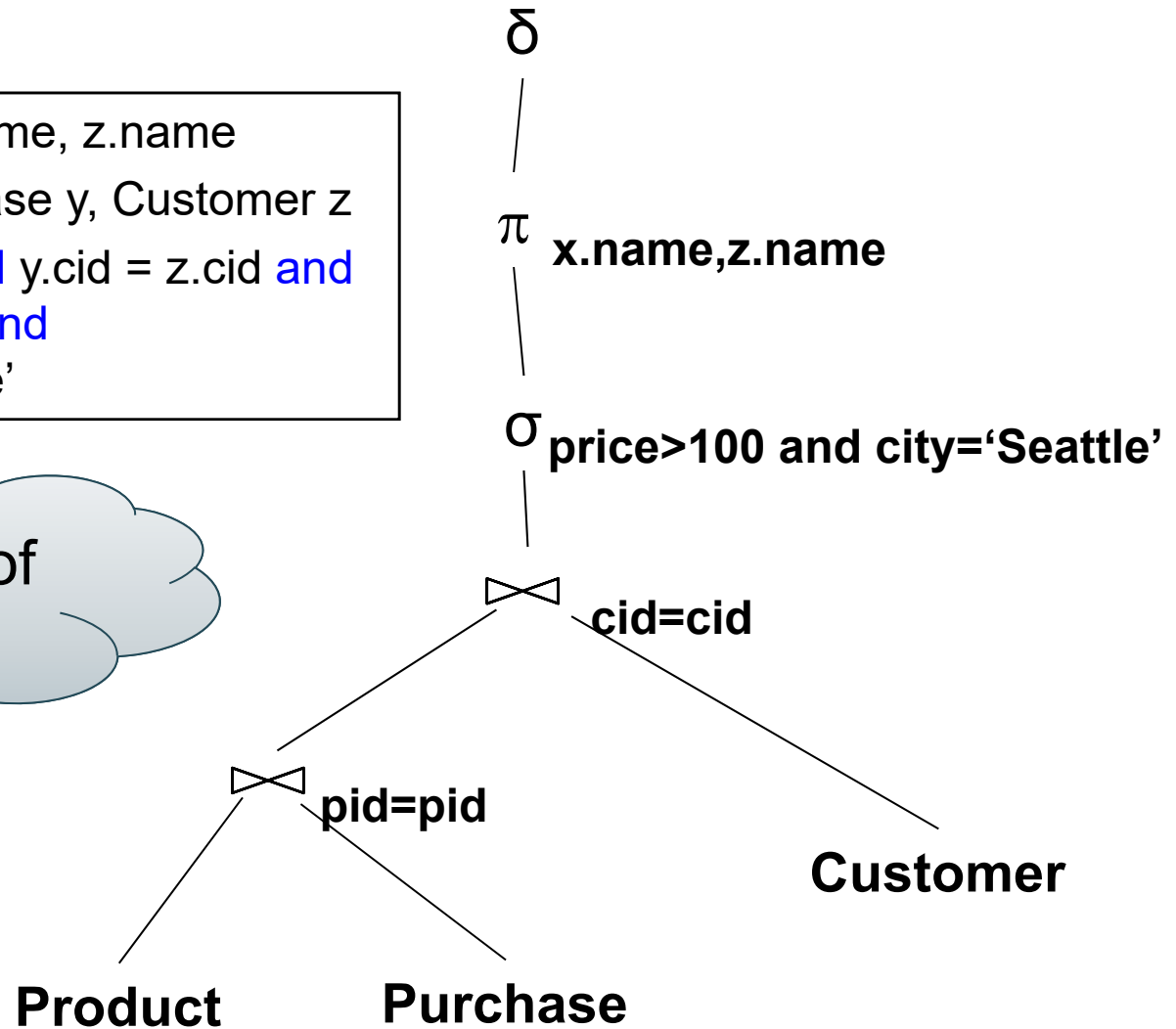
Purchase(pid, cid, store)

Customer(cid, name, city)

From SQL to RA

```
SELECT DISTINCT x.name, z.name  
FROM Product x, Purchase y, Customer z  
WHERE x.pid = y.pid and y.cid = z.cid and  
      x.price > 100 and  
      z.city = 'Seattle'
```

Can you think of another plan?



