

Section 4: CUP & LL

CSE 401/M501

Adapted from Autumn 2022

Administrivia

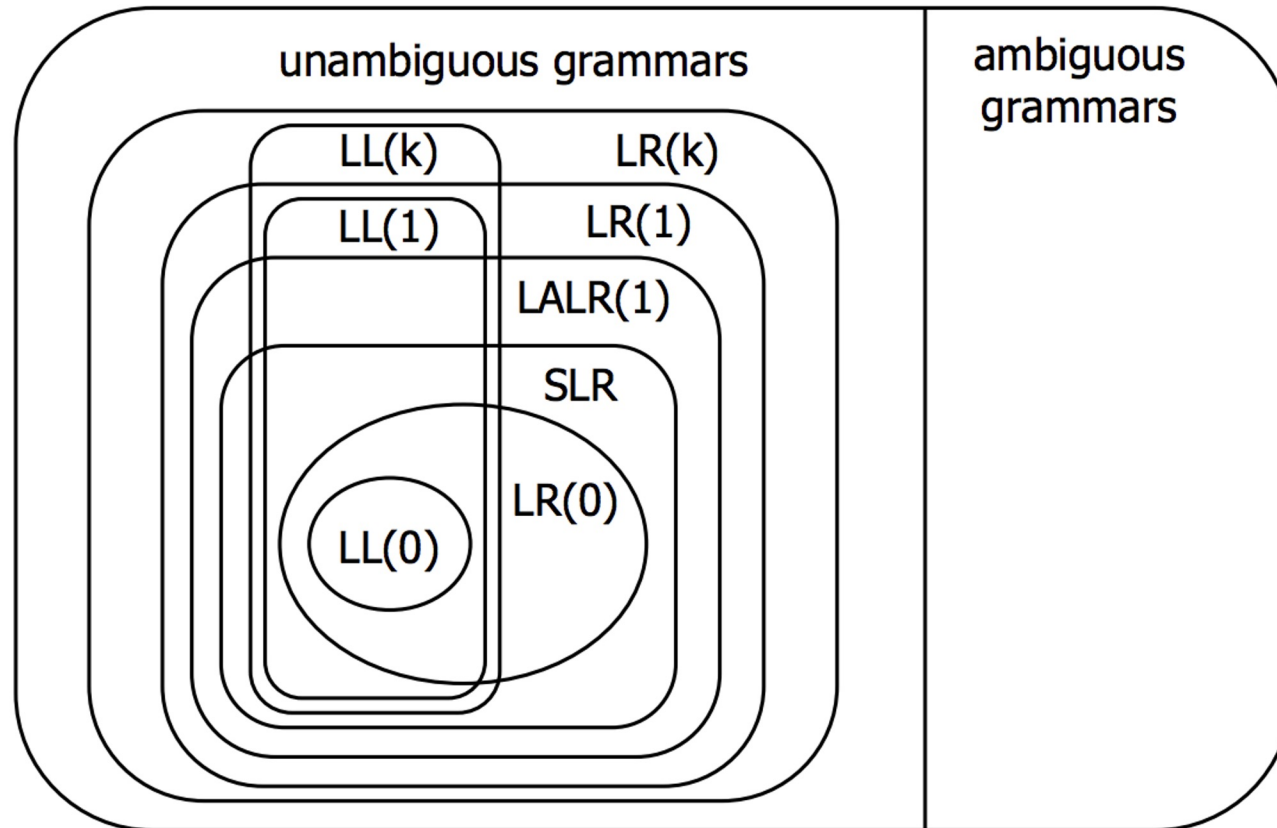
- Homework 2 is due tonight!
 - You have late days if you need them (2 max)
- Parser is due one week from today
 - Be sure to check your Scanner feedback – out later this week
- HW3 is out tomorrow, due in 1.5 weeks on *Monday April 29th*
 - **Only one late day allowed** on this assignment so we can distribute solutions before the midterm at the end of that week.
 - More on hw3 in sections next week, but start before then if you can

12:00-13:00 OH (Connor) CSE2 150	15	12:00-13:00 OH (Eric) CSE2 153	16	11:30-12:30 OH (Aragorn) CSE2 150	17	Section <i>CUP parser generator, ASTs; LL parsing</i>	18	12:00-13:00 OH (Connor) CSE2 151	19
14:30-15:20 Lecture CSE2 G10 <i>ASTs & visitors slides</i>		15:30-16:30 OH (Edward) CSE2 151		14:30-15:20 Lecture CSE2 G10 <i>LL Parsing & recursive descent (3.3)</i>		10:30-11:30 OH (Richard) CSE2 151		14:30-15:20 Lecture CSE2 G10 <i>Intro to semantics and type checking (4.1-4.2)</i>	
15:30-16:30 OH (Aragorn) CSE2 151				15:30-16:30 OH (Richard) CSE2 151		16:30-18:00 OH (Edward) CSE2 150		15:30-16:30 OH (Eric) CSE2 153	
						23:59 hw2 due (LR grammars)			
12:00-13:00 OH (Connor) CSE2 150	22	12:00-13:00 OH (Eric) CSE2 153	23	11:30-12:30 OH (Aragorn) CSE2 150	24	Section <i>LL parsing review; ASTs & semantics</i>	25	12:00-13:00 OH (Connor) CSE2 151	26
14:30-15:20 Lecture CSE2 G10 <i>Symbol tables and representation of types</i>		15:30-16:30 OH (Edward) CSE2 151		14:30-15:20 Lecture CSE2 G10 <i>Type checking / semantics wrapup</i>		10:30-11:30 OH (Richard) CSE2 151		14:30-15:20 Lecture CSE2 G10 <i>x86-64 (everything you forgot from 351)</i>	
15:30-16:30 OH (Aragorn) CSE2 151				15:30-16:30 OH (Richard) CSE2 151		16:30-18:00 OH (Edward) CSE2 150		15:30-16:30 OH (Eric) CSE2 153	
						23:59 Project: parser+AST due			
12:00-13:00 OH (Connor) CSE2 150	29	12:00-13:00 OH (Eric) CSE2 153	30	11:30-12:30 OH (Aragorn) CSE2 150	01	Section <i>Midterm review</i>	02	12:00-13:00 OH (Connor) CSE2 151	03
14:30-15:20 Lecture CSE2 G10 <i>x86-64 function calls; Code shape I - basics (start)</i>		15:30-16:30 OH (Edward) CSE2 151		14:30-15:20 Lecture CSE2 G10 <i>Code shape I (concl); Code shape II - objects and dynamic dispatch (start)</i>		10:30-11:30 OH (Richard) CSE2 151		14:30-15:20 Midterm exam	
15:30-16:30 OH (Aragorn) CSE2 151				15:30-16:30 OH (Richard) CSE2 151		16:30-18:00 OH (Edward) CSE2 150		15:30-16:30 OH (Eric) CSE2 153	
23:59 mini hw3 due (LL grammars & parsing) Only one late day max so we can discuss solutions before the midterm									

Parser Live Demo

A video recording of this demo will be posted on the website as a supplement

Language Hierarchies



The CUP parser generator

- Uses LALR(1)
 - A little weaker (less selective), but many fewer states than LR(1) parsers
 - Handles most realistic programming language grammars
 - More selective than SLR (or LR(0)) about when to do reductions, so works for more languages

