

# Section 4: CUP & LL

CSE 401/M501

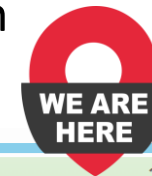
Adapted from Autumn 2022

# Administrivia

- Homework 2 is due tonight!
  - You have late days if you need them (2 max)
- Parser is due one week from today (also 2 late days)
  - Be sure to check your scanner feedback – out later this week
- HW3 will be out soon, due in 1.5 weeks on **Monday, May 5<sup>th</sup>**
  - **Only one late day allowed** on this assignment so we can distribute solutions before the midterm at the end of that week.
  - More on hw3 in sections next week, but start before then if you can

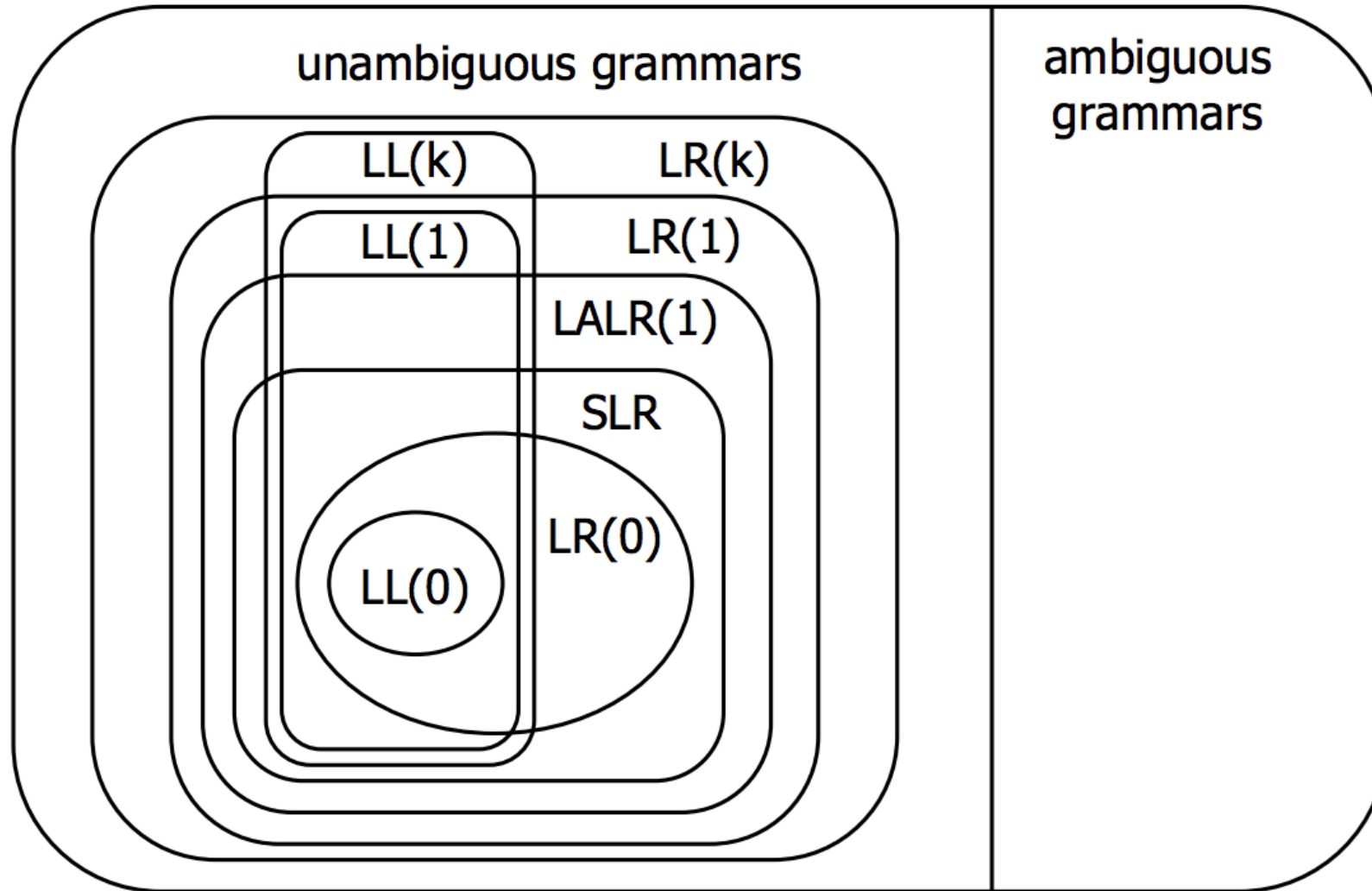
## April:

11:30-12:30 OH (Karen) CSE2 150	21	13:30-14:30 OH (Sriya) CSE2 152	22	11:30-12:30 OH (Karen) CSE2 150	23	Section <i>CUP parser generator, ASTs; LL parsing</i>	24	13:30-14:30 OH (Sriya) CSE2 152	25
13:00-14:00 OH (Bill) CSE 3rd floor breakout		14:30-15:30 OH (Eric) CSE2 152		13:00-14:00 OH (Bill) CSE 3rd floor breakout		15:30-16:30 OH (Eric) CSE2 152		14:30-15:20 Lecture CSE2 G10	
14:30-15:20 Lecture CSE2 G10 <i>ASTs &amp; visitors</i>				14:30-15:20 Lecture CSE2 G10 <i>LL Parsing &amp; recursive descent (3.3)</i>		23:59 <b>hw2 due</b> (LR grammars)		<i>Intro to Checking (Semantics and Types) (4.1-4.2)</i>	



# Parser Live Demo

# Language Hierarchies



# The CUP parser generator

- Uses LALR(1)
  - A little weaker (less selective), but many fewer states than LR(1) parsers
  - Handles most realistic programming language grammars
  - More selective than SLR (or LR(0)) about when to do reductions, so works for more languages

# The CUP parser generator

- LALR(1) parser generator based on YACC and Bison
- CUP can resolve some ambiguities itself
  - Precedence for reduce/reduce conflicts
  - Associativity for shift/reduce conflicts
  - Useful for our project for things like arithmetic expressions (use  $\text{exp}+\text{exp}$ ,  $\text{exp}*\text{exp}$ , etc. for fewer non-terminals, then add precedence and associativity declarations). *Read the CUP docs!*

# MiniJava Grammar -> AST Node

Use this to check your work *only after* your team has examined the grammar and AST code first.

Program

MainClass

ClassDecl

VarDecl

MethodDecl

Type

Statement

Exp

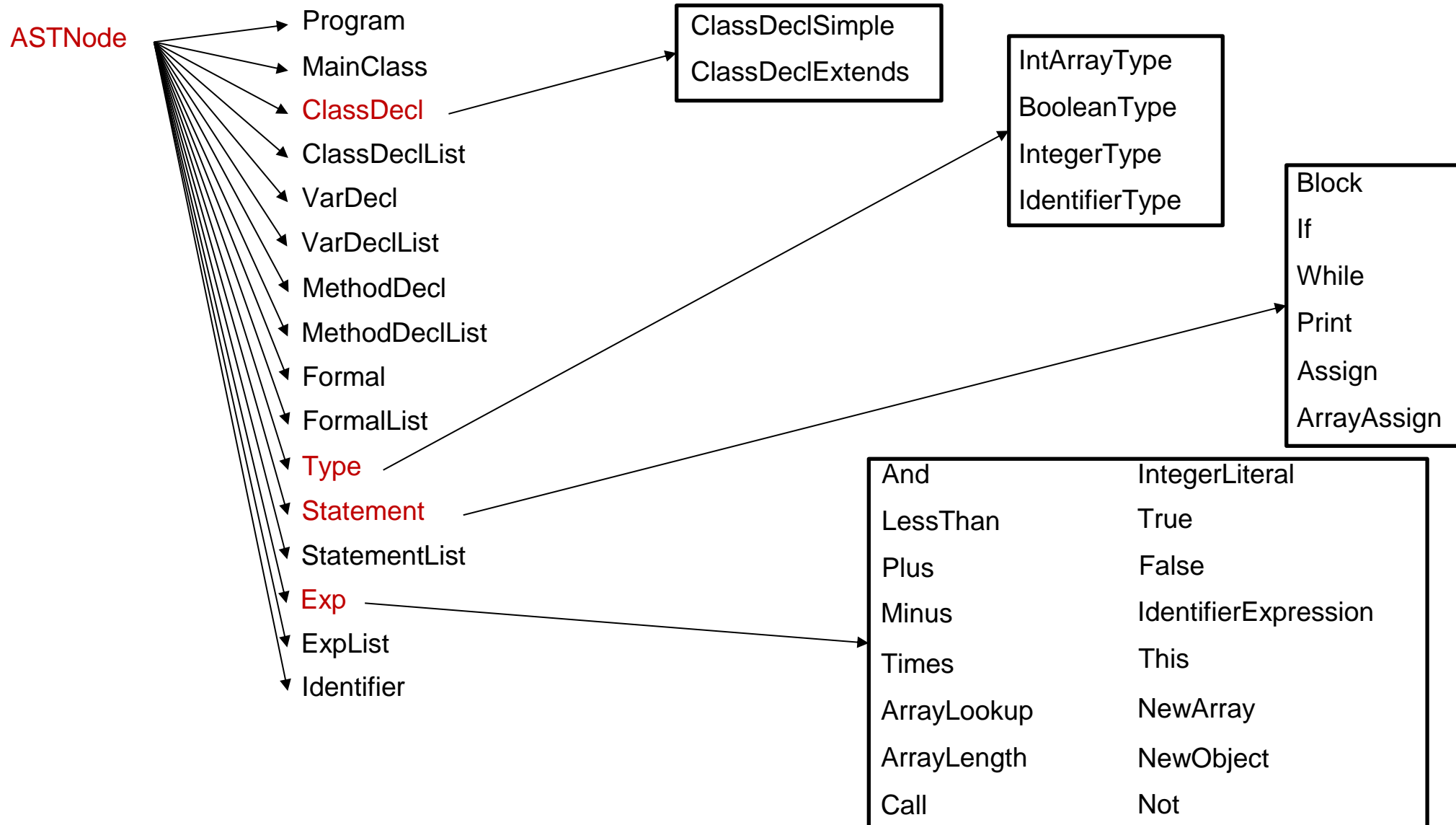
Identifier

```
Goal ::= MainClass ( ClassDeclaration )* <EOF>
MainClass ::= "class" Identifier "{" "public" "static" "void" "main" "(" "String" "[" "]" Identifier ")" "{" Statement "}" "}"
ClassDeclaration ::= "class" Identifier ( "extends" Identifier )? "{" ( VarDeclaration )* ( MethodDeclaration )* "}"
VarDeclaration ::= Type Identifier ";"
MethodDeclaration ::= "public" Type Identifier "(" ( Type Identifier ( "," Type Identifier )* )? ")" "{" ( VarDeclaration )* ( Statement )* "return" Expression ";" "}"
Type ::= "int" "[" "]"
      | "boolean"
      | "int"
      | Identifier
Statement ::= "{" ( Statement )* "}"
      | "if" "(" Expression ")" Statement "else" Statement
      | "while" "(" Expression ")" Statement
      | "System.out.println" "(" Expression ")" ";"
      | Identifier "=" Expression ";"
      | Identifier "[" Expression "]" "=" Expression ";"
Expression ::= Expression ( "&&" | "<" | "+" | "-" | "*" ) Expression
      | Expression "[" Expression "]"
      | Expression "." "length"
      | Expression "." Identifier "(" ( Expression ( "," Expression )* )? ")"
      | <INTEGER_LITERAL>
      | "true"
      | "false"
      | Identifier
      | "this"
      | "new" "int" "[" Expression "]"
      | "new" Identifier "(" " "
      | "!" Expression
      | "(" Expression ")"
Identifier ::= <IDENTIFIER>
```

ClassDeclSimple  
ClassDeclExtends (if there is "extends")