Product(pid, name, price)
 Purchase(pid, cid, store)
 Customer(cid, name, city)

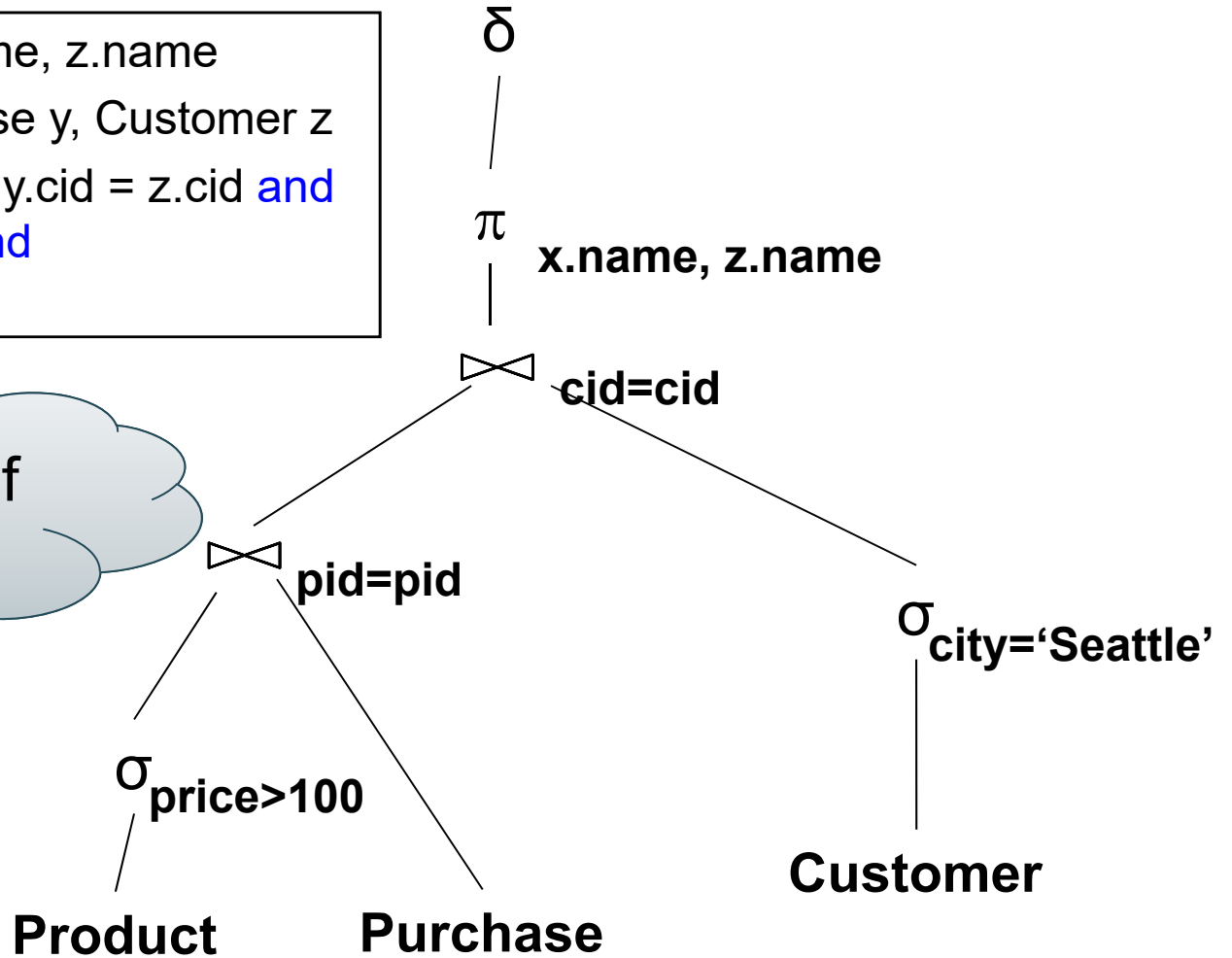
From SQL to RA

```
SELECT DISTINCT x.name, z.name
FROM Product x, Purchase y, Customer z
WHERE x.pid = y.pid and y.cid = z.cid and
      x.price > 100 and
      z.city = 'Seattle'
```

Can you think of another plan?