The CUP parser generator

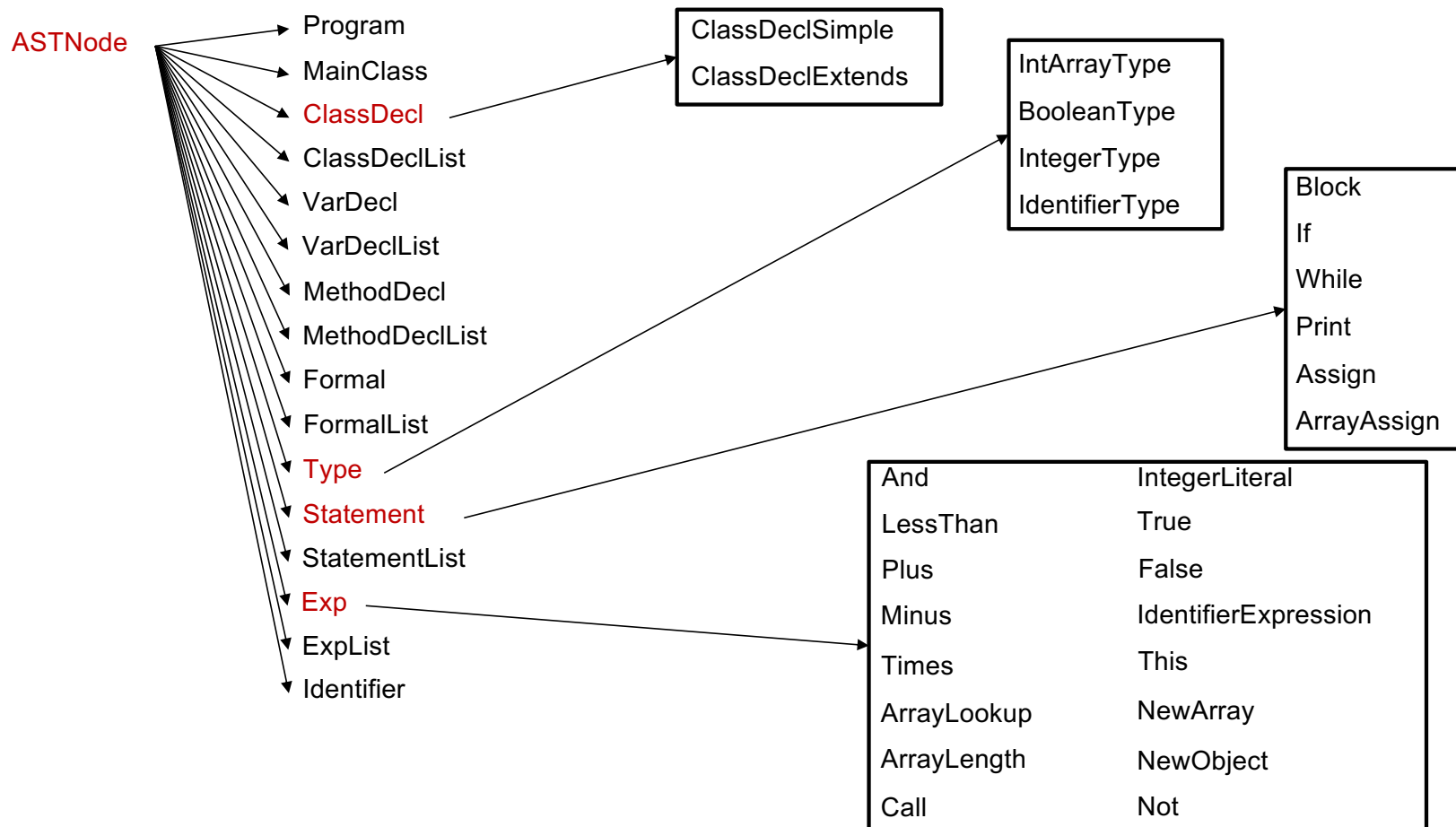
- LALR(1) parser generator based on YACC and Bison
- CUP can resolve some ambiguities itself
 - Precedence for reduce/reduce conflicts
 - Associativity for shift/reduce conflicts
 - Useful for our project for things like arithmetic expressions (use $\text{exp}+\text{exp}$, $\text{exp}*\text{exp}$, etc. for fewer non-terminals, then add precedence and associativity declarations). *Read the CUP docs!*

MiniJava BNF with AST Nodes

Use this to check your work *only after* your team has examined the grammar and AST code first.

Program	Goal ::= MainClass (ClassDeclaration)* <EOF>	
MainClass	MainClass ::= "class" Identifier "{ " "public" "static" "void" "main" "(" "String" "[" "]" Identifier ")" "{ " Statement "}" "}"	
ClassDecl	ClassDeclaration ::= "class" Identifier ("extends" Identifier)? "{ " (VarDeclaration)* (MethodDeclaration)* "}"	ClassDeclSimple ClassDeclExtends (if there is "extends")
VarDecl	VarDeclaration ::= Type Identifier ";"	Formal
MethodDecl	MethodDeclaration ::= "public" Type Identifier "(" (Type Identifier ("," Type Identifier)*)? ")" "{ " (VarDeclaration)* (Statement)* "return" Expression ";" "}"	
Type	Type ::= "int" "[" "]" "boolean" "int" Identifier	IntArrayType BooleanType IntegerType IdentifierType
Statement	Statement ::= "{ " (Statement)* "}" "if" "(" Expression ")" Statement "else" Statement "while" "(" Expression ")" Statement "System.out.println" "(" Expression ")" ";" Identifier "=" Expression ";" Identifier "[" Expression "]" "=" Expression ";"	Block If While Print Assign ArrayAssign
Exp	Expression ::= Expression ("&&" "<" "+" "-" "*") Expression Expression "[" Expression "]" Expression "." "length" Expression "." Identifier "(" (Expression ("," Expression)*)? ")" <INTEGER_LITERAL> "true" "false" Identifier "this" "new" "int" "[" Expression "]" "new" Identifier "(" " "!" Expression "(" Expression ")"	And LessThanPlus Minus Times ArrayLookup ArrayLength Call IntegerLiteral True False IdentifierExpression This NewArray NewObject Not
Identifier	Identifier ::= <IDENTIFIER>	

Abstract Syntax Tree Class Hierarchy

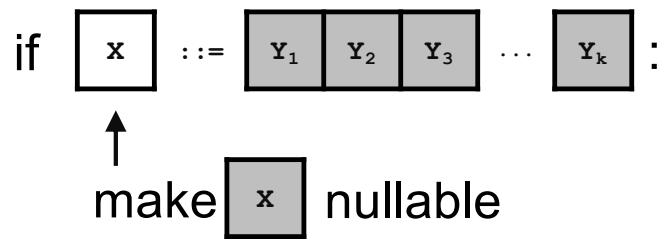


LL Parsing

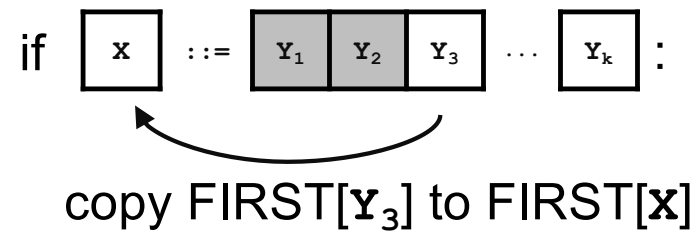
Computing FIRST, FOLLOW, & nullable (3)

\boxed{y} = nullable

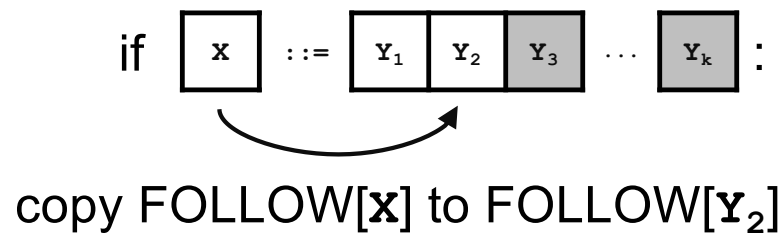
①



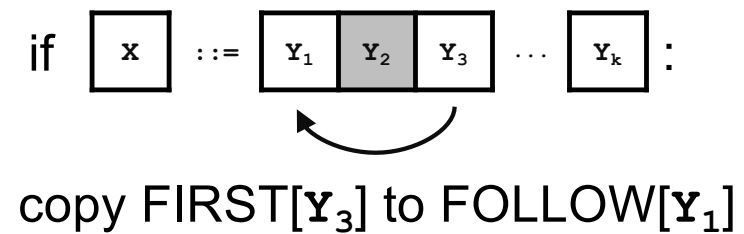
②



③



④



Computing FIRST, FOLLOW, and nullable

```
repeat
  for each production  $X := Y_1 Y_2 \dots Y_k$ 
    if  $Y_1 \dots Y_k$  are all nullable (or if  $k = 0$ )
      set nullable[X] = true
    for each  $i$  from 1 to  $k$  and each  $j$  from  $i+1$  to  $k$ 
      if  $Y_1 \dots Y_{i-1}$  are all nullable (or if  $i = 1$ )
        add FIRST[ $Y_i$ ] to FIRST[X]
      if  $Y_{i+1} \dots Y_k$  are all nullable (or if  $i = k$ )
        add FOLLOW[X] to FOLLOW[ $Y_i$ ]
      if  $Y_{i+1} \dots Y_{j-1}$  are all nullable (or if  $i+1=j$ )
        add FIRST[ $Y_j$ ] to FOLLOW[ $Y_i$ ]
Until FIRST, FOLLOW, and nullable do not change
```

L L (k)



Left-to-Right

Only takes one pass,
performed from the left

Leftmost

At each point, finds the
derivation for the leftmost
handle (**top-down**)

k Terminal Lookahead

Must determine derivation
from the next unparsed
terminal in the string
Typically $k = 1$, just like LR

LL(k) parsing

- LL(k) scans left-to-right, builds leftmost derivation, and looks ahead k symbols
- The LL condition enable the parser to choose productions correctly with 1 symbol of look-ahead
- We can often transform a grammar to satisfy this if needed

LL(1) parsing: An example top-down derivation of “a z x”