Formal  
Block

# Abstract Syntax Tree Class Hierarchy



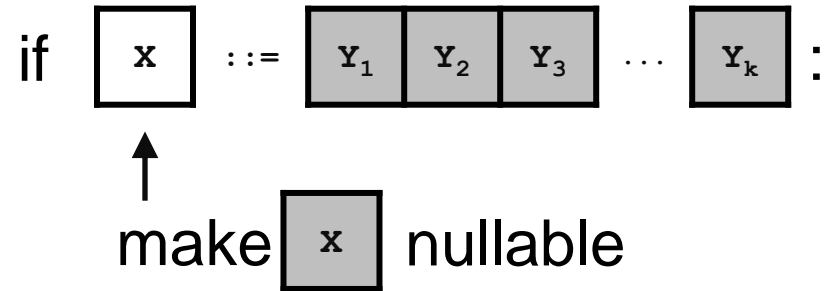


# LL Parsing

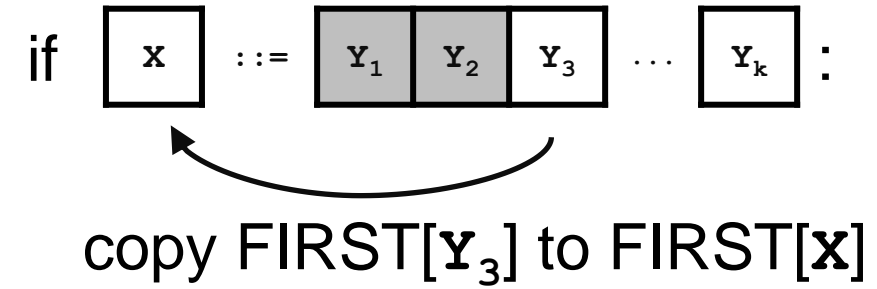
# Computing FIRST, FOLLOW, & nullable (3)

$\boxed{Y}$  = nullable

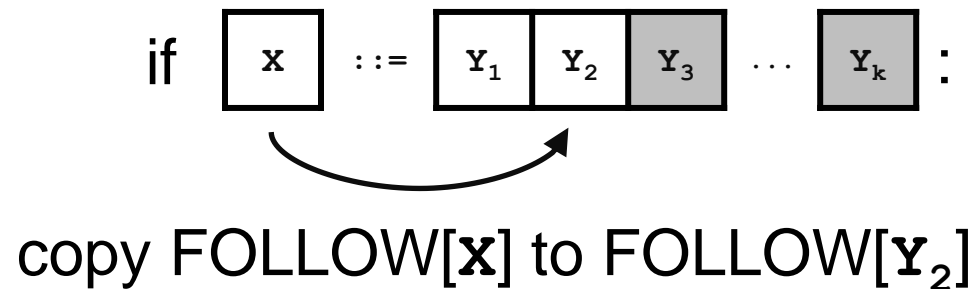
1



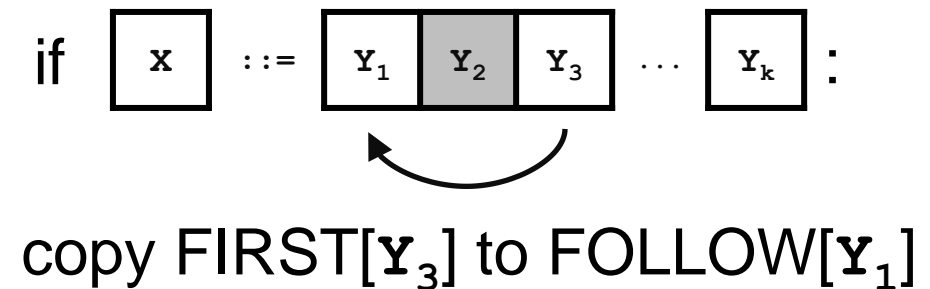
2



3



4



# Computing FIRST, FOLLOW, and nullable

```
repeat
  for each production  $X := Y_1 Y_2 \dots Y_k$ 
    if  $Y_1 \dots Y_k$  are all nullable (or if  $k = 0$ )
      set nullable[X] = true
    for each  $i$  from 1 to  $k$  and each  $j$  from  $i + 1$  to  $k$ 
      if  $Y_1 \dots Y_{i-1}$  are all nullable (or if  $i = 1$ )
        add FIRST[ $Y_i$ ] to FIRST[X]
      if  $Y_{i+1} \dots Y_k$  are all nullable (or if  $i = k$ )
        add FOLLOW[X] to FOLLOW[ $Y_i$ ]
      if  $Y_{i+1} \dots Y_{j-1}$  are all nullable (or if  $i+1=j$ )
        add FIRST[ $Y_j$ ] to FOLLOW[ $Y_i$ ]
Until FIRST, FOLLOW, and nullable do not change
```

L L (k)



## Left-to-Right

Only takes one pass,  
performed from the left

## Leftmost

At each point, finds the  
derivation for the leftmost  
handle (**top-down**)

## k Terminal Lookahead

Must determine derivation  
from the next unparsed  
terminal in the string  
Typically  $k = 1$ , just like LR

# LL( $k$ ) parsing

- LL( $k$ ) scans left-to-right, builds leftmost derivation, and looks ahead  $k$  symbols
- The LL condition enables the parser to choose productions correctly with 1 symbol of look-ahead
- We can often transform a grammar to satisfy this if needed