Push selections down the query plan!

Query optimization: find an equivalent optimal plan



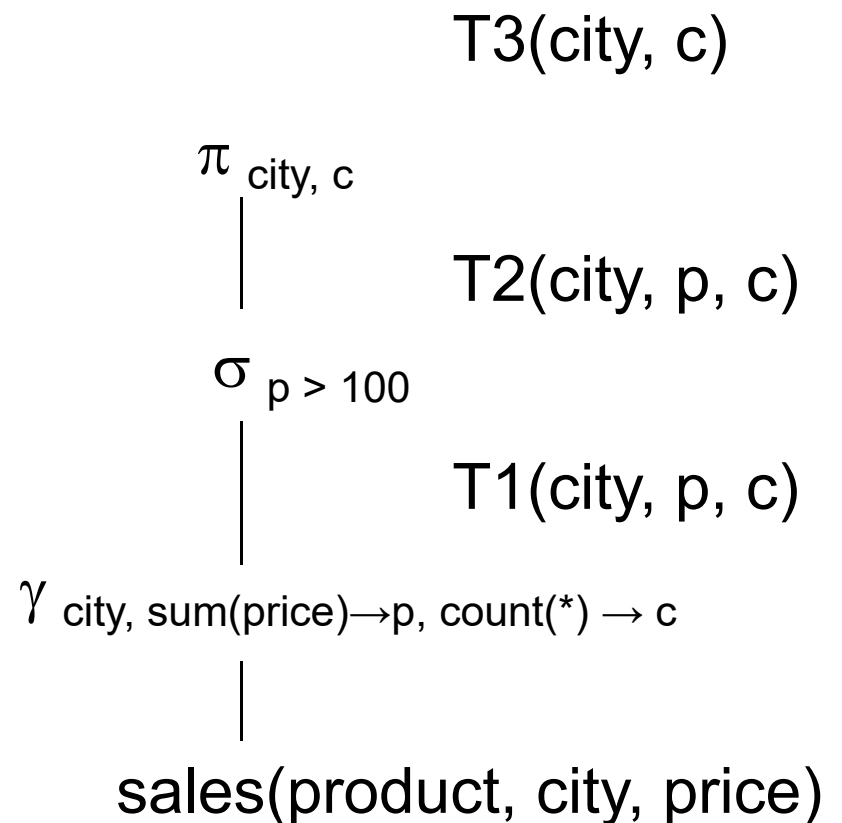
Extended RA: Operators on Bags

- Duplicate elimination δ
- Grouping & aggregation γ
- Sorting τ