0. $S ::= a B$

1. $B ::= C x \mid y$

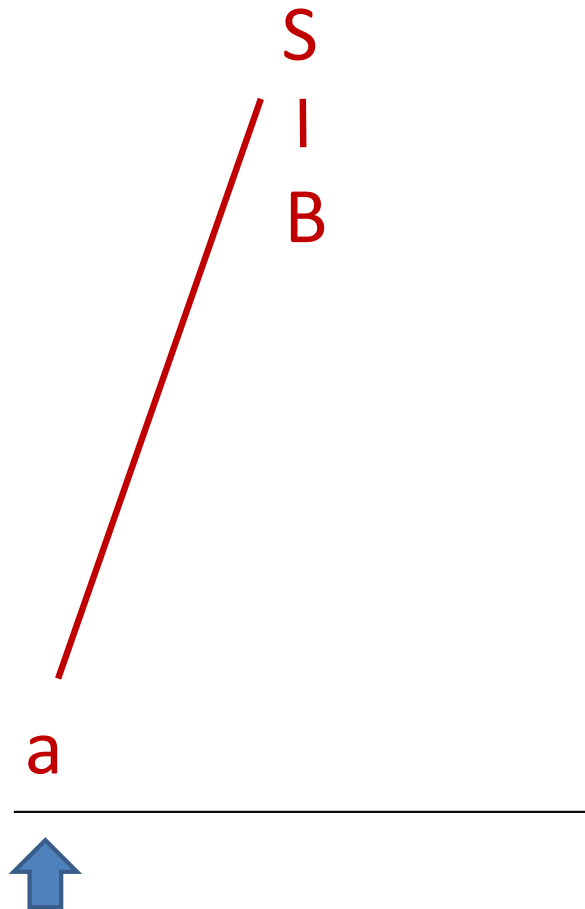
2. $C ::= \epsilon \mid z$

Lookahead Remaining

a

z x

Top-Down Derivation of "a z x"



0. $S ::= a B$

1. $B ::= C x \mid y$

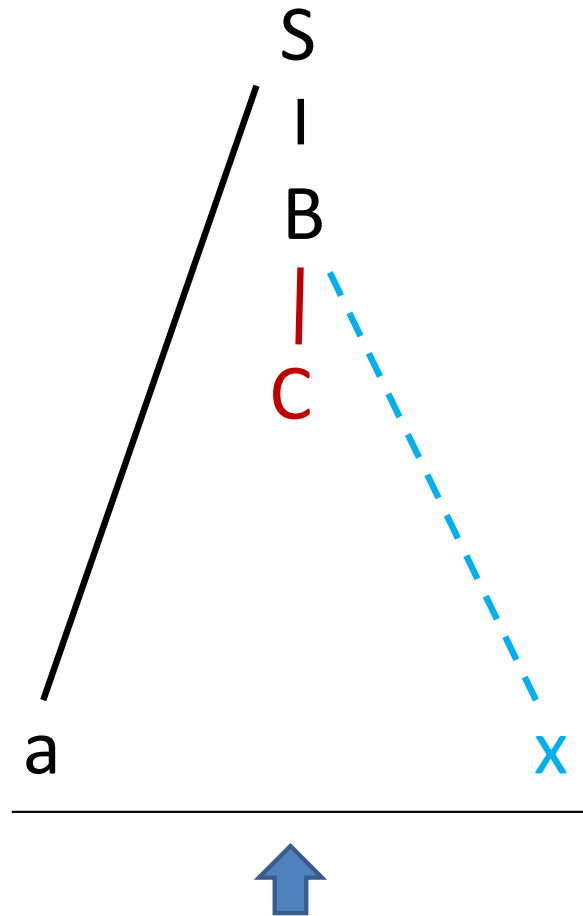
2. $C ::= \epsilon \mid z$

Lookahead Remaining

a

$z x$

Top-Down Derivation of "a z x"



0. $S ::= a B$

1. $B ::= C x \mid y$

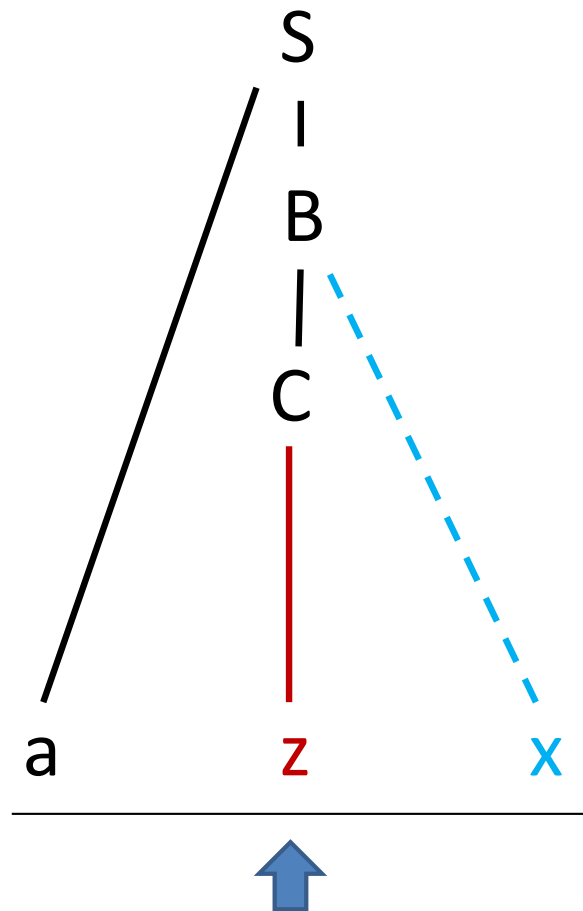
2. $C ::= \epsilon \mid z$

Lookahead Remaining

z

x

Top-Down Derivation of "a z x"



0. $S ::= a B$

1. $B ::= C x \mid y$

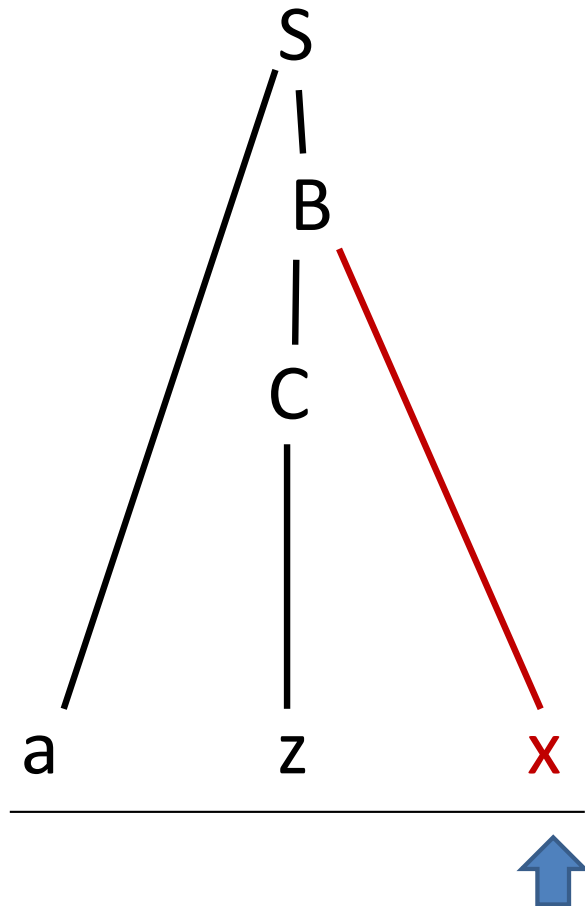
2. $C ::= \epsilon \mid z$

Lookahead Remaining

z

x

Top-Down Derivation of "a z x"



0. $S ::= a B$

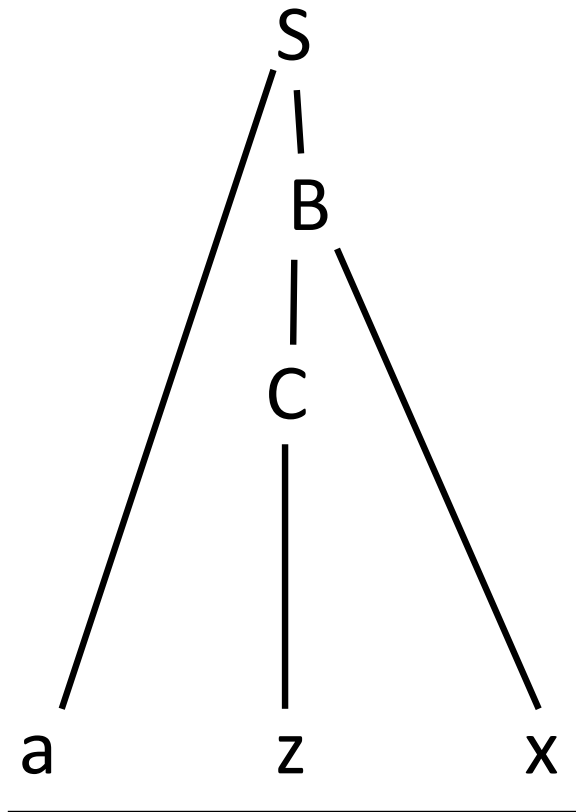
1. $B ::= C x \mid y$

2. $C ::= \epsilon \mid z$

Lookahead Remaining

x

Top-Down Derivation of "a z x"



0. **S ::= a B**

1. **B ::= C x | y**

2. **C ::= ε | z**

Successful parse!