# LL(1) parsing: An example top-down derivation of “a z x”

0.  $S ::= a B$

1.  $B ::= C x \mid y$

2.  $C ::= \epsilon \mid z$

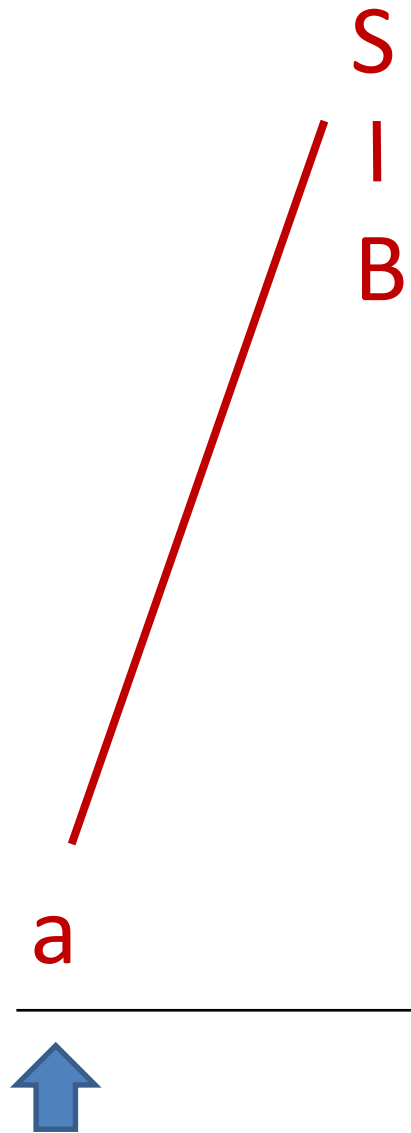
Lookahead

Remaining

a

z x

# Top-Down Derivation of “a z x”



0.  $S ::= a B$

1.  $B ::= C x \mid y$

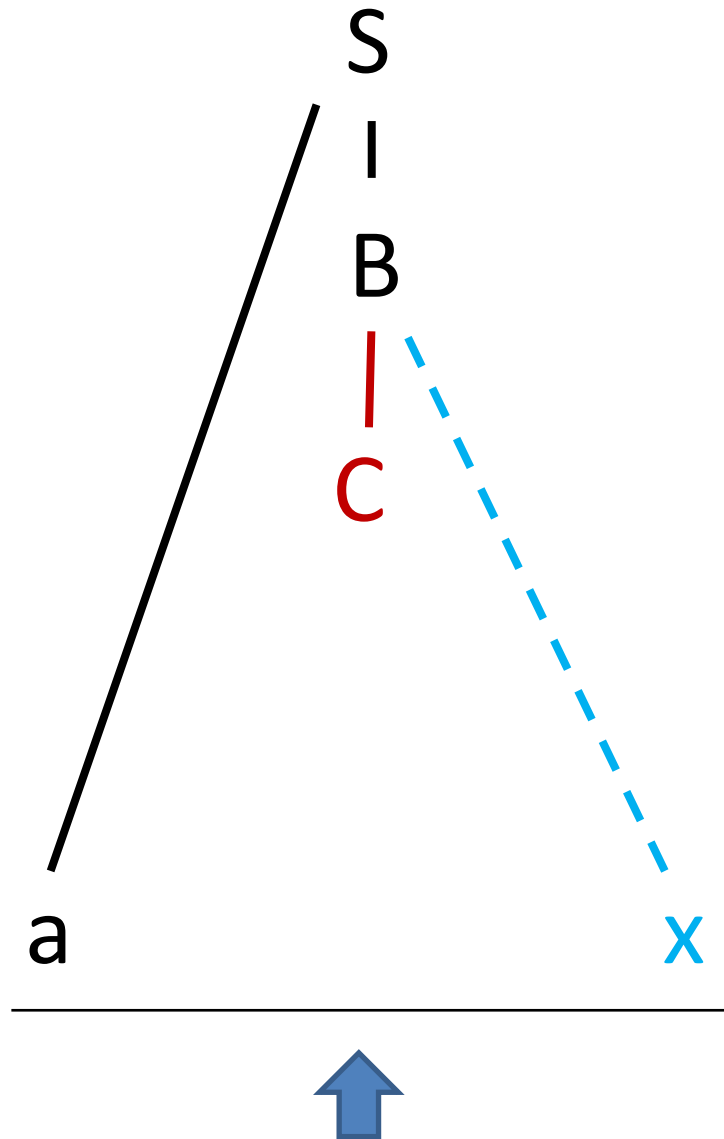
2.  $C ::= \varepsilon \mid z$

Lookahead      Remaining

a

z x

# Top-Down Derivation of "a z x"



0.  $S ::= a B$

1.  $B ::= C x \mid y$

2.  $C ::= \varepsilon \mid z$

Lookahead

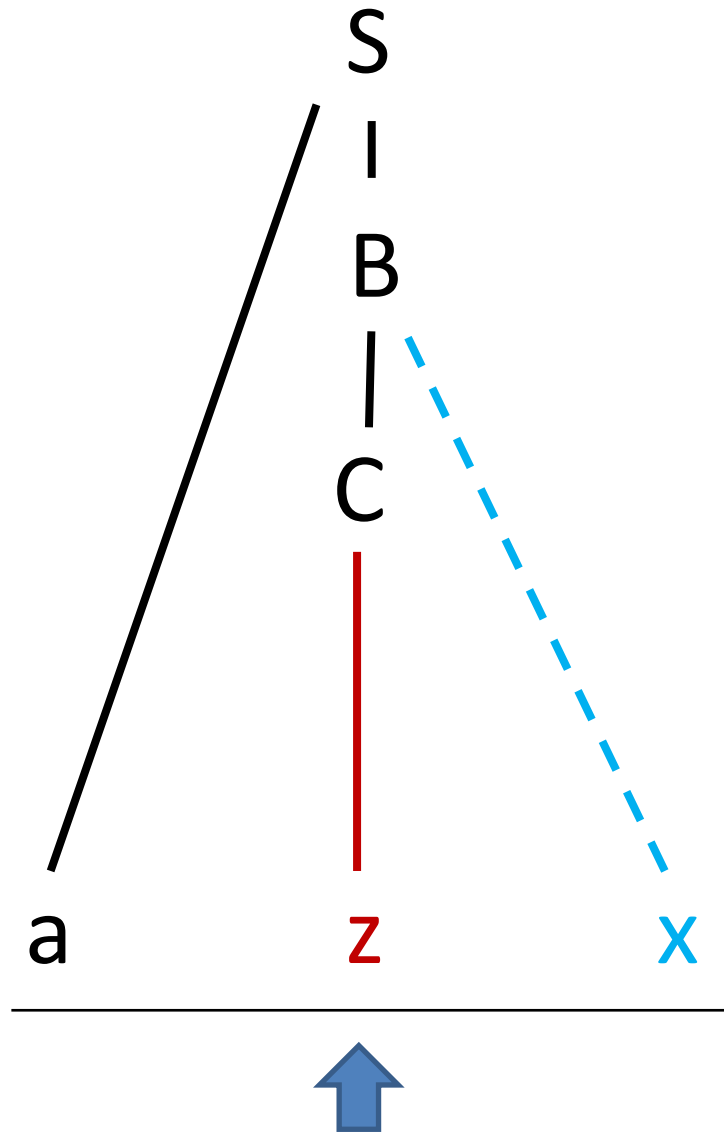
Remaining

**z**

x



# Top-Down Derivation of “a z x”



0.  $S ::= a B$

1.  $B ::= C x \mid y$

2.  $C ::= \varepsilon \mid z$

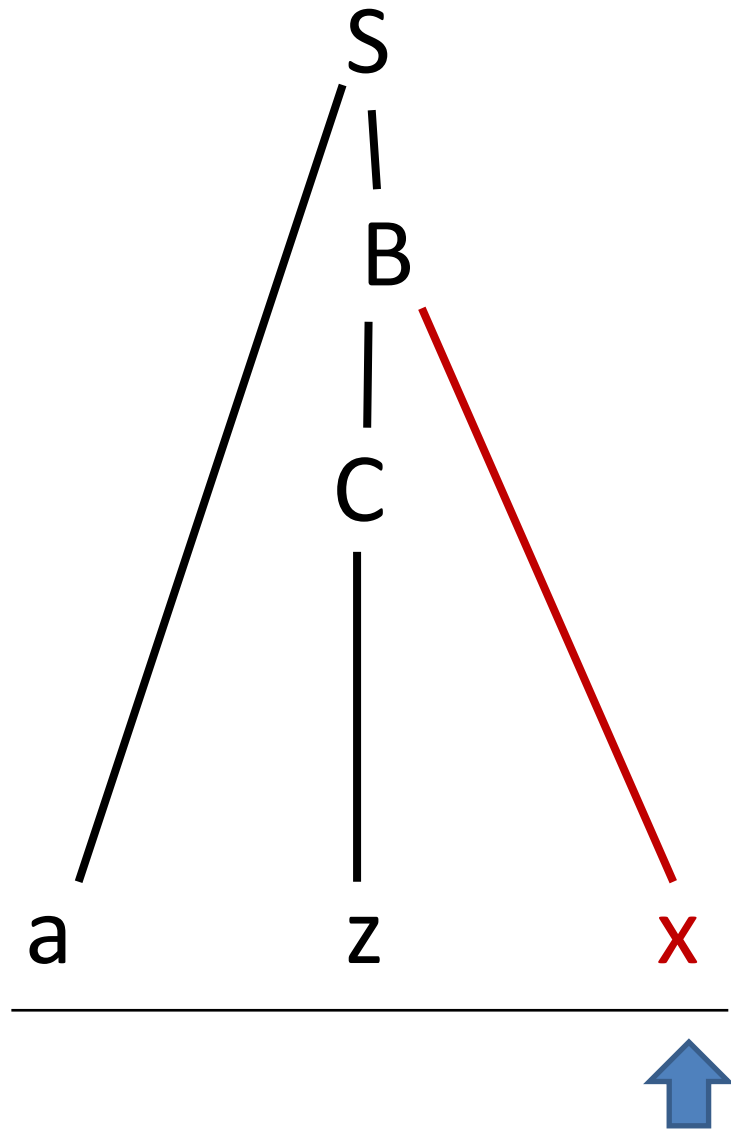
Lookahead

Remaining

$z$

$x$

# Top-Down Derivation of “a z x”



0.  $S ::= a B$

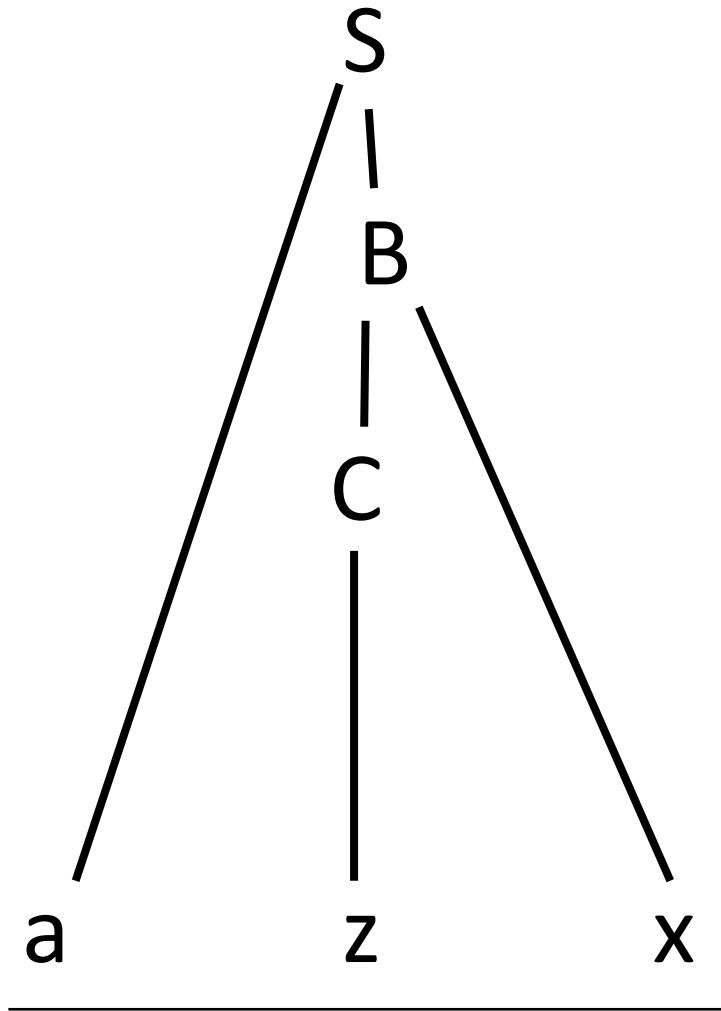
1.  $B ::= C x \mid y$

2.  $C ::= \varepsilon \mid z$

Lookahead      Remaining

x

# Top-Down Derivation of “a z x”



0. **S ::= a B**

1. **B ::= C x | y**

2. **C ::= ε | z**

Successful parse!

# LL Condition

For each nonterminal in the grammar:

- Its *productions* must have disjoint FIRST sets

✗  $A ::= x \mid B$   
 $B ::= x$

✓  $A ::= x \mid B$   
 $B ::= y$

- If it is *nullable*, the FIRST sets of its productions must be disjoint from its FOLLOW set

✗  $S ::= A x$   
 $A ::= \varepsilon \mid x$

✓  $S ::= A y$   
 $A ::= \varepsilon \mid x$

**\*\***We can often transform a grammar to satisfy this if needed

# Canonical FIRST Conflict

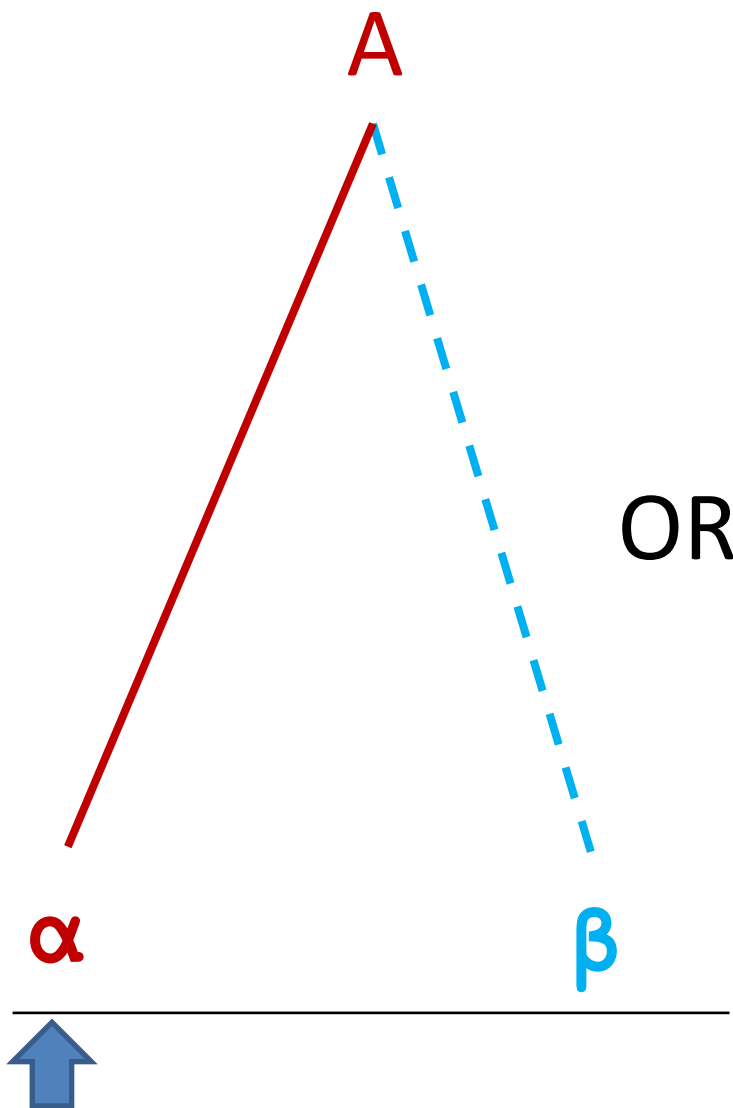
## Problem

$$0. \quad A ::= \alpha\beta \mid \alpha\gamma$$

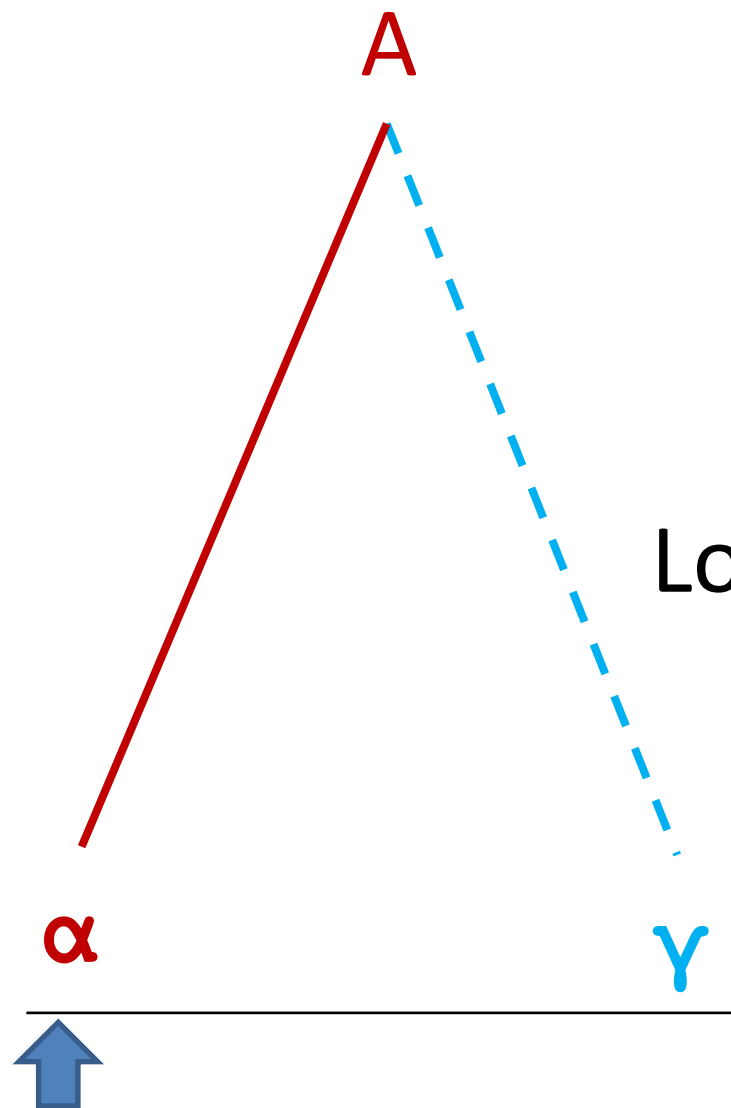
The FIRST sets of the right-hand sides for the SAME NON-TERMINAL must be disjoint!

