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# Symbols

CSE 413, Autumn 2002  
Programming Languages

<http://www.cs.washington.edu/education/courses/413/02au/>

# Readings and References

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- Reading
  - » Section 2.3.1, *Structure and Interpretation of Computer Programs*, by Abelson, Sussman, and Sussman
- Other References
  - » Sections 4.1.2, 6.1, 6.3.3, *Revised<sup>5</sup> Report on the Algorithmic Language Scheme (R5RS)*

# Evaluating symbols and expressions

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- We've been using symbols and lists of symbols to refer to values of all kinds in our programs

`(+ a 3)`

`(inc b)`

- Scheme evaluates the symbols and lists that we give it
  - » numbers evaluate to themselves
  - » symbols evaluate to their current value
  - » lists are evaluated as expressions defining procedure calls on a sets of actual arguments

# Manipulating symbols, not values

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- What if we want to manipulate the symbols, and not the value of the symbols
  - » perhaps evaluate after all the manipulation is done
- We need a way to say "use this symbol or list as it is, don't evaluate it"
- Special form `quote`

```
>(define a 1)
>a           => 1
>(quote a)   => a
```

# Special form: quote

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`(quote <datum>)`

*or* `'<datum>`

- This expression always evaluates to *datum*
  - » datum is the external representation of the object
- The `quote` form tells Scheme to treat the given expression as a data object directly, rather than as an expression to be evaluated

# Quote examples

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```
(define a 1)
```

```
a => 1
```

```
(quote a) => a
```

a is a symbol whose value is the number 1

```
(define b (+ a a))
```

```
b => 2
```

b is a symbol whose value is the number 2

```
(define c (quote (+ a b)))
```

```
c => (+ a b)
```

```
(car c) => +
```

```
(cadr c) => a
```

```
(caddr c) => b
```

c is a symbol whose value is the list (+ a b)

# quote can be abbreviated: '

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```
'a           => a
'(+ a b)     => (+ a b)
'()          => ()
(null? '())  => #t
```

a single quote has the exact same effect as the quote form

```
'(1 (2 3) 4)  => (1 (2 3) 4)
'(a (b (c)))  => (a (b (c)))
(car '(1 (2 3) 4)) => 1
(cdr '(1 (2 3) 4)) => ((2 3) 4)
```

lists are easily expressed as quoted objects

# Building lists with symbols

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- What would the interpreter print in response to evaluating each of the following expressions?

`(list 'a 'b)`

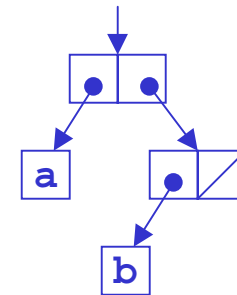
`(cons 'a (list 'b))`

`(cons 'a (cons 'b '()))`

`(cons 'a '(b))`

`'(a b)`

`(a b)`



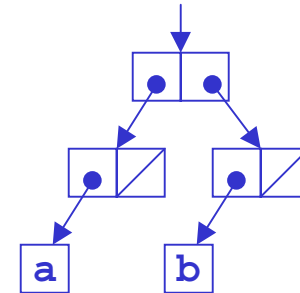


# Building lists with symbols

- What would the interpreter print in response to evaluating each of the following expressions?

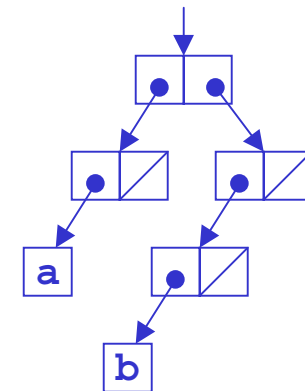
`(cons ' (a) ' (b) )`

`((a) b)`



`(list ' (a) ' (b) )`

`((a) (b))`



# Comparing items

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- Scheme provides several different means of comparing objects
  - » Do two numbers have the same value?  
(= a b)
  - » Are two objects the same object?  
(eq? a b) , (eqv? a b)
  - » Are the corresponding elements the same objects?  
Comparison is done recursively if elements are lists.  
(equal? list-a list-b)

# (member item s)

---

```
; find an item of any kind in a list s
; return the sublist that starts with the item
; or return #f
```

```
(define (member item s)
  (cond
    ((null? s) #f)
    ((equal? item (car s)) s)
    (else (member item (cdr s)))))
```

```
(member 'a '(c d a))           => (a)
(member '(1 3) '(1 (1 3) 3))   => ((1 3) 3)
(member 'b '(a (b) c))        => #f
```

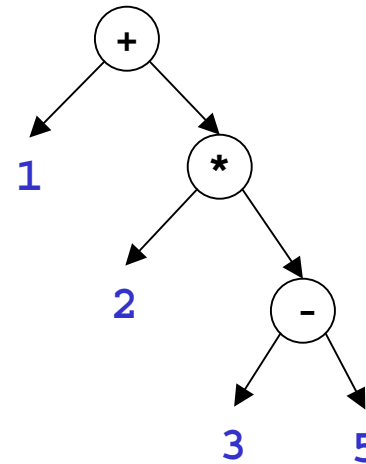
# Recall: Expression tree example

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infix notation       $(1 + (2 * (3 - 5)))$