LL Condition

For each nonterminal in the grammar:

- Its *productions* must have disjoint FIRST sets

✗ $A ::= x \mid B$
 $B ::= x$

✓ $A ::= x \mid B$
 $B ::= y$

- If it is *nullable*, the FIRST sets of its productions must be disjoint from its FOLLOW set

✗ $S ::= A x$
 $A ::= \varepsilon \mid x$

✓ $S ::= A y$
 $A ::= \varepsilon \mid x$

**We can often transform a grammar to satisfy this if needed

Canonical FIRST Conflict

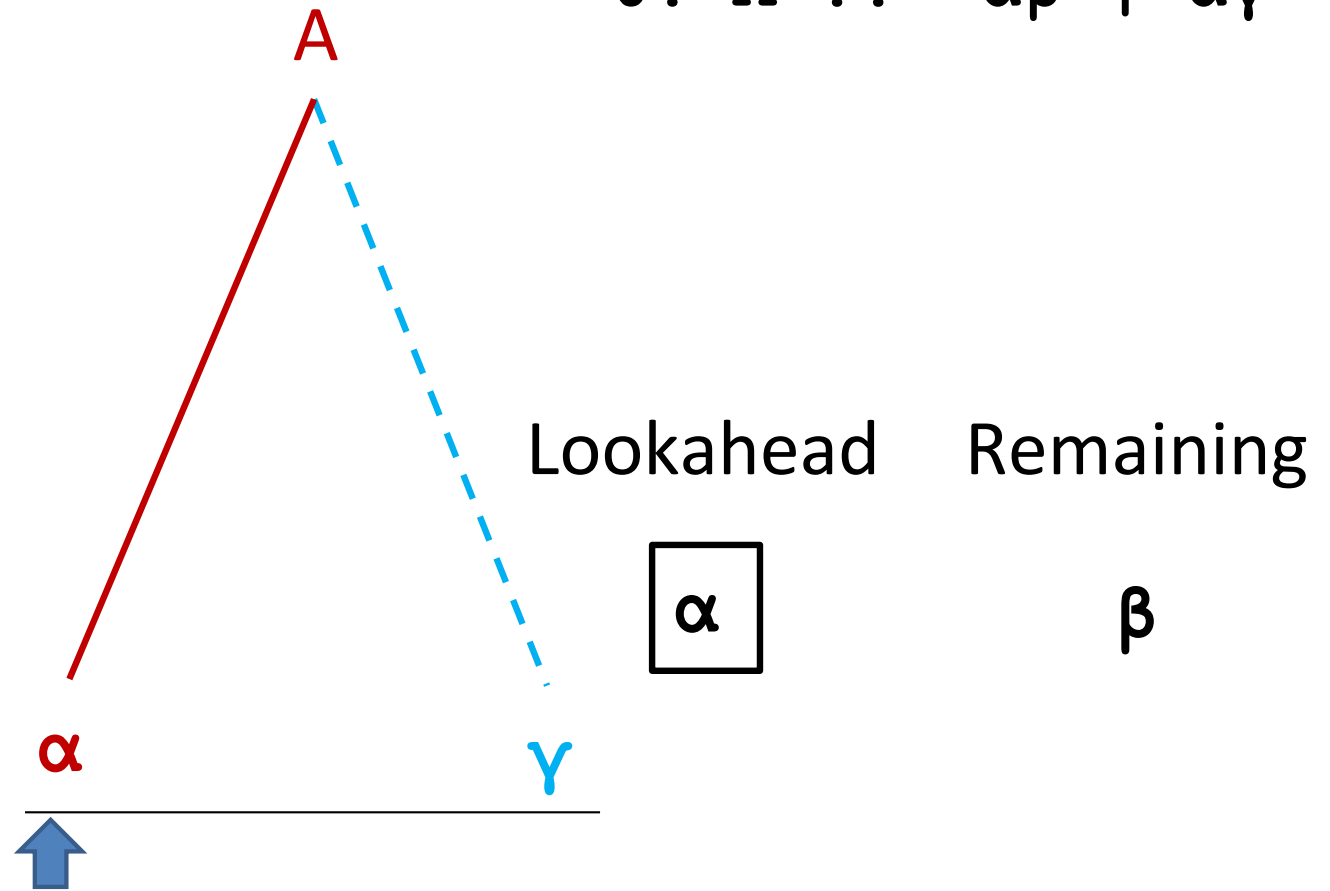
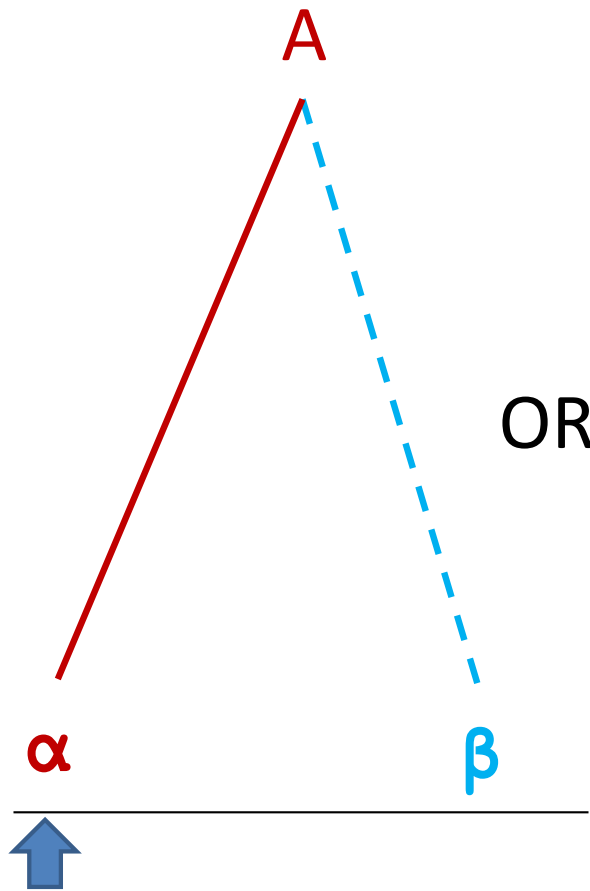
Problem

$$0. \mathbf{A} ::= \alpha\beta \mid \alpha\gamma$$

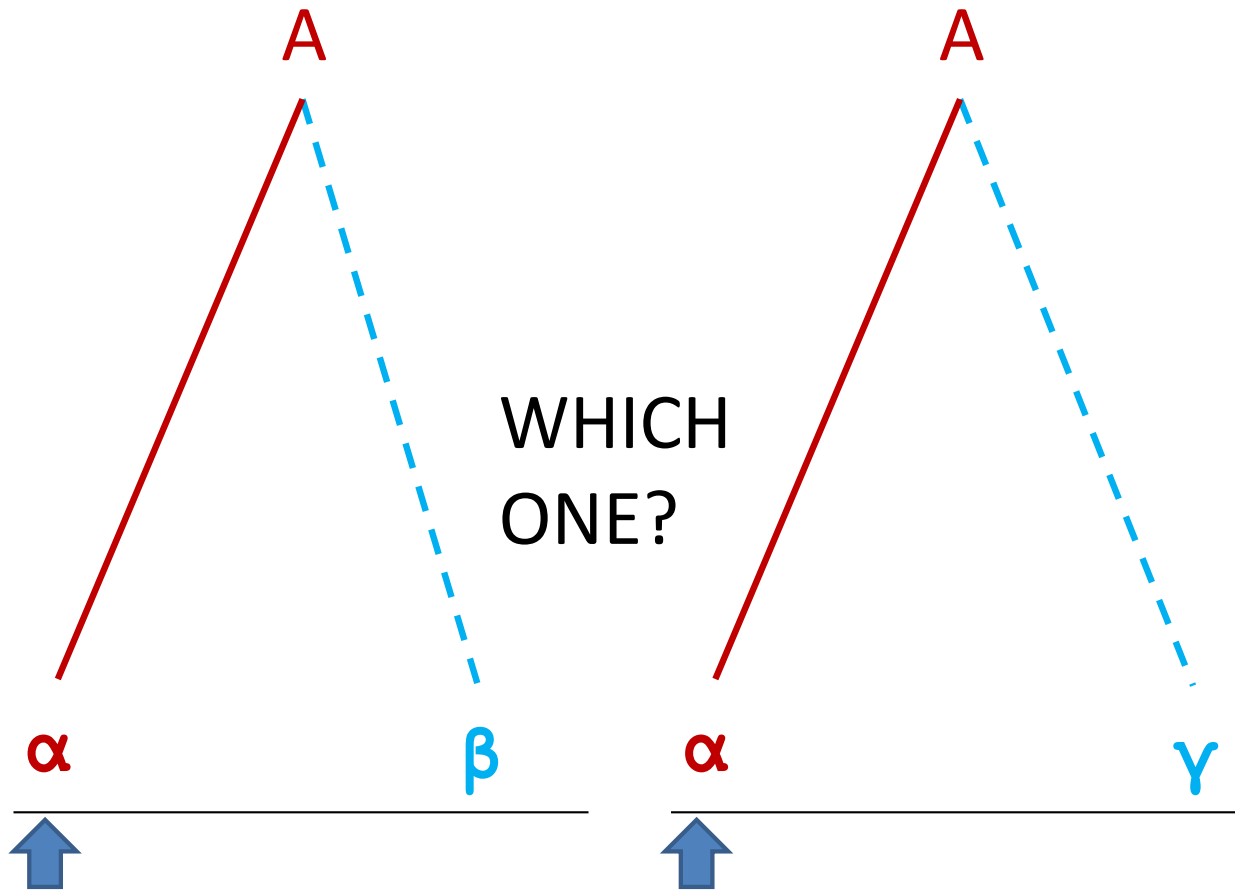
The FIRST sets of the right-hand sides for the SAME NON-TERMINAL must be disjoint!