# Let's try a top-down derivation of $\alpha\beta$

0.  $A ::= \alpha\beta \mid \alpha\gamma$



OR



Lookahead

$\alpha$

Remaining

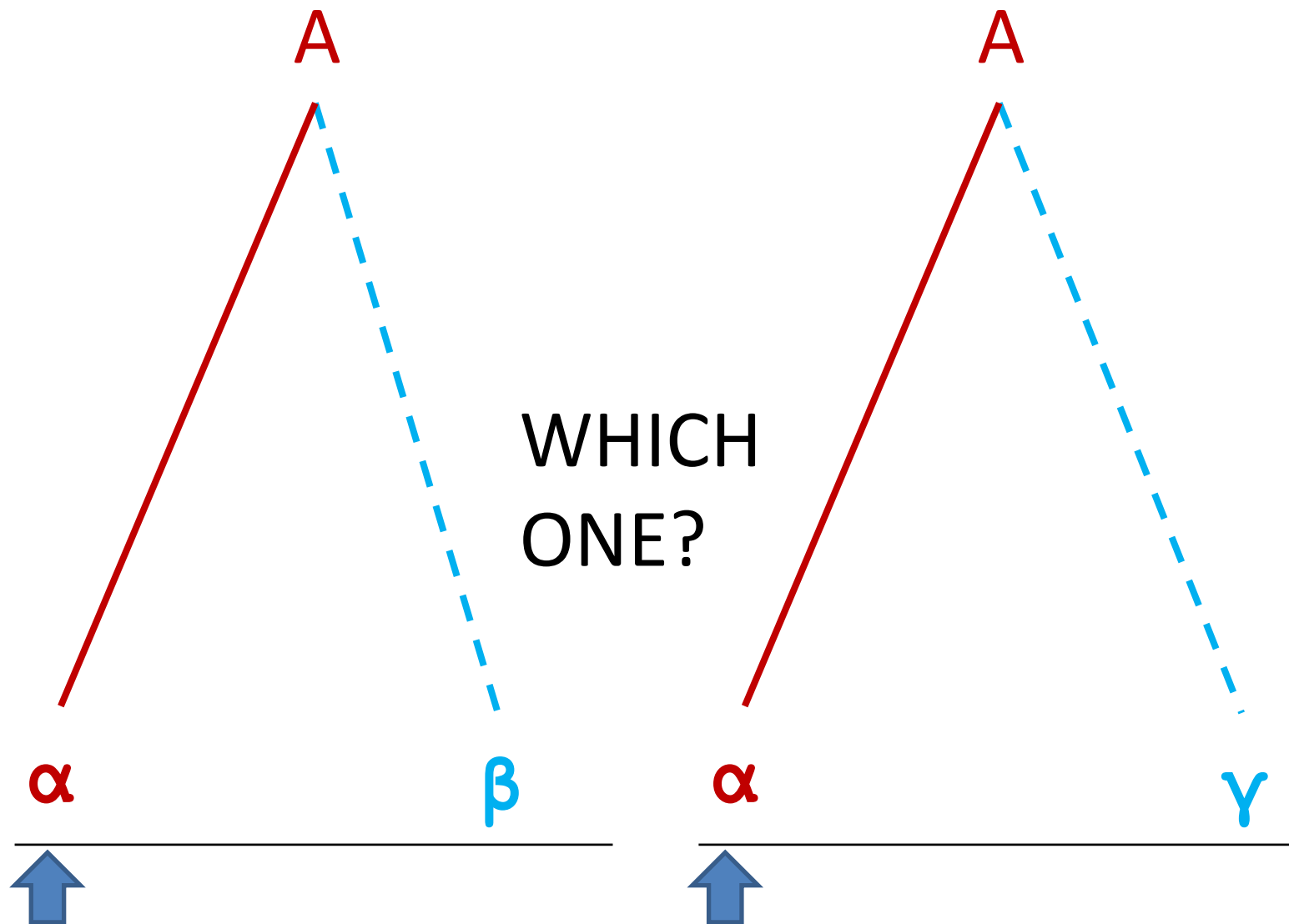
$\beta$

# Let's try a top-down derivation of $\alpha\beta$

0.  $A ::= \alpha\beta \mid \alpha\gamma$

We don't know!

We are using an LL(1) parser, we can't see more than  $\alpha$ !



# Canonical FIRST Conflict Solution

## Solution

0.  $A ::= \alpha\beta \mid \alpha\gamma$

0.  $A ::= \alpha \text{Tail}$

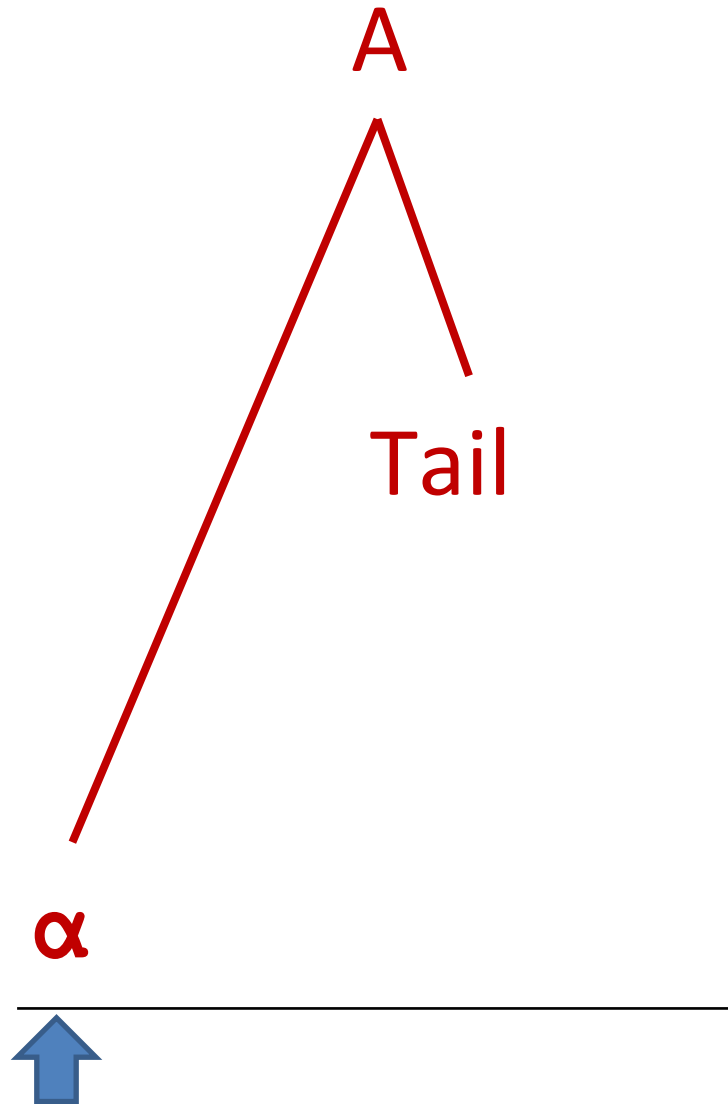
1.  $\text{Tail} ::= \beta \mid \gamma$

Factor out the  
common prefix

When multiple productions of a nonterminal share a common prefix, turn the different suffixes into a new nonterminal.



# Top-Down Derivation of “ $\alpha\beta$ ”



0.  $A ::= \alpha \text{ Tail}$

1.  $\text{Tail} ::= \beta \mid \gamma$

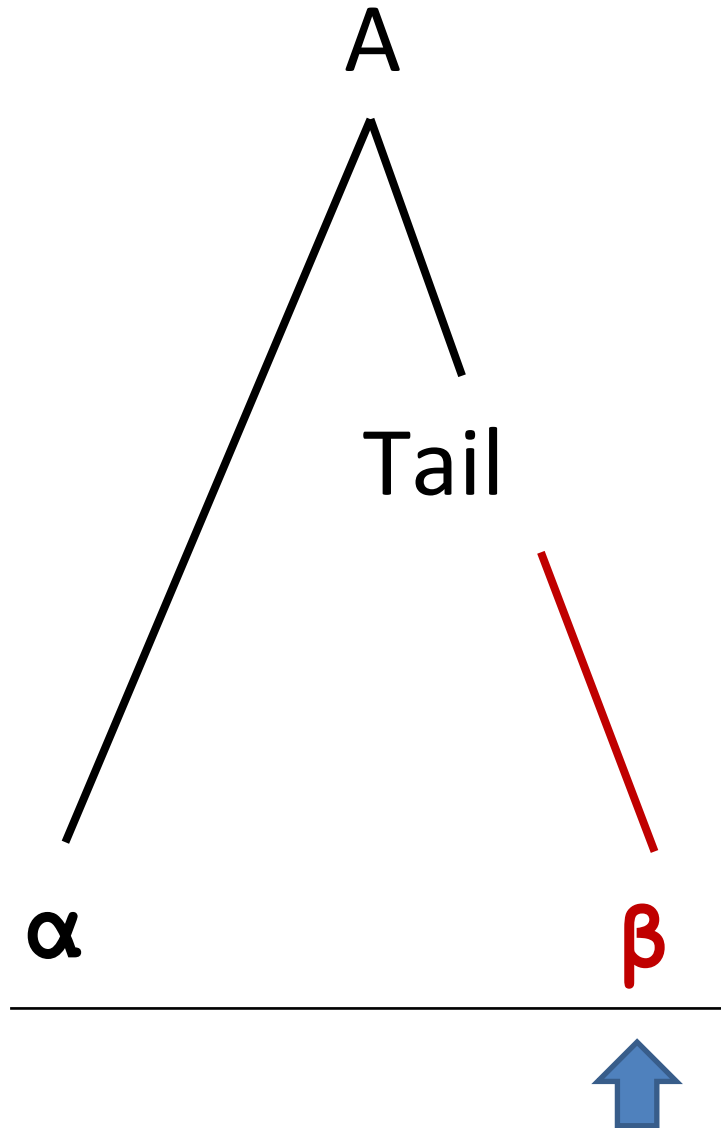
Lookahead

Remaining

$\alpha$

$\beta$

# Top-Down Derivation of “ $\alpha\beta$ ”



0.  $A ::= \alpha \text{ Tail}$

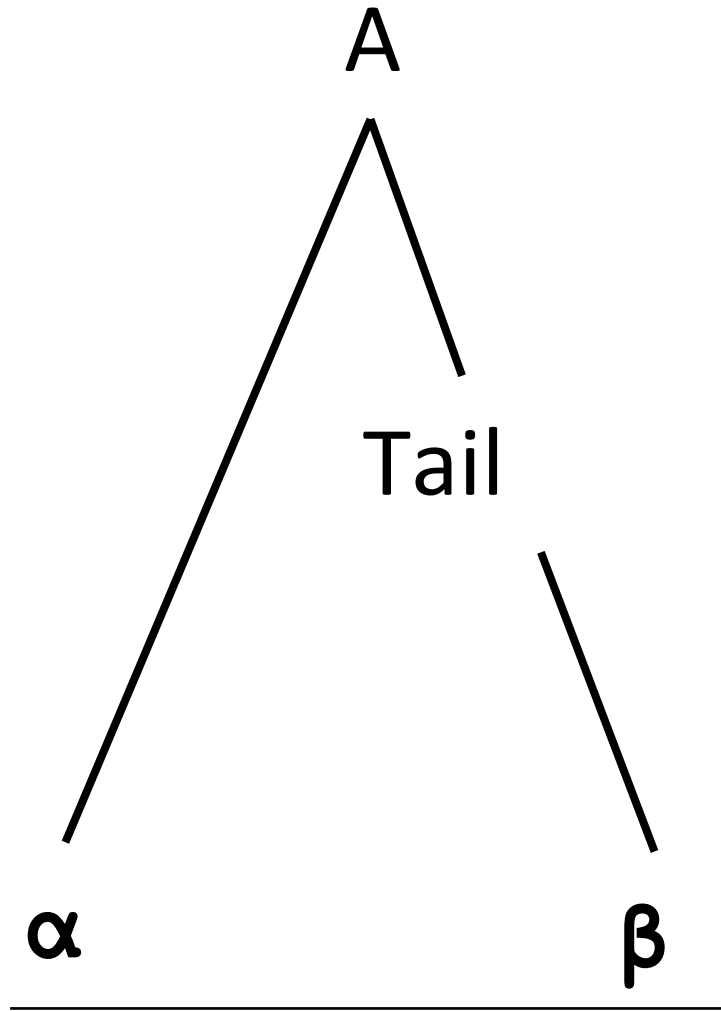
1.  $\text{Tail} ::= \beta \mid \gamma$

Lookahead

Remaining

$\beta$

# Top-Down Derivation of “ $\alpha\beta$ ”



0.  $A ::= \alpha \text{ Tail}$

1.  $\text{Tail} ::= \beta \mid \gamma$

Successful parse!

# Changing original grammar a little (Grammar 1)

0.  $S ::= a B \mid a w$

1.  $B ::= C x \mid y$

2.  $C ::= \varepsilon \mid z$

Lookahead

Remaining

a

z x

# What's the issue?

0.  $S ::= \boxed{\mathbf{a} \ B} \mid \boxed{\mathbf{a} \ W}$   
1.  $B ::= C \ x \mid y$   
2.  $C ::= \varepsilon \mid z$

There's a FIRST Conflict!

