
More Lambda

CSE 413, Autumn 2002
Programming Languages

<http://www.cs.washington.edu/education/courses/413/02au/>

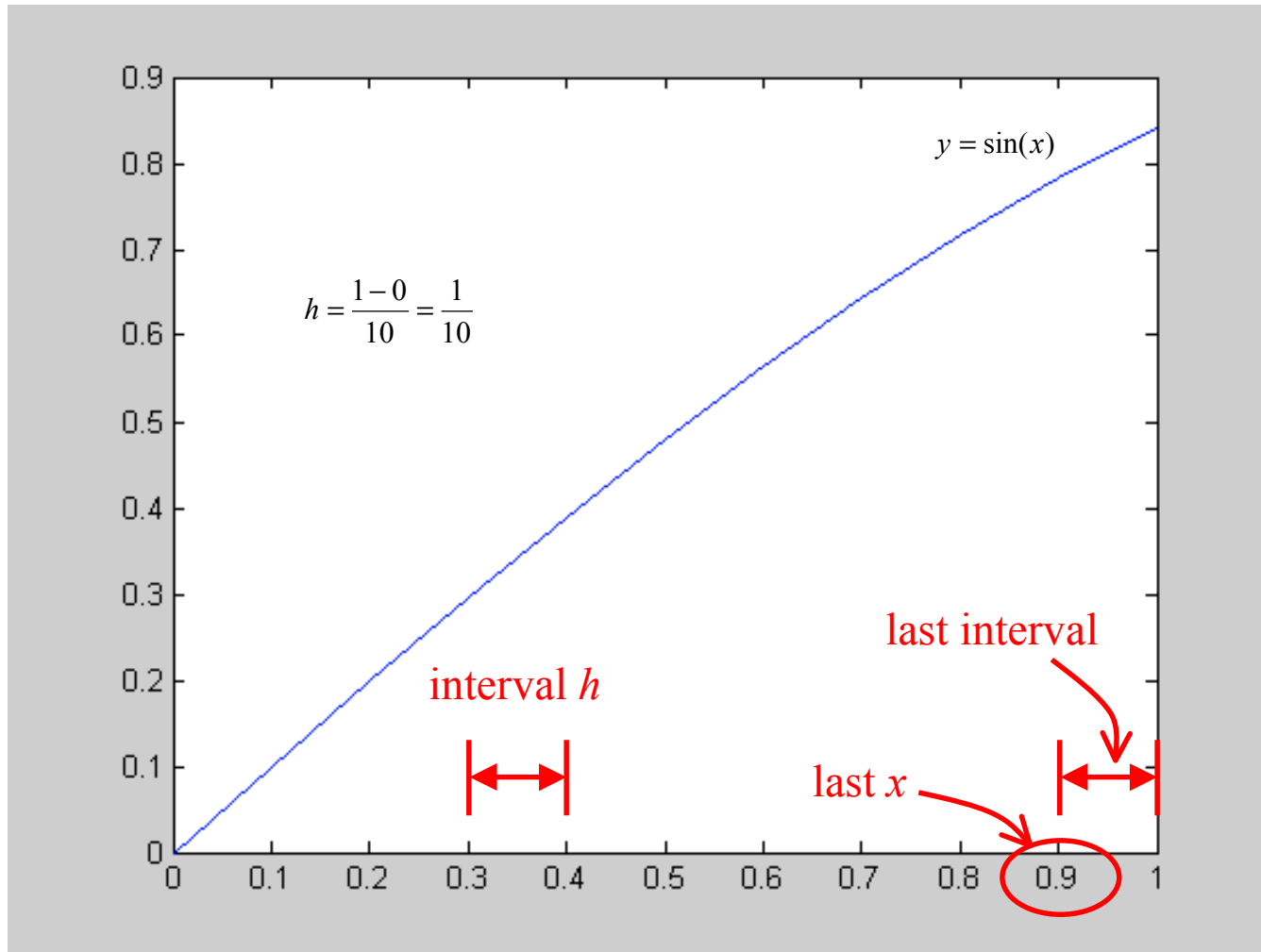
Readings and References

- Reading
 - » Section 1.3, *Structure and Interpretation of Computer Programs*, by Abelson, Sussman, and Sussman, but you've already read this, right?
- Other References

Procedures as unnamed blobs

- With `lambda`, we've separated the body of the procedure from any particular name for the procedure
- Procedures are objects like any other, and can be handed around from procedure to procedure as arguments, return values, etc
- Procedures can be defined and applied without ever getting a name assigned to them

a numeric interval



calculate-h

```
; define a function to calculate an  
; interval size (b-a)/n
```

```
(define calculate-h (lambda (a b n) (/ (- b a) n)))
```

define a function body ...



... and bind it to the name calculate-h



```
; try it out on [0,1]  
(calculate-h 0 1 10)
```

```
1  
-  
10
```

apply the function to some arguments



anonymous calculate-h

; do the same thing without naming the function

```
((lambda (a b n) (/ (- b a) n)) 0 1 10)
```

define a function body ...