Let's try a top-down derivation of $\alpha\beta$

0. $A ::= \alpha\beta \mid \alpha\gamma$



Let's try a top-down derivation of $\alpha\beta$



0. $A ::= \alpha\beta \mid \alpha\gamma$

We don't know!

We are using an LL(1) parser, we can't see more than α !

Canonical FIRST Conflict Solution

Solution

0. $A ::= \alpha\beta \mid \alpha\gamma$

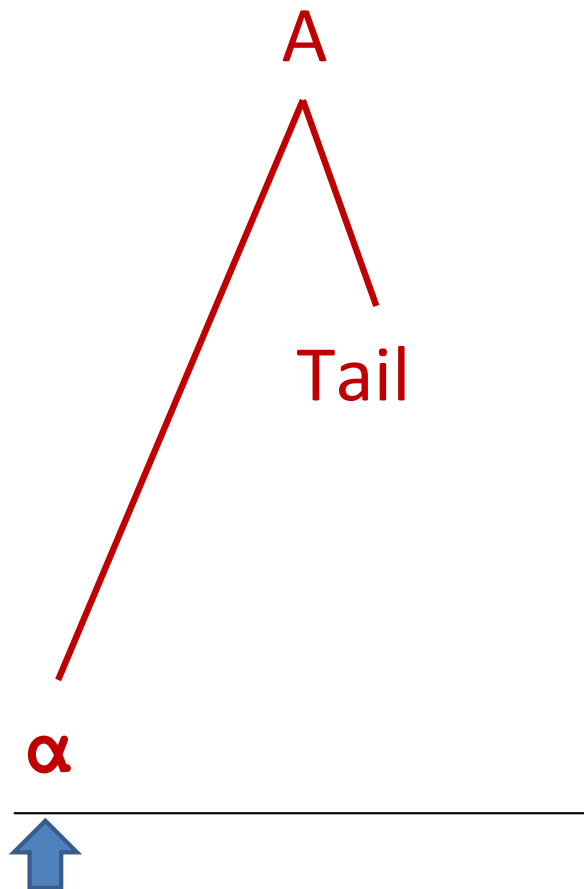
0. $A ::= \alpha \text{Tail}$

1. $\text{Tail} ::= \beta \mid \gamma$

Factor out the
common prefix

When multiple productions of a nonterminal share a common prefix, turn the different suffixes into a new nonterminal.

Top-Down Derivation of “ $\alpha\beta$ ”



0. $A ::= \alpha \text{ Tail}$

1. $\text{Tail} ::= \beta \mid \gamma$

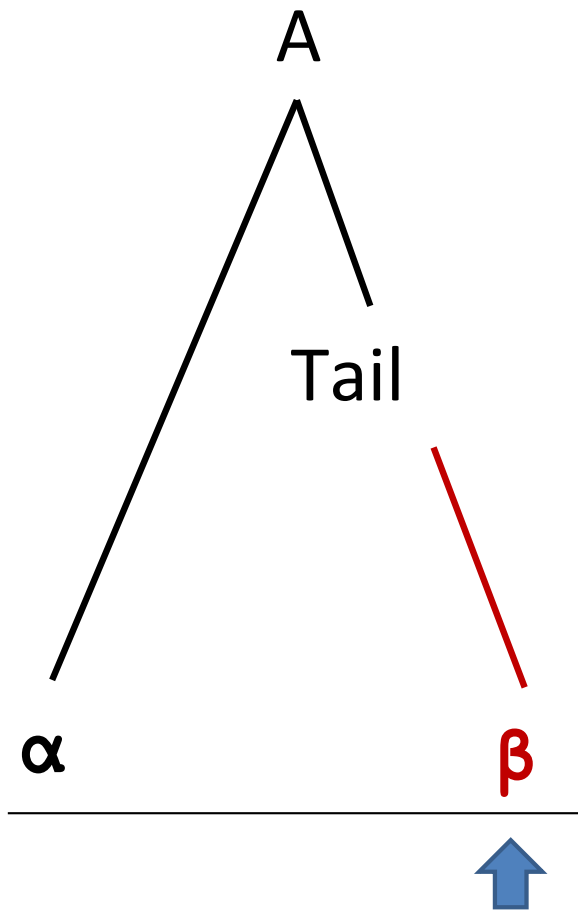
Lookahead

Remaining

α

β

Top-Down Derivation of “ $\alpha\beta$ ”



0. $A ::= \alpha \text{ Tail}$

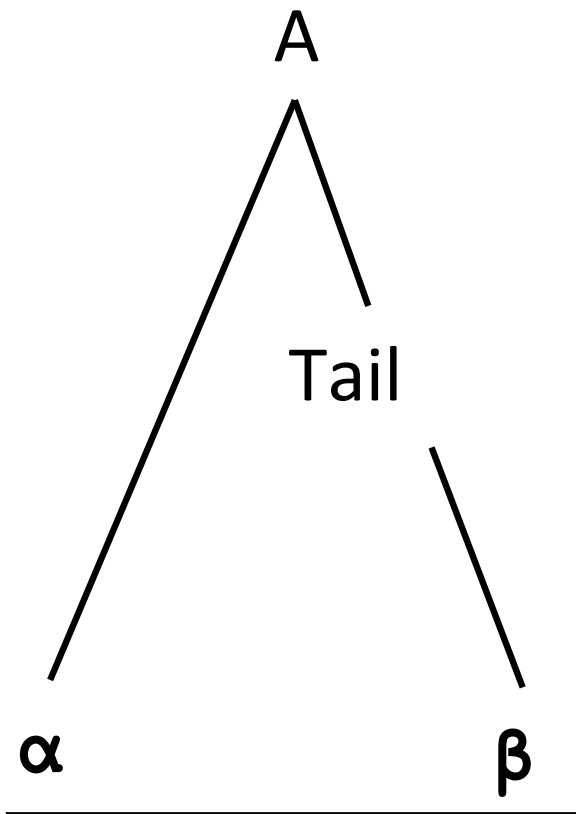
1. $\text{Tail} ::= \beta \mid \gamma$

Lookahead

Remaining

β

Top-Down Derivation of “ $\alpha\beta$ ”



0. $A ::= \alpha Tail$

1. $Tail ::= \beta \mid \gamma$

Successful parse!

Changing original grammar a little (Grammar 1)

0. $S ::= a B \mid a w$

1. $B ::= C x \mid y$

2. $C ::= \varepsilon \mid z$

Lookahead Remaining

a

z x

What's the issue?

0. $S ::= \mathbf{a} B \mid \mathbf{a} w$
1. $B ::= C x \mid y$
2. $C ::= \varepsilon \mid z$

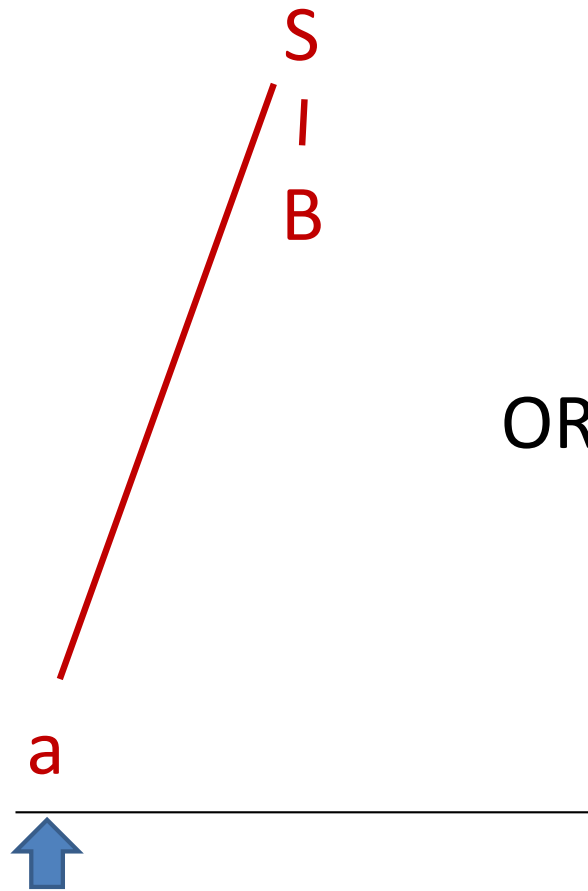
There's a FIRST Conflict!