# Top-Down Derivation of “a z x”: LL(1) can't parse

0.  $S ::= a B \mid a w$

1.  $B ::= C x \mid y$

2.  $C ::= \varepsilon \mid z$

$S$

$|$

$B$

OR

$S$

$|$

$w$

Lookahead

Remaining

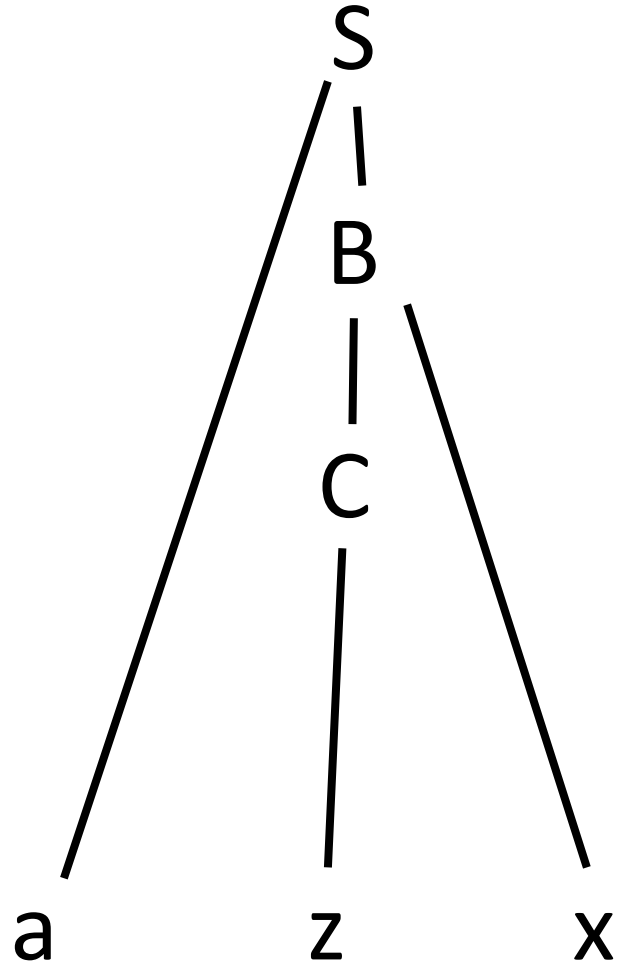
a

z x

a

a

# Parse Tree without changing Grammar



0.  $S ::= a B \mid a w$

1.  $B ::= C x \mid y$

2.  $C ::= \varepsilon \mid z$

# Applying the Fix: Factor out the Common Prefix

0.  $S ::= a \text{ Tail}$

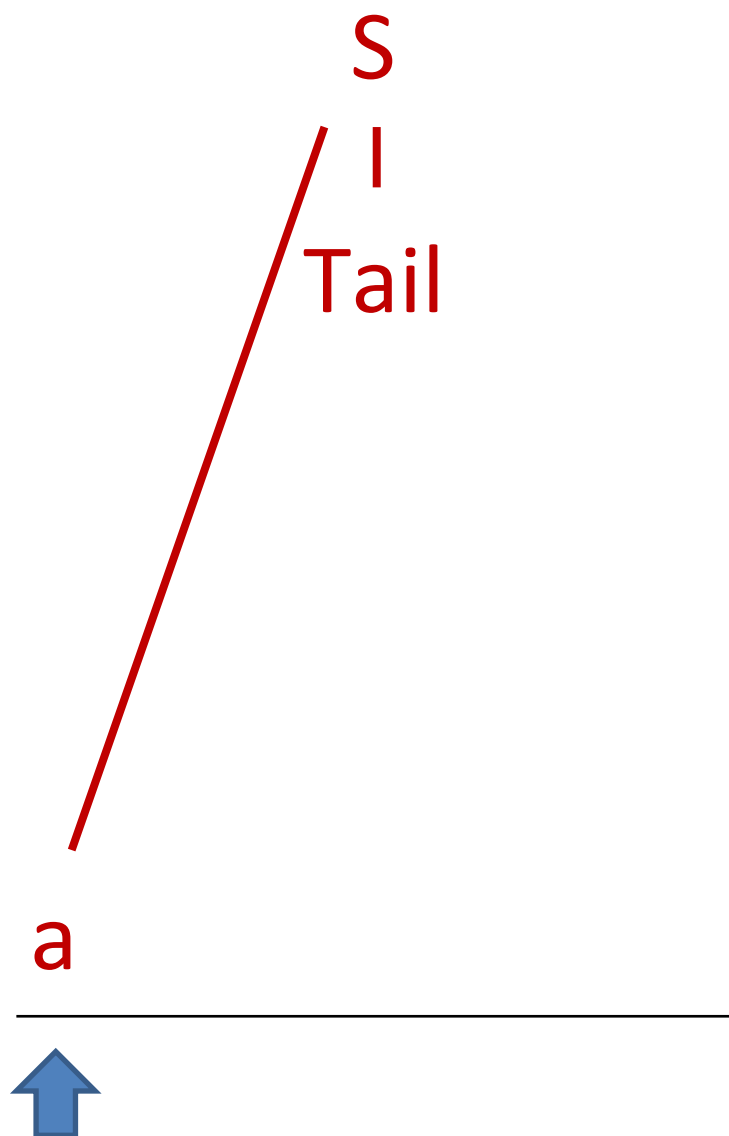
1.  $\text{Tail} ::= B \mid w$

2.  $B ::= C \ x \mid y$

3.  $C ::= \varepsilon \mid z$



# Top-Down Derivation of "a z x"



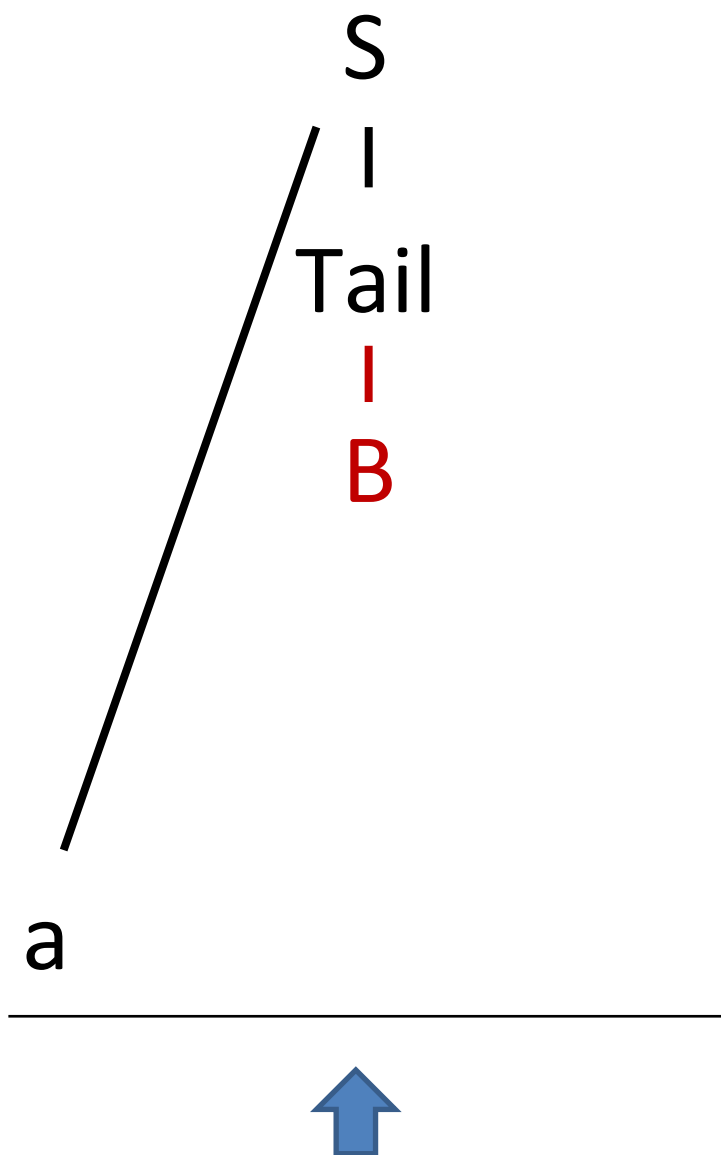
- 0. **S** ::= **a Tail**
- 1. **Tail** ::= **B | w**
- 2. **B** ::= **C x | y**
- 3. **C** ::= **ε | z**

Lookahead      Remaining

a

z x

# Top-Down Derivation of "a z x"



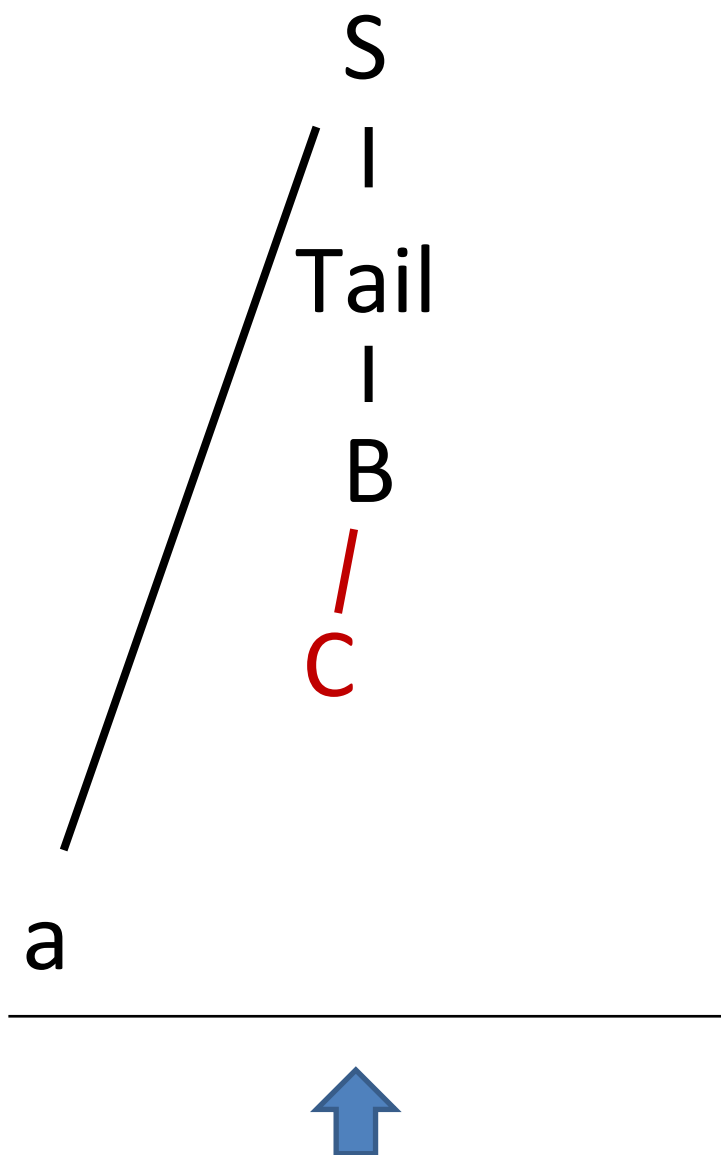
- 0. **S** ::= **a Tail**
- 1. **Tail** ::= **B | w**
- 2. **B** ::= **C x | y**
- 3. **C** ::= **ε | z**

Lookahead      Remaining

z

x

# Top-Down Derivation of "a z x"



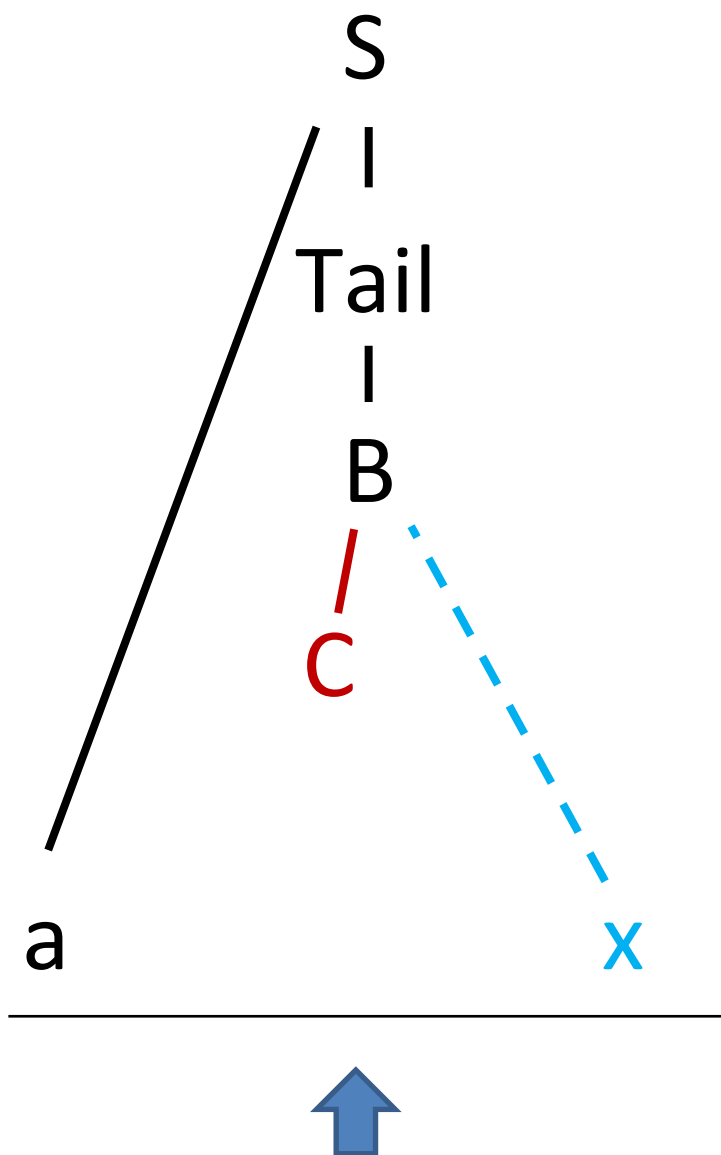
- 0. **S** ::= **a Tail**
- 1. **Tail** ::= **B | w**
- 2. **B** ::= **C x | y**
- 3. **C** ::=  $\epsilon$  | **z**