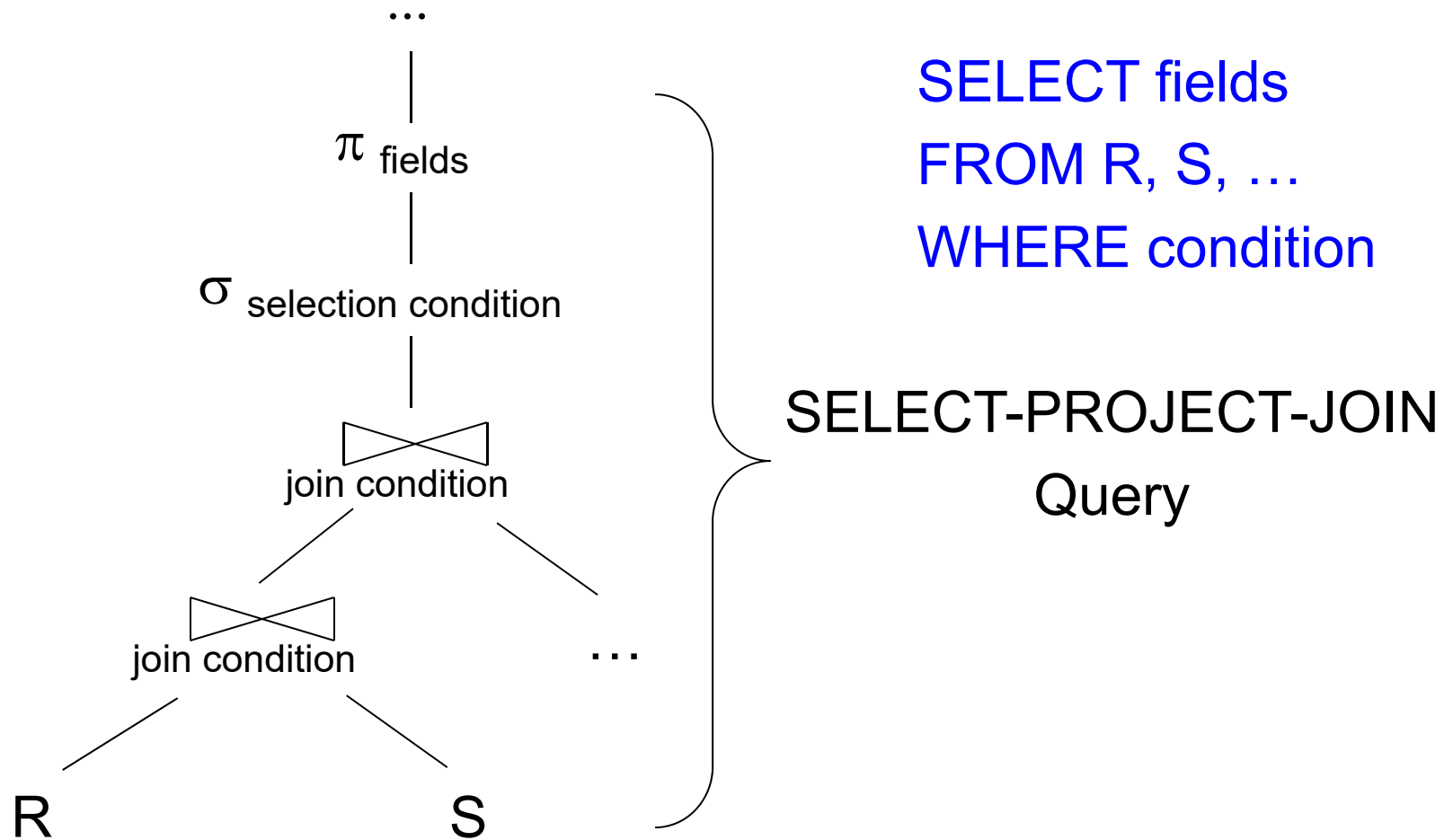
Logical Query Plan

```
SELECT city, count(*)  
FROM sales  
GROUP BY city  
HAVING sum(price) > 100
```

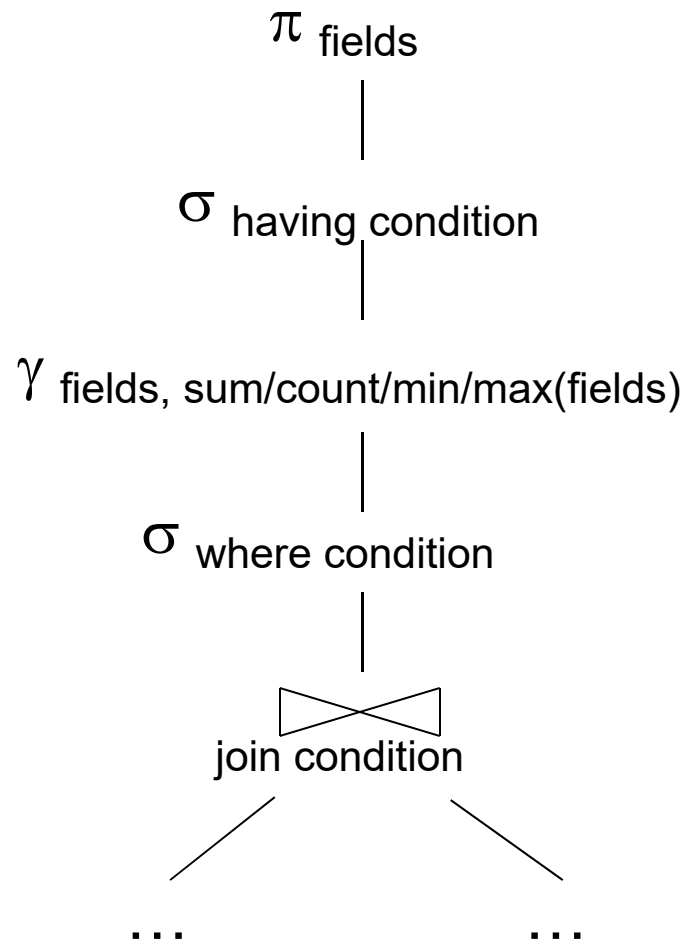
T1, T2, T3 = temporary tables



Typical Plan for Block (1/2)