Top-Down Derivation of "a z x": LL(1) can't parse

0. $S ::= a B \mid a w$

1. $B ::= C x \mid y$

2. $C ::= \epsilon \mid z$



OR



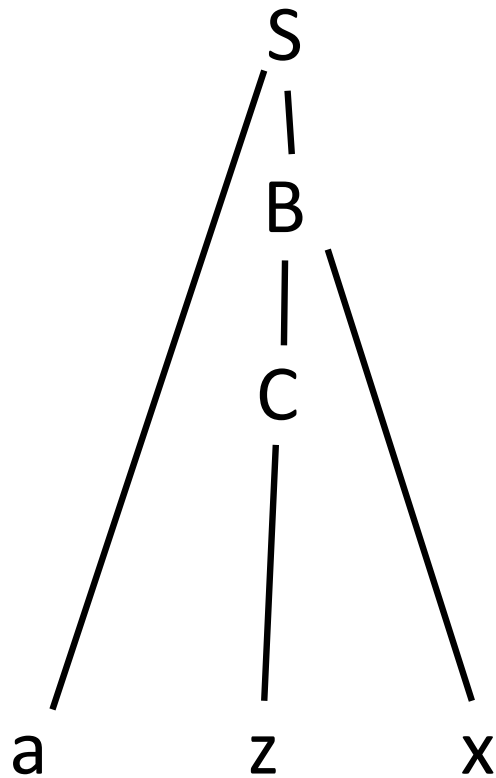
Lookahead

a

Remaining

z x

Parse Tree without changing Grammar



0. $S ::= a B \mid a w$

1. $B ::= C x \mid y$

2. $C ::= \varepsilon \mid z$

Applying the Fix: Factor out the Common Prefix

0. **S ::= a Tail**

1. **Tail ::= B | w**

2. B ::= C x | y

3. C ::= ε | z

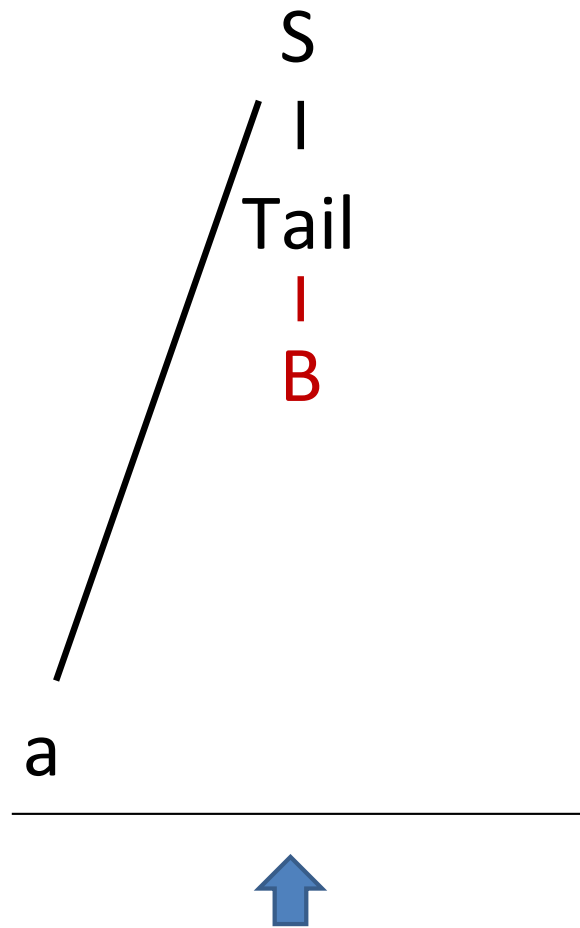
Top-Down Derivation of "a z x"



0. **S ::= a Tail**
1. **Tail ::= B | w**
2. **B ::= C x | y**
3. **C ::= ε | z**

Lookahead	Remaining
a	z x

Top-Down Derivation of "a z x"



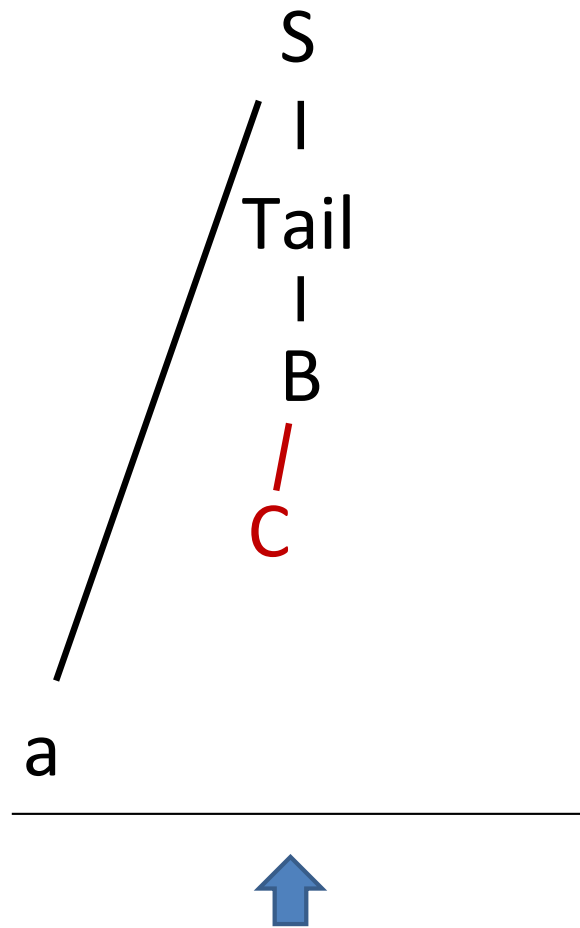
0. $S ::= a \text{ Tail}$
1. $\text{Tail} ::= B \mid w$
2. $B ::= C \ x \mid y$
3. $C ::= \varepsilon \mid z$

Lookahead Remaining

z

x

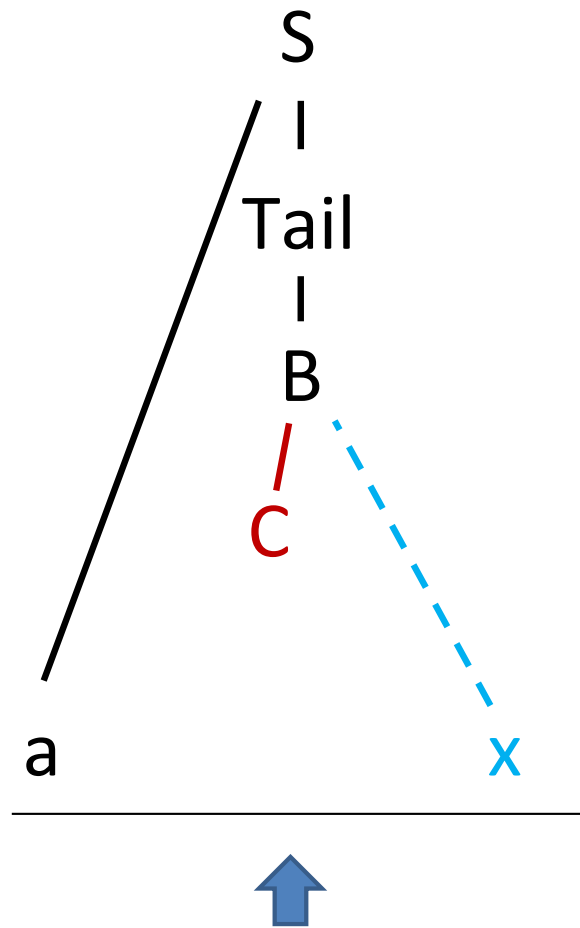
Top-Down Derivation of "a z x"



0. $S ::= a \text{ Tail}$
1. $\text{Tail} ::= B \mid w$
2. $B ::= C \ x \mid y$
3. $C ::= \varepsilon \mid z$