Lookahead      Remaining

z

x

# Top-Down Derivation of "a z x"



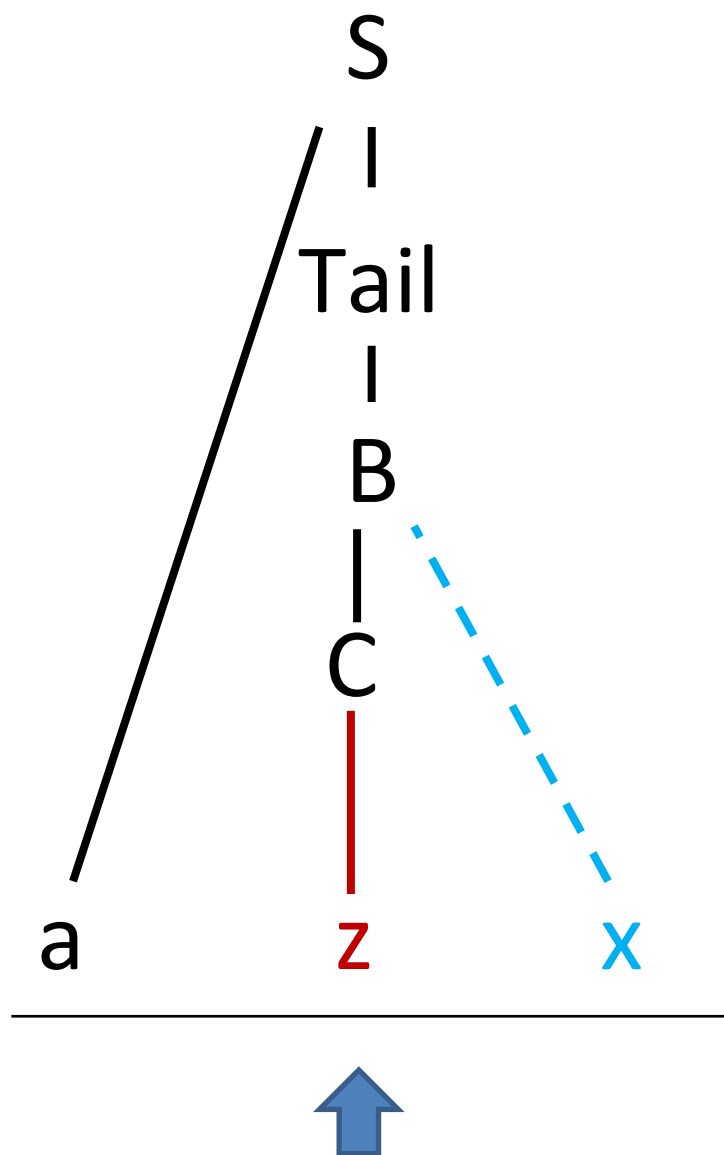
- 0.  $S ::= a \text{ Tail}$
- 1.  $\text{Tail} ::= B \mid w$
- 2.  $B ::= C \ x \mid y$
- 3.  $C ::= \varepsilon \mid z$

Lookahead      Remaining

z

x

# Top-Down Derivation of “a z x”



0. **S ::= a Tail**

1. **Tail ::= B | w**

2. **B ::= C x | y**

3. **C ::= ε | z**

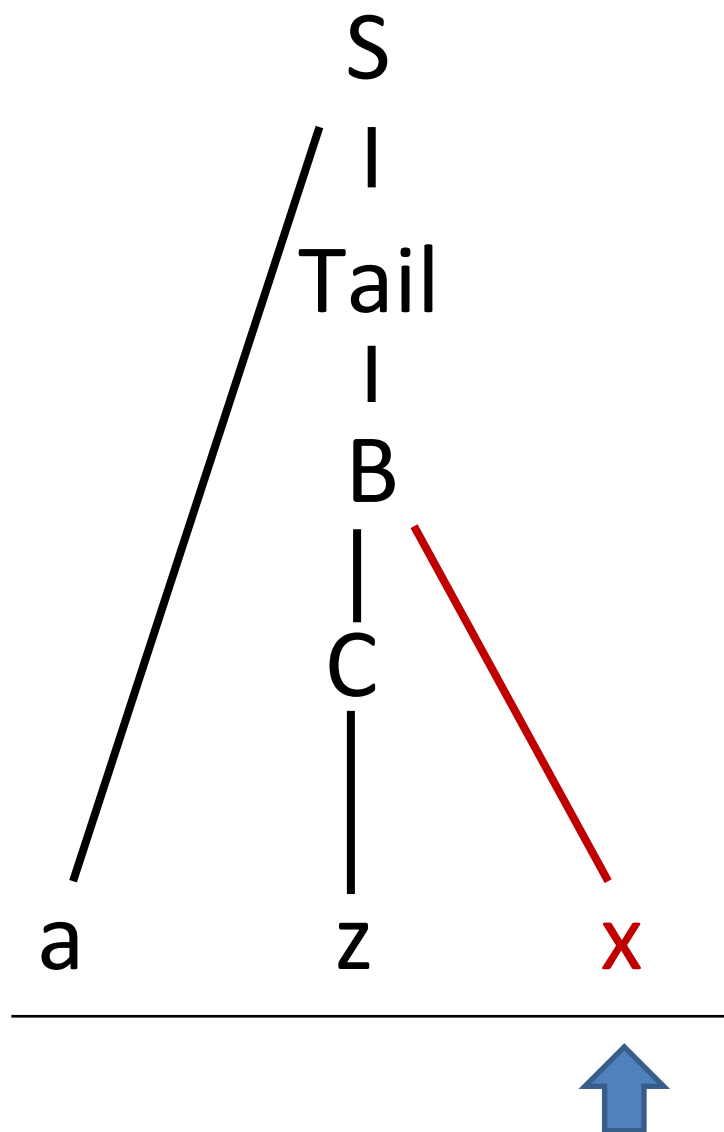
Lookahead

Remaining

z

x

# Top-Down Derivation of “a z x”



0. **S** ::= **a Tail**

1. **Tail** ::= **B | w**

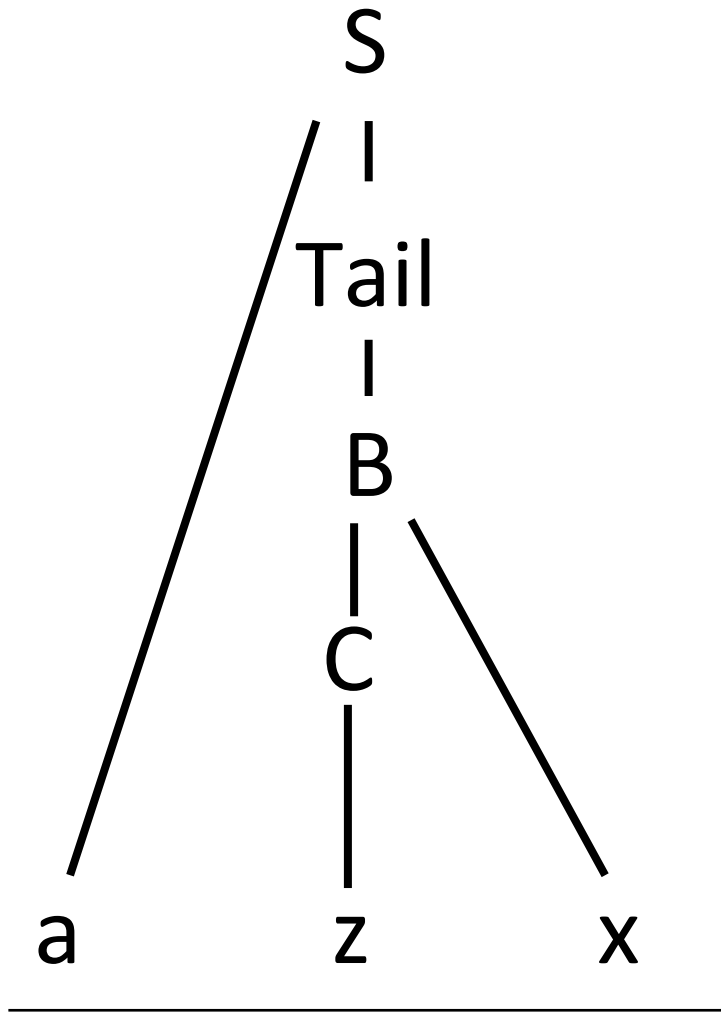
2. **B** ::= **C x | y**

3. **C** ::= **ε | z**

Lookahead      Remaining

x

# Top-Down Derivation of “a z x”



0. **S ::= a Tail**

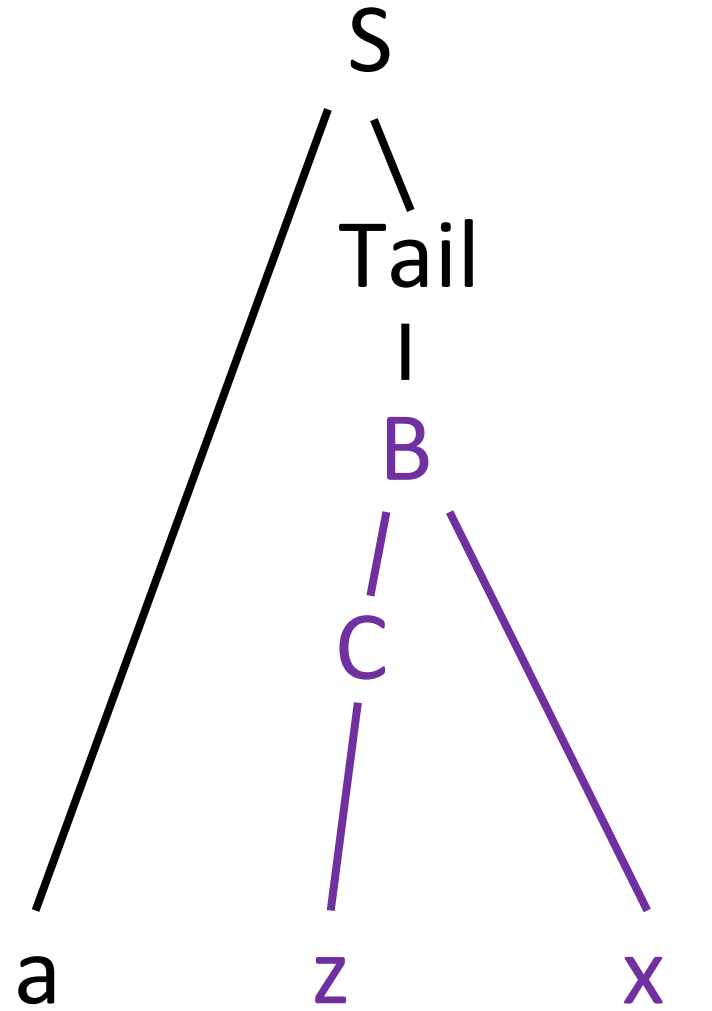
1. **Tail ::= B | w**

2. **B ::= C x | y**

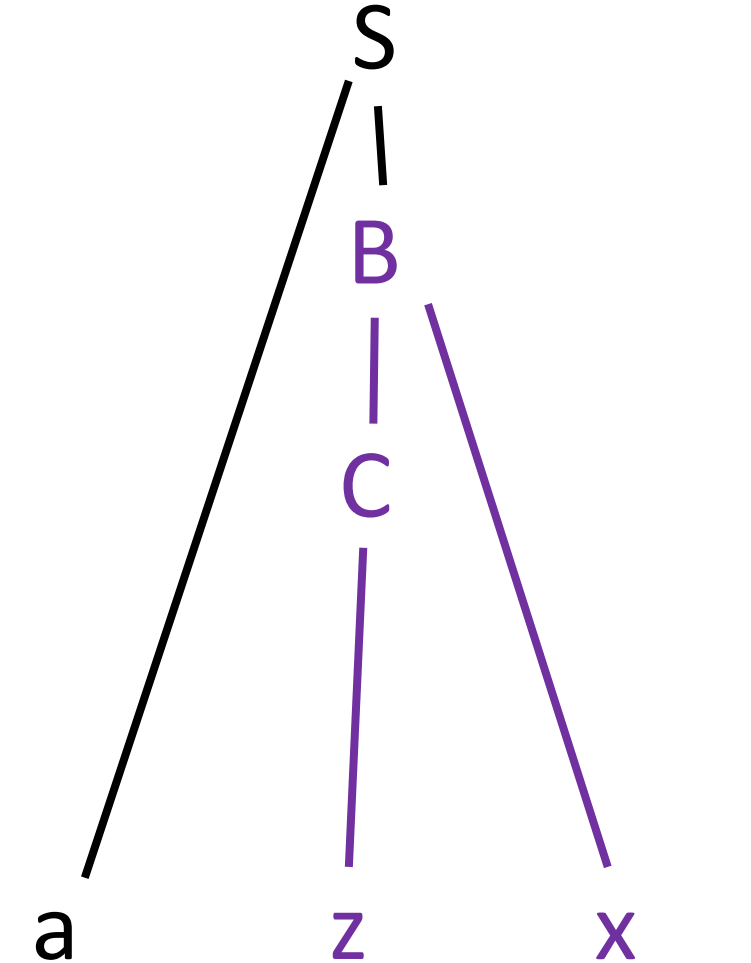
3. **C ::= ε | z**

Success!