Typical Plan for Block (2/2)



SELECT fields
FROM R, S, ...
WHERE condition
GROUP BY fields
HAVING condition

Supplier(sno, sname, scity, sstate)

Part(pno, pname, psize, pcolor)

Supply(sno, pno, price)

How about Subqueries?

```
SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA'
and not exists
  (SELECT *
   FROM Supply P
   WHERE P.sno = Q.sno
   and P.price > 100)
```

Correlation !



Supplier(sno, sname, scity, sstate)

Part(pno, pname, psize, pcolor)

Supply(sno, pno, price)

How about Subqueries?

```
SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA'
and not exists
  (SELECT *
   FROM Supply P
   WHERE P.sno = Q.sno
        and P.price > 100)
```

De-Correlation

```
SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA'
and Q.sno not in
  (SELECT P.sno
   FROM Supply P
   WHERE P.price > 100)
```


Supplier(sno, sname, scity, sstate)

Part(pno, pname, psize, pcolor)

Supply(sno, pno, price)

How about Subqueries?

Un-nesting

```
(SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA')
EXCEPT
(SELECT P.sno
FROM Supply P
WHERE P.price > 100)
```

EXCEPT = set difference

```
SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA'
and Q.sno not in
(SELECT P.sno
FROM Supply P
WHERE P.price > 100)
```

Supplier(sno, sname, scity, sstate)

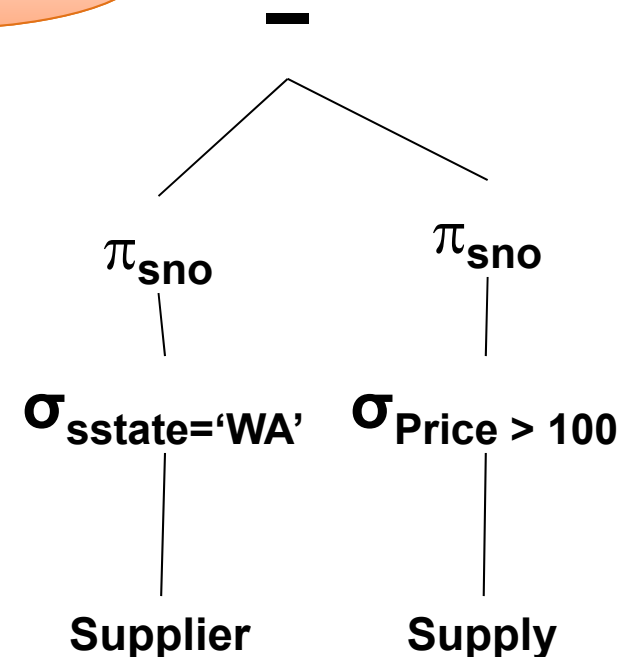
Part(pno, pname, psize, pcolor)

Supply(sno, pno, price)

How about Subqueries?

```
(SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA')
EXCEPT
(SELECT P.sno
FROM Supply P
WHERE P.price > 100)
```

Finally...