Lookahead	Remaining
z	x

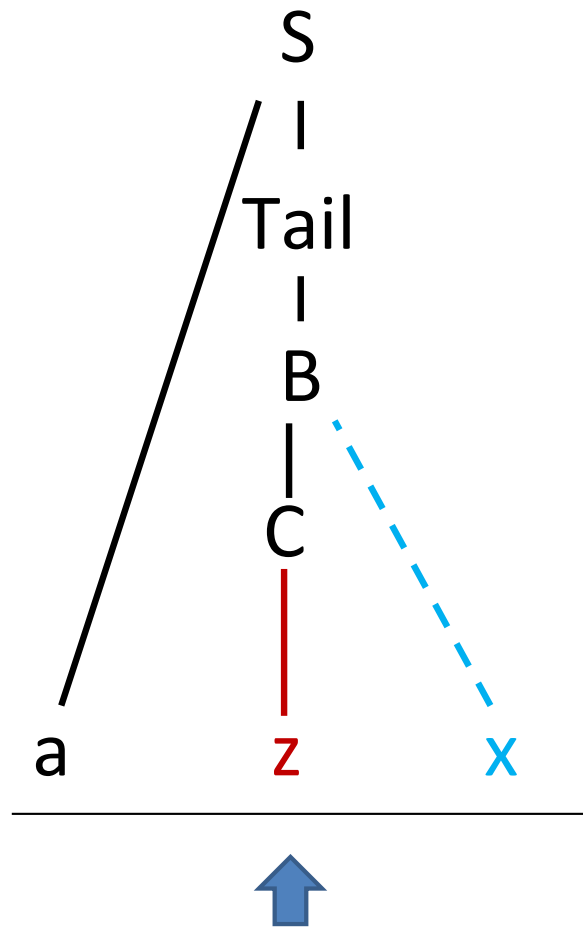
Top-Down Derivation of "a z x"



0. $S ::= a \text{ Tail}$
1. $Tail ::= B \mid w$
2. $B ::= C \ x \mid y$
3. $C ::= \varepsilon \mid z$

Lookahead	Remaining
z	x

Top-Down Derivation of "a z x"



0. $S ::= a \text{ Tail}$

1. $\text{Tail} ::= B \mid w$

2. $B ::= C \ x \mid y$

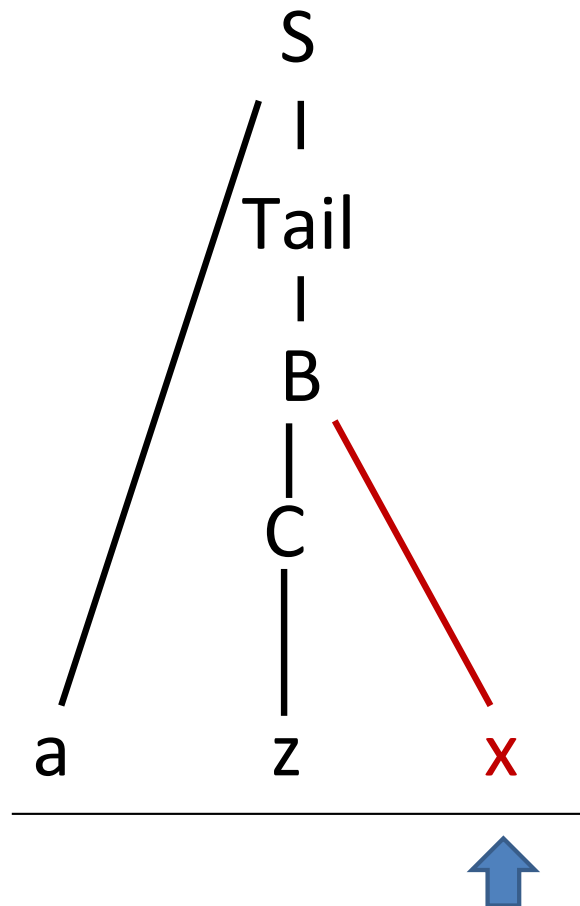
3. $C ::= \varepsilon \mid z$

Lookahead Remaining

z

x

Top-Down Derivation of "a z x"



0. $S ::= a \text{ Tail}$

1. $\text{Tail} ::= B \mid w$

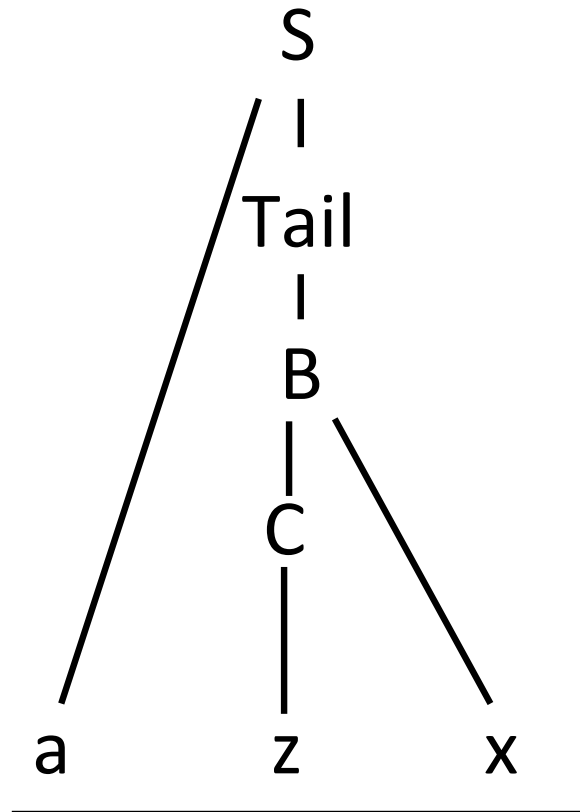
2. $B ::= C \ x \mid y$

3. $C ::= \varepsilon \mid z$

Lookahead Remaining

x

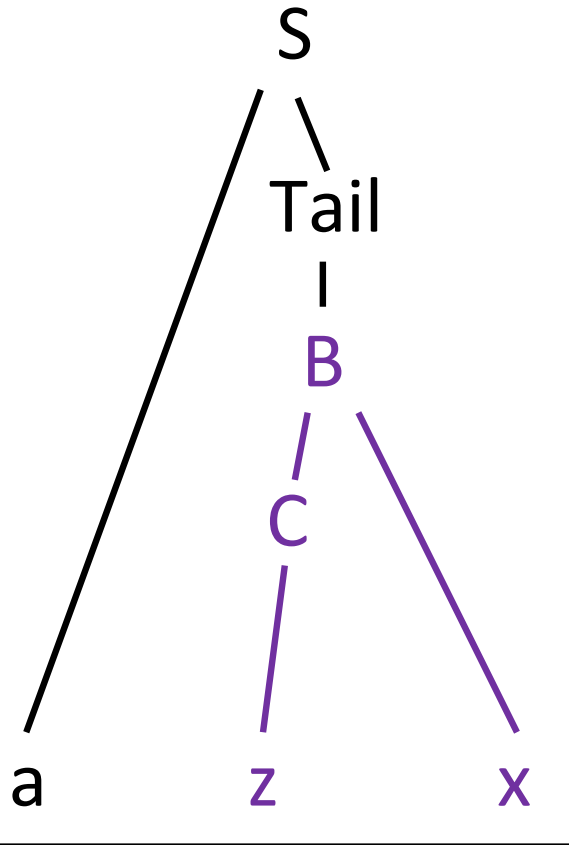
Top-Down Derivation of "a z x"



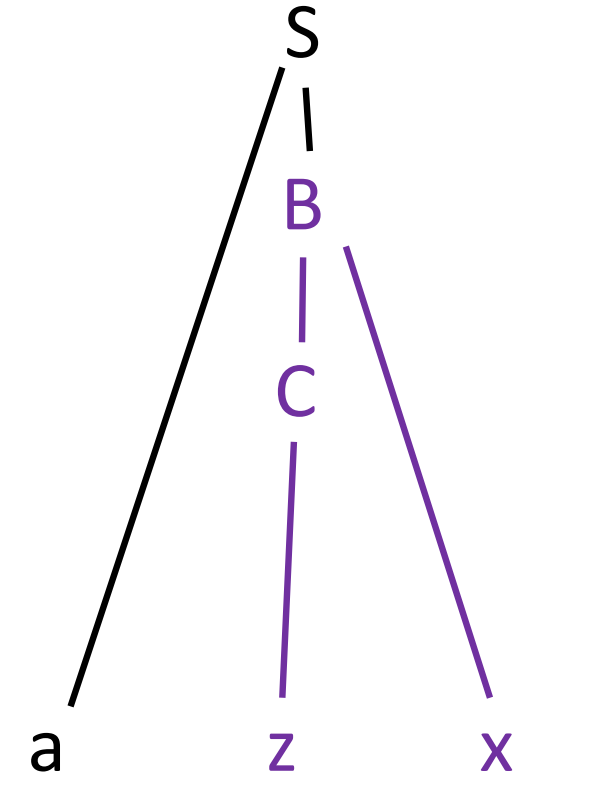
0. **S ::= a Tail**
1. **Tail ::= B | w**
2. **B ::= C x | y**
3. **C ::= ε | z**

Success!