# Comparing Parse Trees



Purple trees  
are the same!





# LL Condition

For each nonterminal in the grammar:

- Its *productions* must have disjoint FIRST sets

✗ 
$$\begin{array}{l} A ::= x \mid B \\ B ::= x \end{array}$$

✓ 
$$\begin{array}{l} A ::= x \mid B \\ B ::= y \end{array}$$

- If it is *nullable*, the FIRST sets of its productions must be disjoint from its FOLLOW set

✗ 
$$\begin{array}{l} S ::= A x \\ A ::= \varepsilon \mid x \end{array}$$

✓ 
$$\begin{array}{l} S ::= A y \\ A ::= \varepsilon \mid x \end{array}$$

**\*\***We can often transform a grammar to satisfy this if needed

# Canonical FIRST FOLLOW Conflict

## Problem

0.  $A ::= B \alpha$

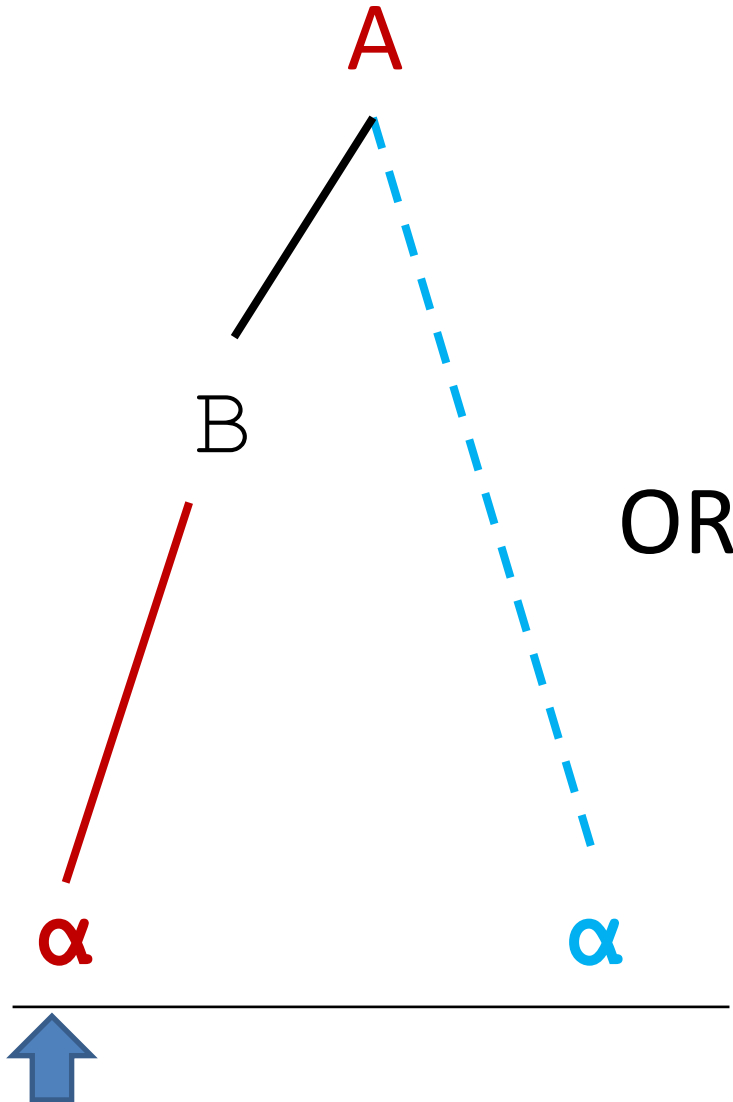
1.  $B ::= \alpha \mid \varepsilon$

Because  $B$  is nullable, its FOLLOW set must be disjoint from the FIRST sets of its right-hand sides!

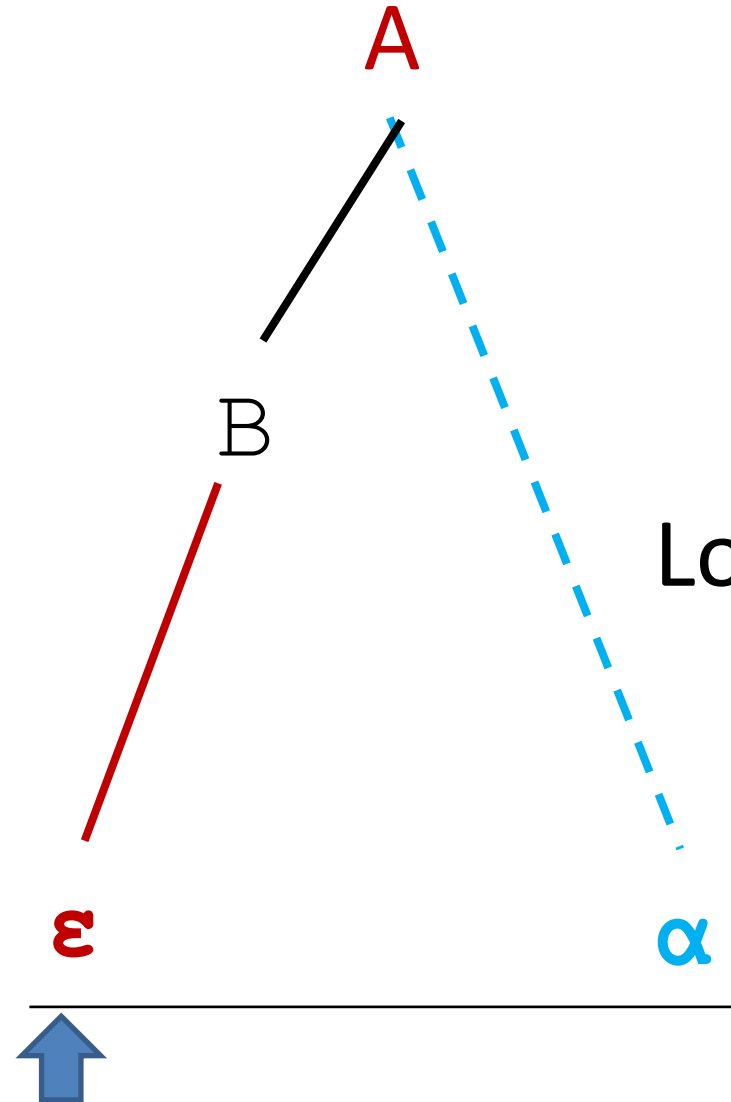
# Let's try a top-down derivation of " $\alpha$ "

0.  $A ::= B \alpha$

1.  $B ::= \alpha \mid \epsilon$



OR



Lookahead

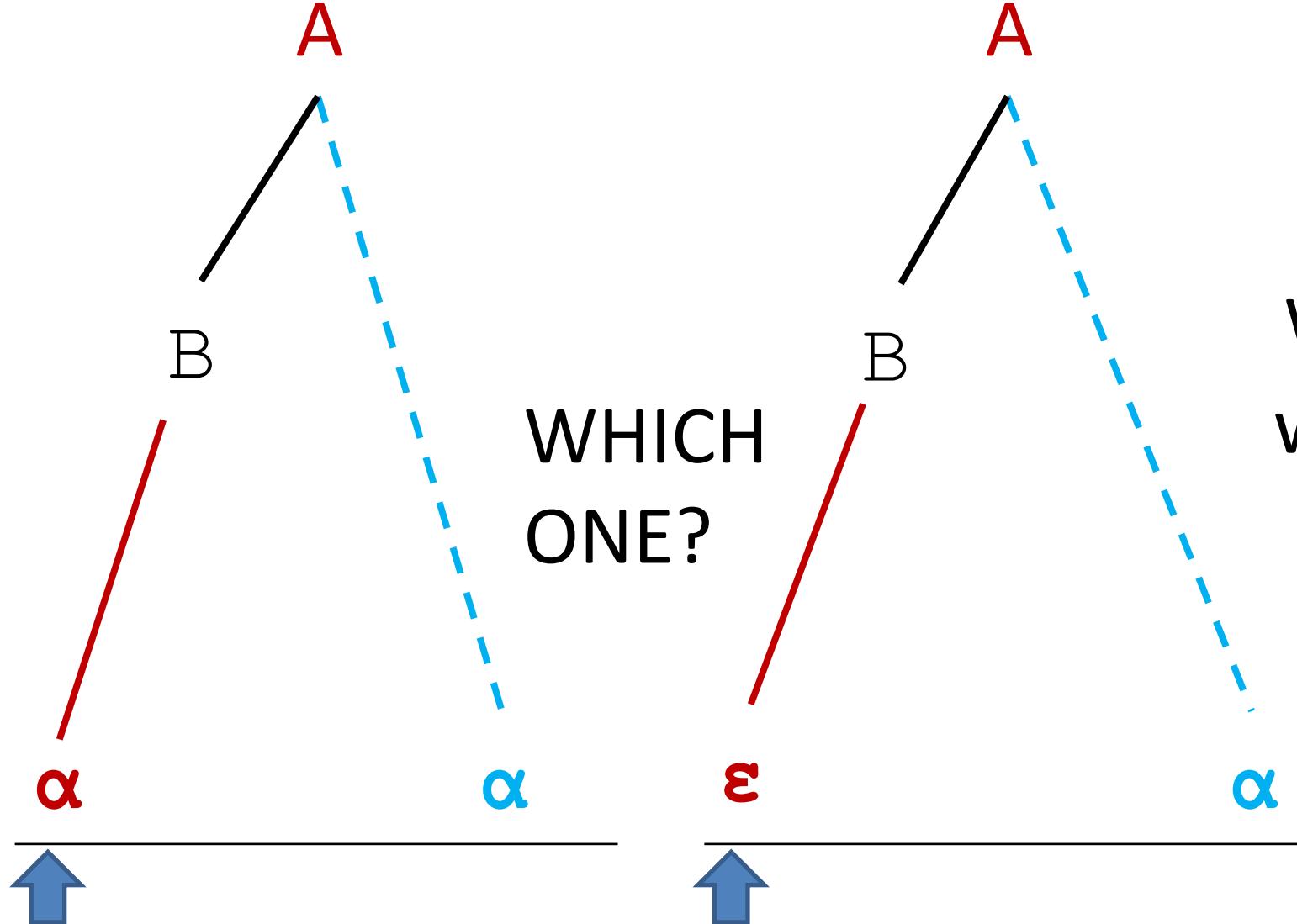
Remaining

$\alpha$

# Let's try a top-down derivation of " $\alpha$ "

0.  $A ::= B \alpha$

1.  $B ::= \alpha \mid \epsilon$



We don't know! Again,  
we can't see more than  
 $\alpha$ !

# Canonical FIRST FOLLOW Conflict Solution

## Solution

0.  $A ::= B \alpha$

1.  $B ::= \alpha \mid \varepsilon$

Substitute the  
common prefix

0.  $A ::= \alpha\alpha \mid \alpha$

0.  $A ::= \alpha \text{ Tail}$

Factor out the  
tail

1.  $\text{Tail} ::= \alpha \mid \varepsilon$

# Watch out for Nullability! (Grammar 2)

Changing the grammar again...