From Logical Plans to Physical Plans

Physical Operators

Each of the logical operators may have one or more implementations = physical operators

Will discuss several basic physical operators, with a focus on join

Product(pid, name, price)
Purchase(pid, cid, store)

Main Memory Algorithms

Logical operator:

Product(pid, name, price) ⋈_{pid=pid} Purchase(pid, cid, store)

Propose three physical operators for the join, assuming the tables are in main memory:

1. Nested Loop Join $O(??)$
2. Merge join $O(??)$
3. Hash join $O(??)$

(note that pid is a key)

Product(pid, name, price)
Purchase(pid, cid, store)

Main Memory Algorithms

Logical operator:

Product(pid, name, price) ⋈_{pid=pid} Purchase(pid, cid, store)

Propose three physical operators for the join, assuming the tables are in main memory:

1. Nested Loop Join

$O(n^2)$

two nested loops

2. Merge join

$O(??)$

3. Hash join

$O(??)$

Product(pid, name, price)
Purchase(pid, cid, store)

Main Memory Algorithms

Logical operator:

Product(pid, name, price) ⋈_{pid=pid} Purchase(pid, cid, store)

Propose three physical operators for the join, assuming the tables are in main memory:

1. Nested Loop Join $O(n^2)$
2. Merge join $O(n \log n)$
3. Hash join $O(??)$

sort both – $O(n \log n)$
merge – $O(n)$

Product(pid, name, price)
Purchase(pid, cid, store)

Main Memory Algorithms

Logical operator:

Product(pid, name, price) ⋈_{pid=pid} Purchase(pid, cid, store)

Propose three physical operators for the join, assuming the tables are in main memory:

1. Nested Loop Join $O(n^2)$
2. Merge join $O(n \log n)$
3. Hash join $O(n) \dots O(n^2)$

add n to hash – $O(n)$?
lookup n in hash – $O(n)$?

BRIEF Review of Hash Tables

Separate chaining:

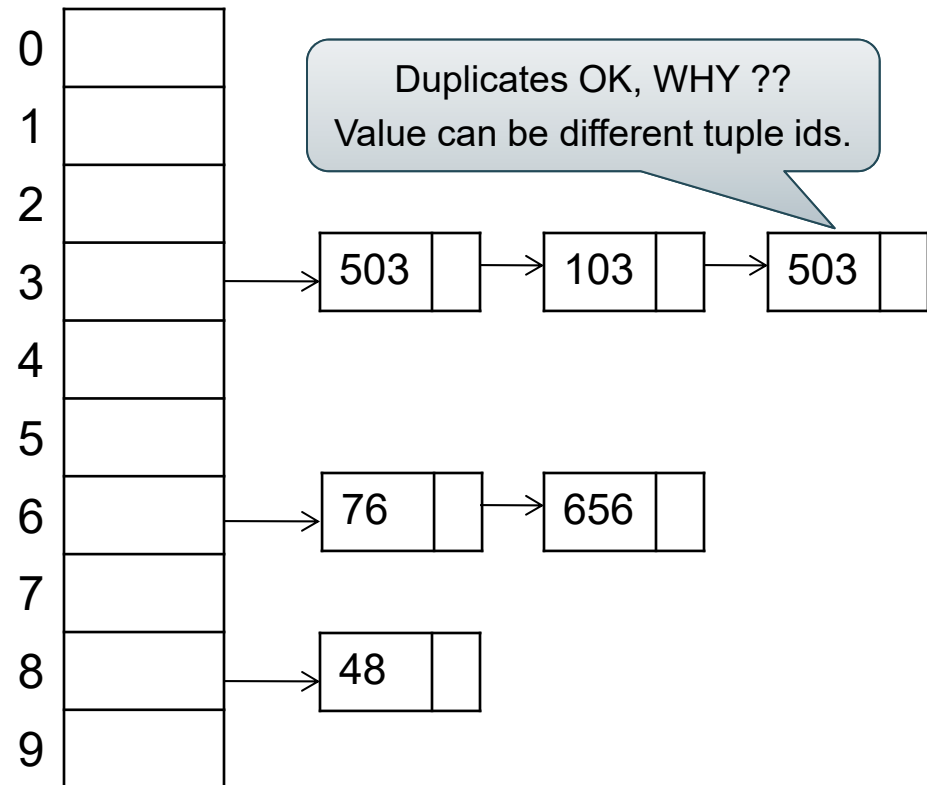
A (naïve) hash function:

$$h(x) = x \bmod 10$$

Operations:

$$\text{find}(103) = ??$$

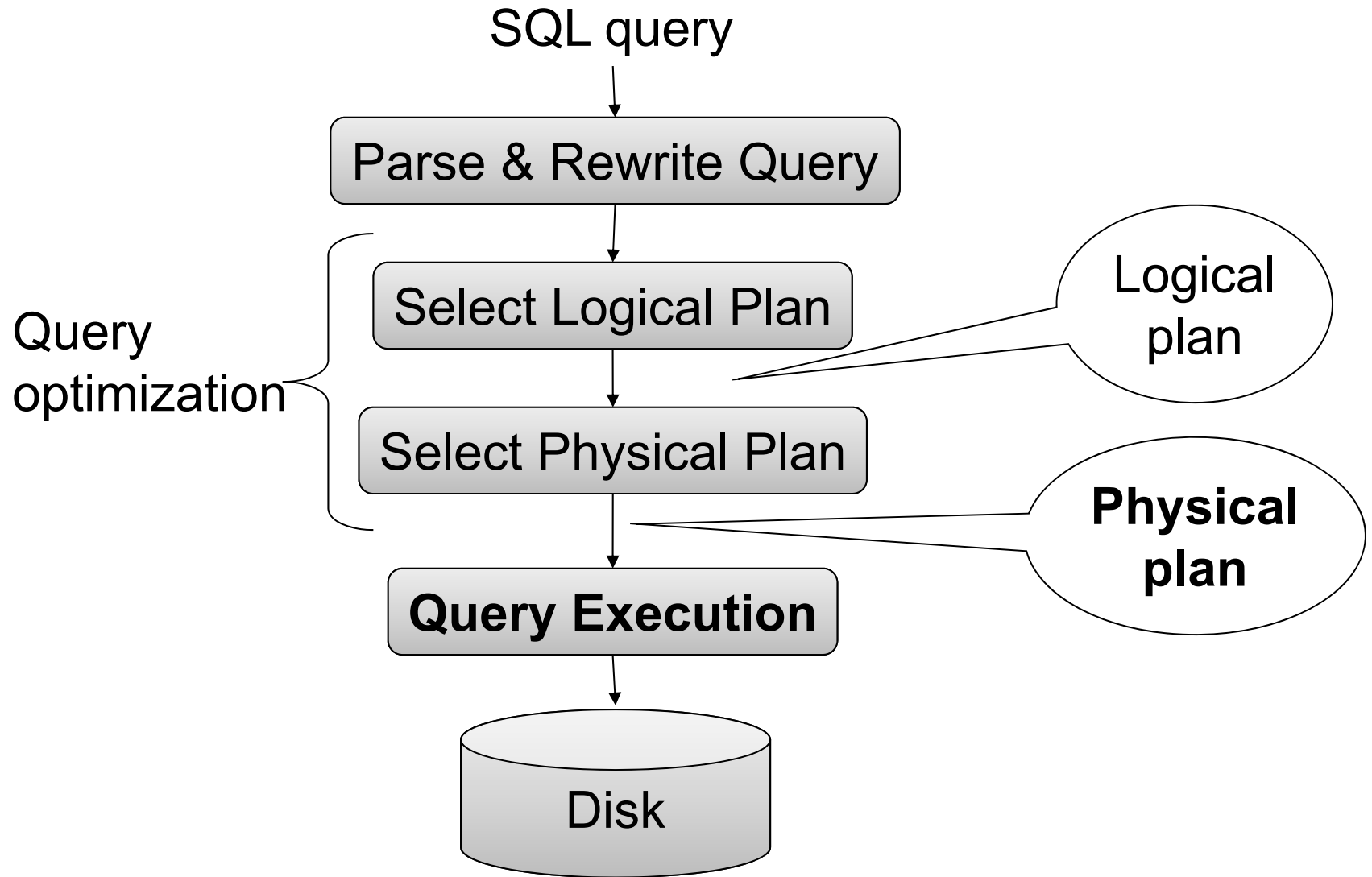
$$\text{insert}(488) = ??$$



BRIEF Review of Hash Tables

- $\text{insert}(k, v)$ = inserts a key k with value v
- Many values for one key
 - Hence, duplicate k 's are OK
- $\text{find}(k)$ = returns the *list* of all values v associated to the key k