... and apply it to some arguments

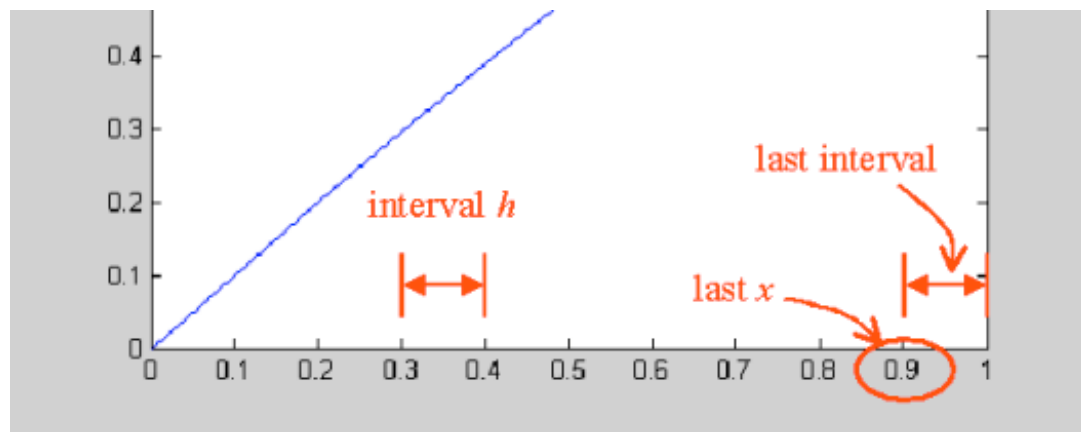
1
—
10

calculate last-x

```
; define a function that figures out what the beginning  
; of the last interval is
```

```
; calculate  $a+(h*(n-1))$  directly
```

```
(define (last-x1 a b n)  
  (+ a (* (- n 1) (/ (- b a) n))))
```




last-x using a helper function

`; calculate a+(k*h) using a simple function, and`
`; pre-calculate k and h to pass to the function`

```
(define (last-x2 a b n)
  (define (use-kh k h)
    (+ a (* k h)))
  (use-kh (- n 1) (/ (- b a) n)))
```

define a function body and
bind it to the name `use-kh`



apply `use-kh` to some arguments



last-x using anonymous helper function

; calculate $a+(k*h)$ using an anonymous function

```
(define (last-x3 a b n)
  ((lambda (k h) (+ a (* k h)))
   (- n 1)
   (/ (- b a) n)))
```

define a function body ...

... and apply it to some arguments

last-x with concealed anonymous function

; hide the use of the anonymous function by using let

```
(define (last-x4 a b n)
  (let ((h (/ (- b a) n))
        (k (- n 1)))
    (+ a (* k h))))
```

bind some values to some names ...



... and use those names in the body of the let



Special form `let`

```
(let ( (⟨var1⟩ ⟨exp1⟩ )
      (⟨var2⟩ ⟨exp2⟩ ) )
  ⟨body⟩ )
```

- When the `let` is evaluated, each expression exp_i is evaluated and the resulting value is associated with the related name var_i , then the *body* is evaluated.
- There is no order implied in the evaluation of exp_i
- This is exactly the same as parameter evaluation before a procedure call
 - » This *is* parameter evaluation before a procedure call

scope and let

; an example in scoping with let

```
(define x 2)
```

```
(let ((x 3)
      (y (+ x 2)))
  (* x y))
```

```
((lambda (x y)
  (* x y))
 3
(+ x 2))
```

this let and this lambda are equivalent

scope of the local x and y

the parameter values are calculated *outside* the scope of the parameter variables in the procedure

nesting lets lets us get x

`; nested lets and let*`

```
(define x 2) ] ← is this x referenced anywhere?
```

```
(let ((x 3))  
  (let ((y (+ x 2)))  
    (* x y)))
```

```
(let* ((x 3)  
      (y (+ x 2)))  
  (* x y))
```

Special form `let*`

`(let* ((<var1> <exp1>)
 (<var2> <exp2>))
<body>)`

- When the `let*` is evaluated, each expression exp_i is evaluated in turn and the resulting value is associated with the related name var_i , then the *body* is evaluated.
- The exp_i are evaluated in left to right order
 - » each binding indicated by $(\langle var_i \rangle \langle exp_i \rangle)$ is part of the environment for $(\langle var_{i+1} \rangle \langle exp_{i+1} \rangle)$ and following
 - » This is exactly equivalent to nesting the `let` statements

an iterator with parameter h

`; show all the x values on the interval`

```
(define (show-x1 a b n)
  (define (iter h count)
    (if (> count n)
        (newline)
        (begin
            (display (+ a (* h count)))
            (display " ")
            (iter h (+ count 1)))))
  (iter (/ (- b a) n) 0))
```

h defined in enclosing scope

```
; show all the x values on the interval  
; using let
```

```
(define (show-x2 a b n)  
  (let ((h (/ (- b a) n)))  
    (define (iter count)  
      (if (> count n)  
          (newline)  
          (begin  
            (display (+ a (* h count)))  
            (display " ")  
            (iter (+ count 1)))))  
    (iter 0)))
```


Special form `begin`

(begin $\langle exp_1 \rangle$ $\langle exp_2 \rangle$... $\langle exp_n \rangle$)

- Evaluate the exp_i in sequence from left to right
- The value returned by the entire `begin` expression is the value of exp_n
- Best used to sequence side effects like I/O
 - » for example displaying each of the `x` values in `show-x`
- There is implicit sequencing in the body of a `lambda` procedure or a `let` but we generally don't use it
 - » the procedure returns the value of the last exp_i , so the body of most of our procedures consists of one expression only

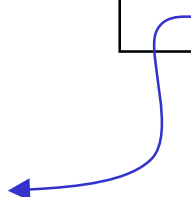
sequencing with begin

```
; show all the x values on the interval  
; using let
```

```
(define (show-x2 a b n)  
  (let ((h (/ (- b a) n)))  
    (define (iter count)  
      (if (> count n)  
          (newline)  
          (begin  
            (display (+ a (* h count)))  
            (display " ")  
            (iter (+ count 1))))))  
    (iter 0)))
```

special form: `if`

```
(if exp  
    tx  
    fx)
```



show-x

Welcome to DrScheme, version 201.

Language: Standard (R5RS).

```
> (show-x2 0 1 10)
```

```
0  1/10  1/5  3/10  2/5  1/2  3/5  7/10  4/5  9/10  1
```

```
>
```