Scheme expression       $(+ 1 (* 2 (- 3 5)))$

expression tree

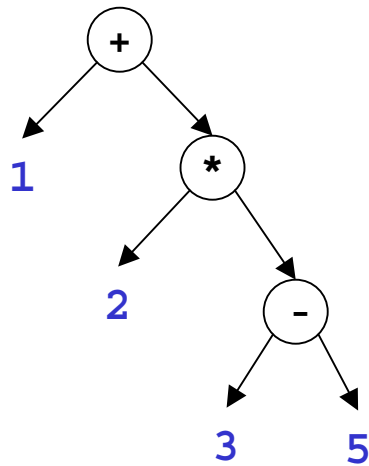


# Represent expression with a list

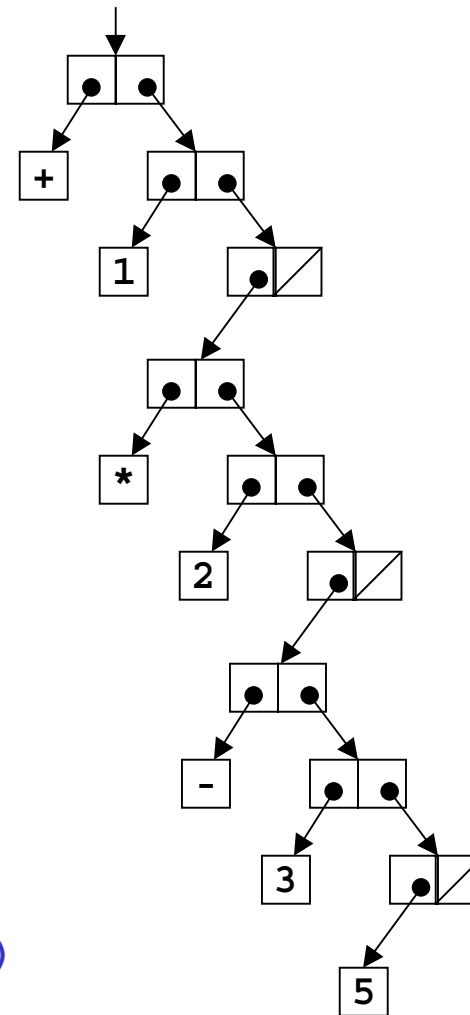
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- Each node is represented by a 3-element list
  - » (operator left-operand right-operand)
- Operands can be
  - » numbers (explicit values)
  - » other expressions (lists)
- In previous implementation, operators were the actual procedures
  - » This time, we will use symbols throughout

# Expressions as trees, trees as lists



logical expression tree  
(1 + (2 \* (3 - 5)))



our data structure

'(+ 1 (\* 2 (- 3 5)))

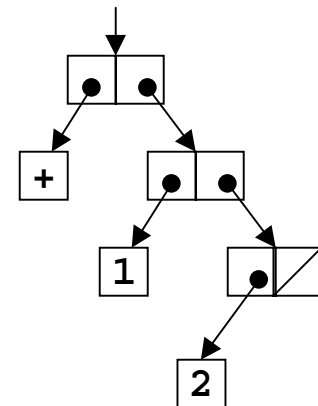
# eval-expr

---

```
(define (eval-op op)
  (cond
    ((eq? op '+) +)
    ((eq? op '-') -)
    ((eq? op '/') /)
    ((eq? op '*') *)))
```

```
(define (eval-expr exp)
  (if (not (pair? exp))
      exp
      ((eval-op (operator exp))
       (eval-expr (left exp))
       (eval-expr (right exp)))))
```

(eval-expr '(+ 1 2))

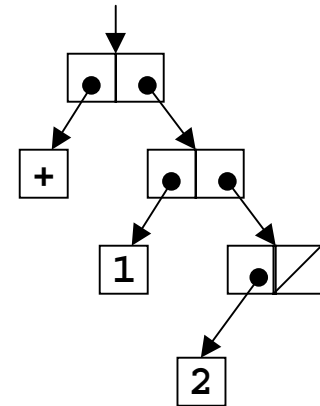


# evaluator

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```
(define (evaluator exp)
  (if (not (pair? exp))
      exp
      ((eval (operator exp))
       (eval-expr (left exp))
       (eval-expr (right exp)))))
```

(evaluator '(+ 1 2))

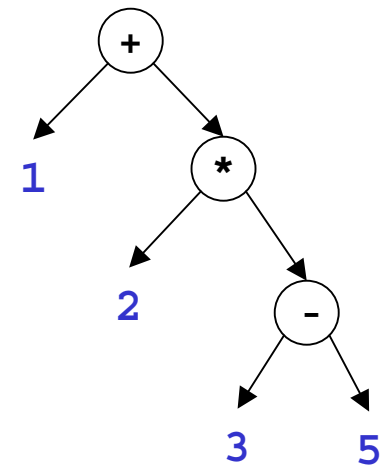




# Traversing a binary tree

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- Recall the definitions of traversal
  - » pre-order  
this node, left branch, right branch
  - » in-order  
left branch, this node, right branch
  - » post-order  
left branch, right branch, this node



$(1 + (2 * (3 - 5)))$

# Traverse the expression tree

---

```
(define f '(+ 1 (* 2 (- 3 5))))
```

```
(define (in-order exp)
  (if (not (pair? exp))
      (list exp)
      (append (in-order (left exp))
              (list (operator exp))
              (in-order (right exp)) )))
```

```
(in-order f)
(1 + 2 * 3 - 5)
```

```
(define (post-order exp)
  (if (not (pair? exp))
      (list exp)
      (append (post-order (left exp))
              (post-order (right exp))
              (list (operator exp)))))
```

```
(post-order f)
(1 2 3 5 - * +)
```