Query Evaluation Steps Review



Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

Relational Algebra

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

Give a relational algebra expression for this query

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

Relational Algebra

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

$\pi_{\text{sname}}(\sigma_{\text{scity}='Seattle' \wedge \text{sstate}='WA' \wedge \text{pno}=2}(\text{Supplier} \bowtie_{\text{sid}=\text{sid}} \text{Supply}))$

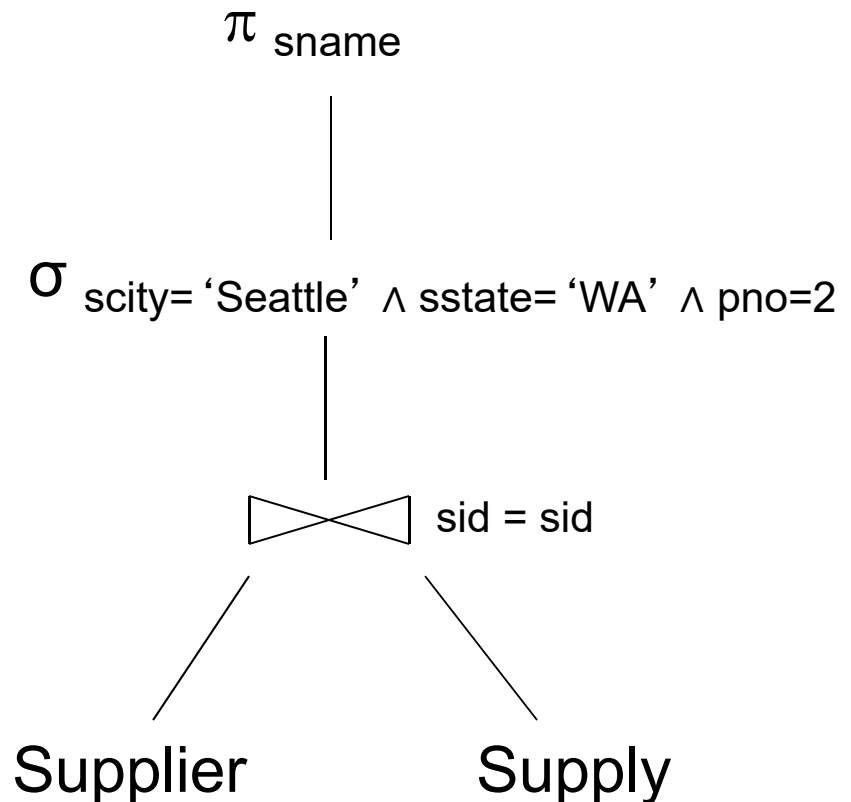
Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

Relational Algebra

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

Relational algebra expression is also called the “logical query plan”



Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

Physical Query Plan 1

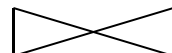
(On the fly)

π_{sname}

(On the fly)

$\sigma_{\text{scity}='Seattle' \wedge \text{sstate}='WA' \wedge \text{pno}=2}$

(Nested loop)


sid = sid

Supplier
(File scan)

Supply
(File scan)

A physical query plan is a logical query plan annotated with physical implementation details

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

Physical Query Plan 2

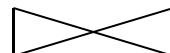
(On the fly)

π_{sname}

(On the fly)

$\sigma_{\text{scity}='Seattle' \wedge \text{sstate}='WA' \wedge \text{pno}=2}$

(Hash join)


sid = sid

Supplier
(File scan)

Supply
(File scan)

Same logical query plan
Different physical plan

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```


Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

Physical Query Plan 3

(On the fly)

(Sort-merge join)

(Scan & write to T1)

Different but equivalent logical query plan; different physical plan

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

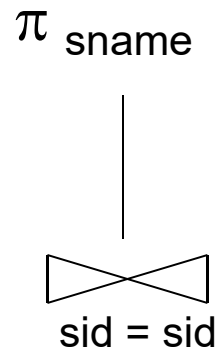
(Scan & write to T2)

$\sigma_{\text{scity}='Seattle' \wedge \text{sstate}='WA'}$

Supplier
(File scan)

$\sigma_{\text{pno}=2}$

Supply
(File scan)



Query Optimization Problem

- For each SQL query... many logical plans
- For each logical plan... many physical plans
- How to find a fast physical plan?
 - Will discuss in a few lectures