

# Not My Problem

Crowdsourcing Code Verification With Video Games

## Section 8.2 Program Correctness (for imperative programs)

A theory of program correctness needs wffs, axioms, and inference rules.

Wffs (called Hoare triples) are of the form

$$\{P\} S \{Q\}$$

Where  $S$  is a program statement and  $P$  (a *precondition*) and  $Q$  (a *postcondition*) are logical statements about the variables of  $S$ .

*Semantics*: The meaning of  $\{P\} S \{Q\}$  is the truth value of the statement:

If  $P$  is true before  $S$  executes, then  $Q$  is true after  $S$  halts.

Note that it is assumed that  $S$  halts. If  $\{P\} S \{Q\}$  is true, then  $S$  is said to be *correct* wrt to precondition  $P$  and postcondition  $Q$ .

*Assignment Axiom (AA)*:  $\{P(x/t)\} x := t \{P\}$ .

*Example*.  $\{x = 4\} x := x - 1 \{x = 3\}$ .

*Example*.  $\{x < 4\} x := x - 1 \{x < 3\}$ .

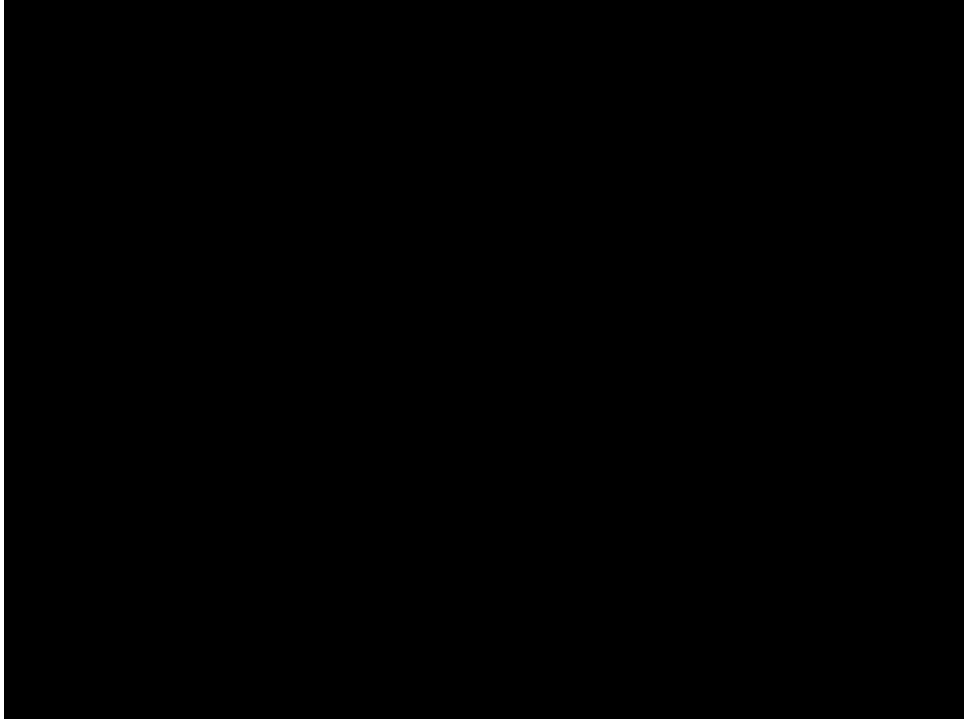
### Inference Rules

**Consequence Rule:** 
$$\frac{P \rightarrow R \text{ and } \{R\} S \{Q\}}{\{P\} S \{Q\}} \quad \text{and} \quad \frac{\{P\} S \{T\} \text{ and } T \rightarrow Q}{\{P\} S \{Q\}}$$

*Example*. Prove the correctness of  $\{x < 3\} x := x - 1 \{x < 3\}$ .

Proof:	1.	$\{x < 4\} x := x - 1 \{x < 3\}$	AA
	2.	$x < 3$	$P$ [for $(x < 3) \rightarrow (x < 4)$ ]
	3.	$x < 4$	2, $T$
	4.	$(x < 3) \rightarrow (x < 4)$	2-3, CP
	5.	$\{x < 3\} x := x - 1 \{x < 3\}$	1, 4, Consequence. QED.

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<https://www.cs.washington.edu/verigames>