0.  $S ::= a B$

1.  $B ::= C x \mid y$

**2.  $C ::= \epsilon \mid x$**

Lookahead

Remaining

a

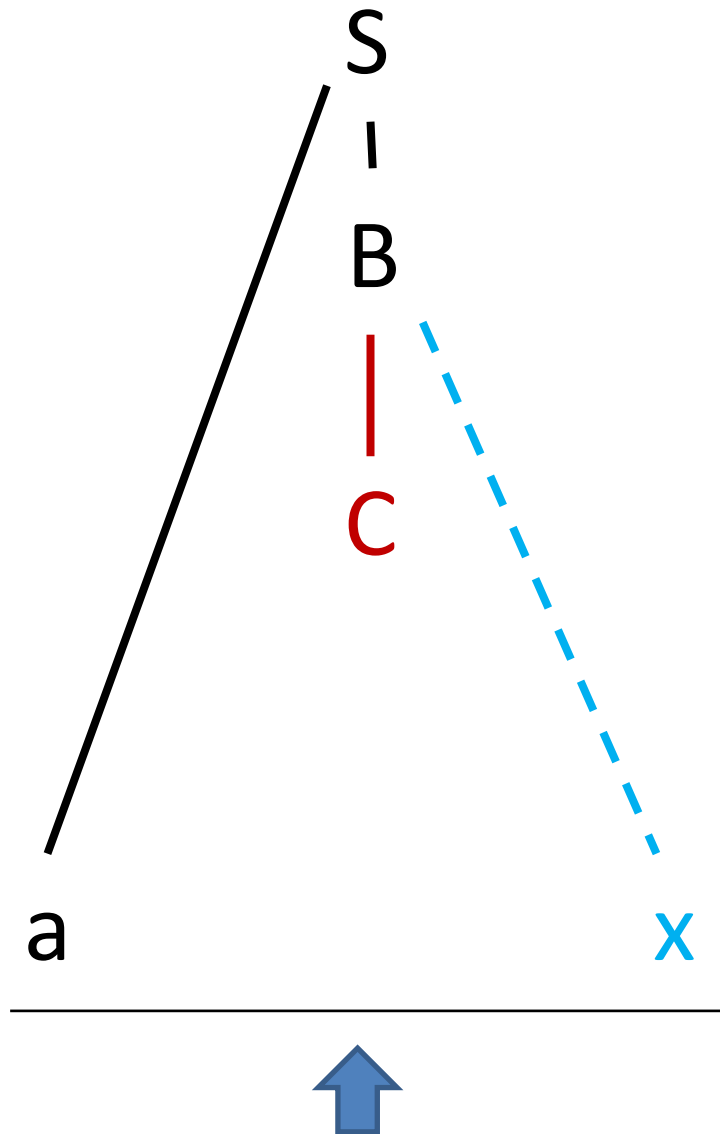
x

# What's the issue?

0.  $S ::= a B$   
1.  $B ::= C \mathbf{x} \mid y$   
2.  $C ::= \varepsilon \mid \mathbf{x}$

FIRST FOLLOW Conflict

# Top down derivation of "ax"



0.  $S ::= a B$

1.  $B ::= C x \mid y$

2.  $C ::= \epsilon \mid \mathbf{x}$

Lookahead    Remaining

$x$

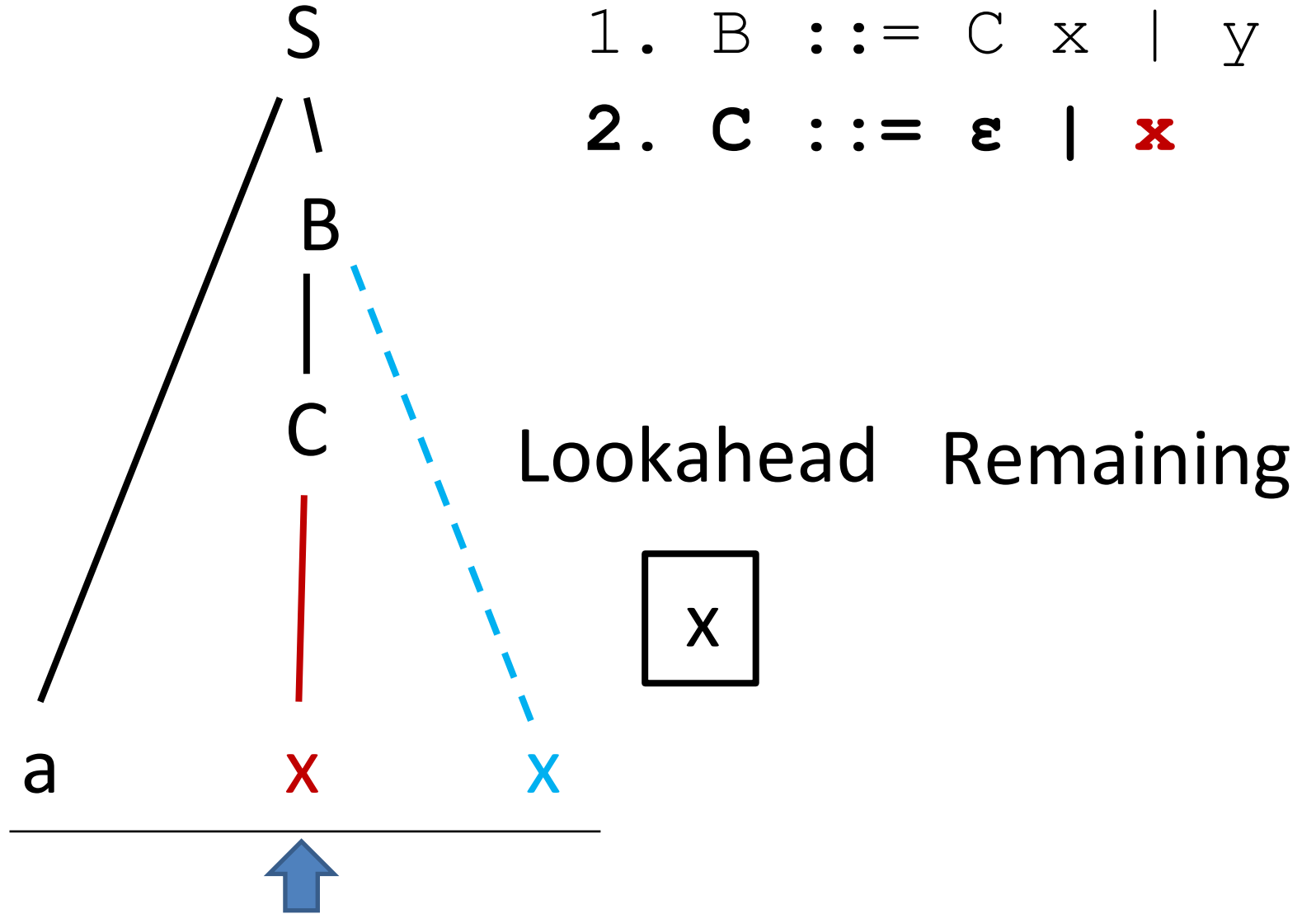
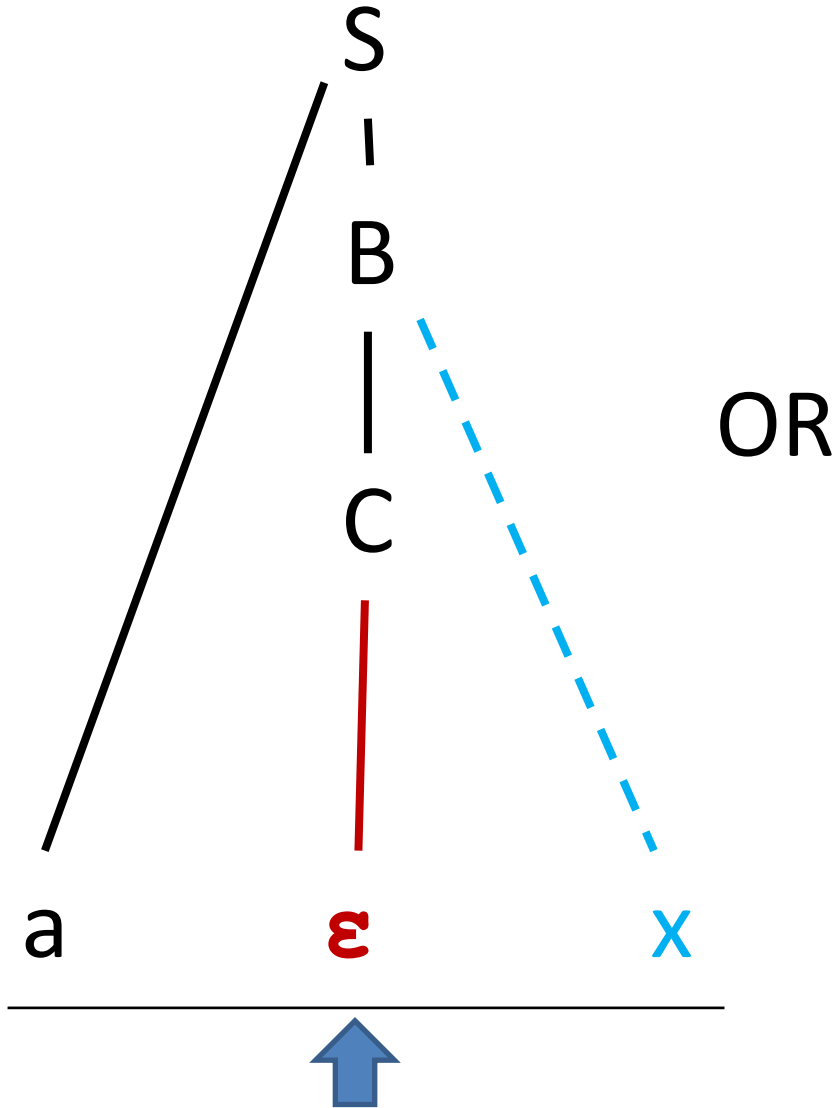


# Top down derivation of “ax”

0.  $S ::= a B$

1.  $B ::= C x \mid y$

2.  $C ::= \epsilon \mid \mathbf{x}$



# Applying the Fix: Substitute the Common Prefix,

1

0.  $S ::= a B$

1.  $B ::= \mathbf{x} \mid \mathbf{xx} \mid y$

~~2.  $C ::= \epsilon \mid x$~~

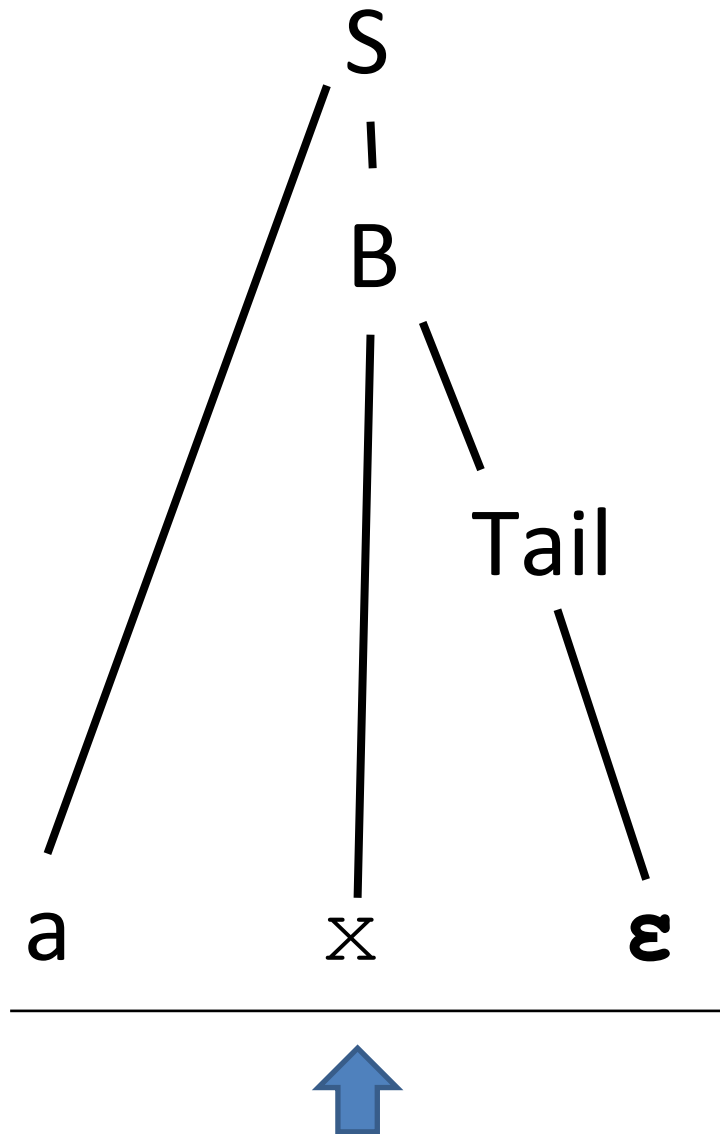
2

0.  $S ::= a B$

1.  $B ::= \mathbf{x Tail} \mid y$

2.  $Tail ::= \mathbf{x} \mid \epsilon$

# Top down derivation of "ax"



0.  $S ::= a B$

1.  $B ::= \mathbf{x Tail} \mid \mathbf{y}$

2.  $\mathbf{Tail} ::= \mathbf{x} \mid \epsilon$

Lookahead    Remaining

x