Comparing Parse Trees



Purple trees
are the same!



LL Condition

For each nonterminal in the grammar:

- Its *productions* must have disjoint FIRST sets

✗ $A ::= x \mid B$
 $B ::= x$

✓ $A ::= x \mid B$
 $B ::= y$

- If it is *nullable*, the FIRST sets of its productions must be disjoint from its FOLLOW set

✗ $S ::= A x$
 $A ::= \varepsilon \mid x$

✓ $S ::= A y$
 $A ::= \varepsilon \mid x$

**We can often transform a grammar to satisfy this if needed

Canonical FIRST FOLLOW Conflict

Problem

0. $A ::= B \alpha$

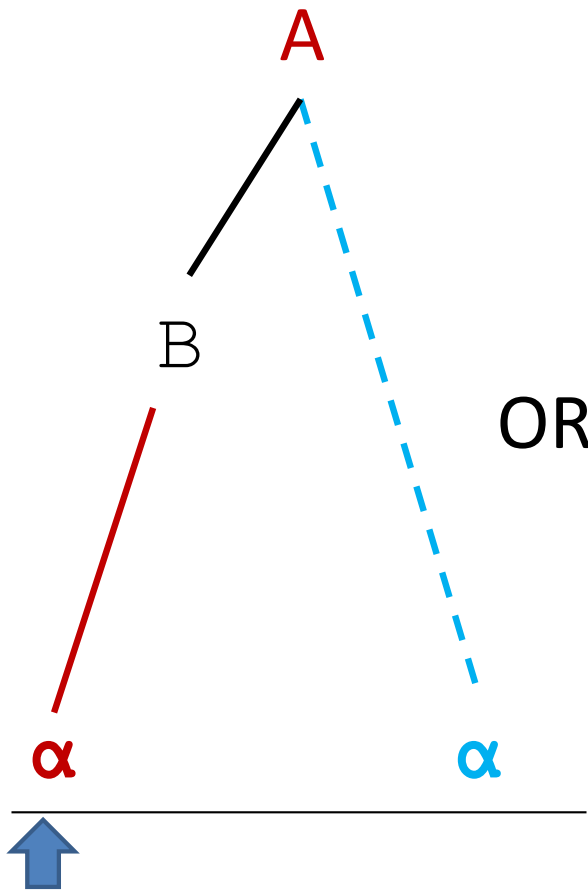
1. $B ::= \alpha \mid \epsilon$

Because B is nullable, its FOLLOW set must be disjoint from the FIRST sets of its right-hand sides!

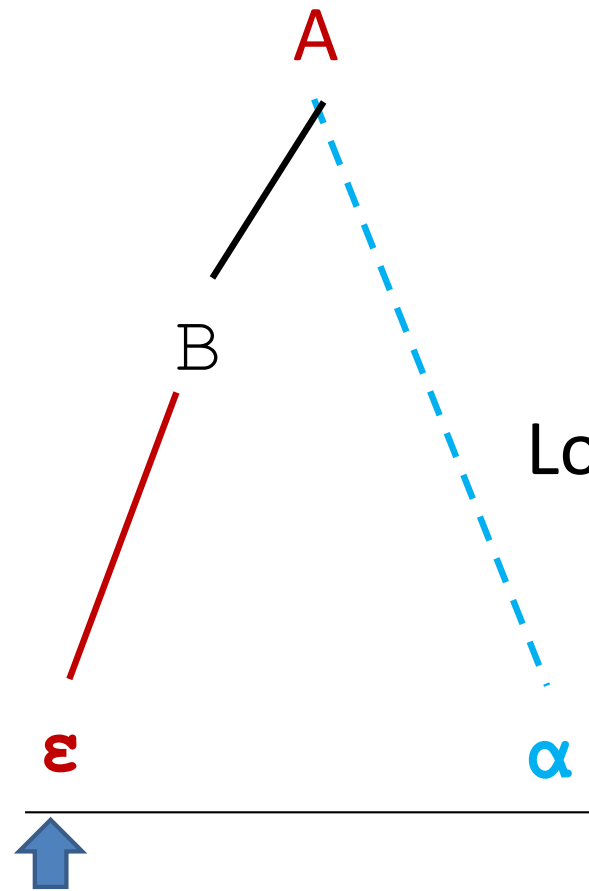
Let's try a top-down derivation of " α "

0. $A ::= B \alpha$

1. $B ::= \alpha \mid \epsilon$



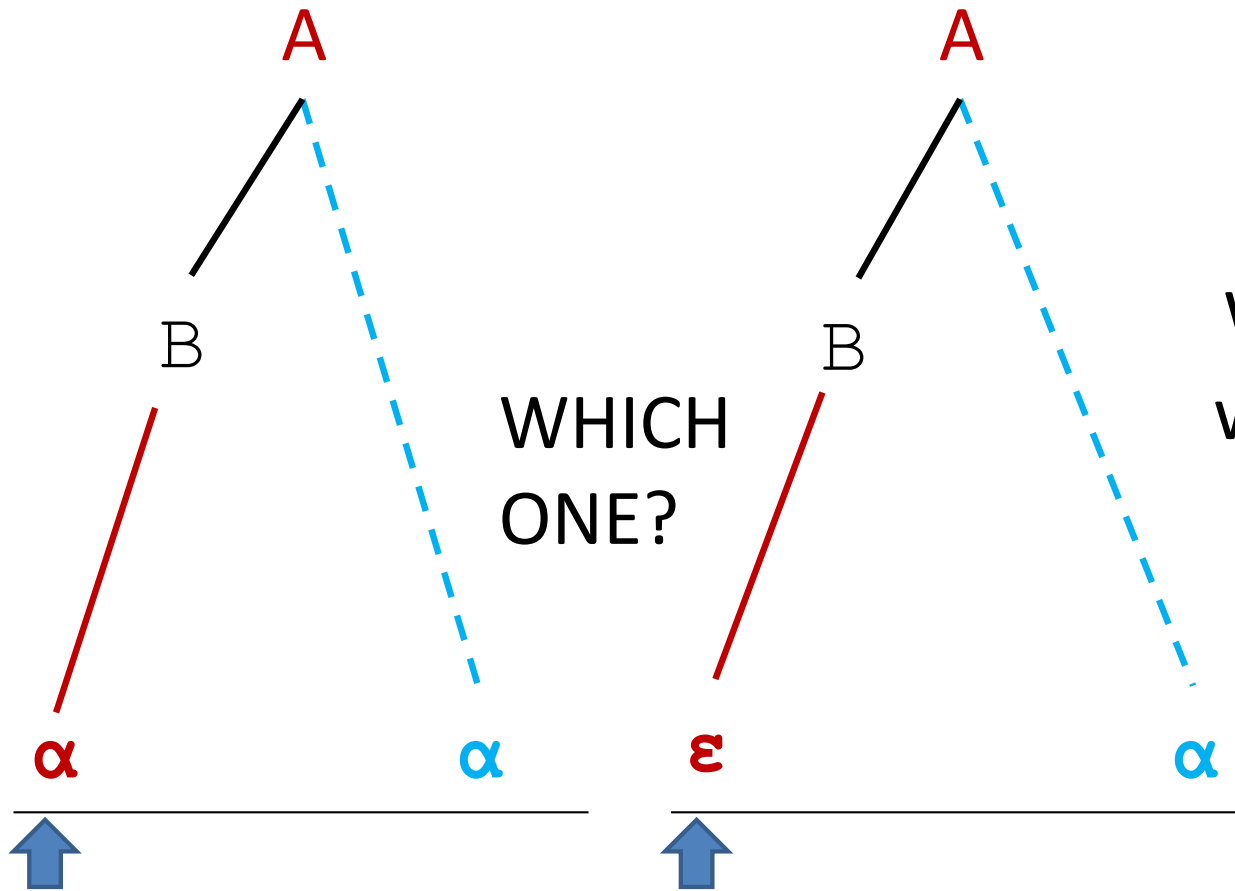
OR



Lookahead Remaining

α

Let's try a top-down derivation of " α "



WHICH
ONE?

0. $A ::= B \alpha$

1. $B ::= \alpha \mid \epsilon$

We don't know! Again,
we can't see more than
 α !

Canonical FIRST FOLLOW Conflict Solution

Solution

0. $A ::= B \alpha$

1. $B ::= \alpha \mid \epsilon$

Substitute the
common prefix

0. $A ::= \alpha\alpha \mid \alpha$

0. $A ::= \alpha \text{ Tail}$

Factor out the
tail

1. $\text{Tail} ::= \alpha \mid \epsilon$

Watch out for Nullability! (Grammar 2)

Changing the grammar again...

0. $S ::= a B$

1. $B ::= C x \mid y$

2. $C ::= \epsilon \mid x$

Lookahead

Remaining

a

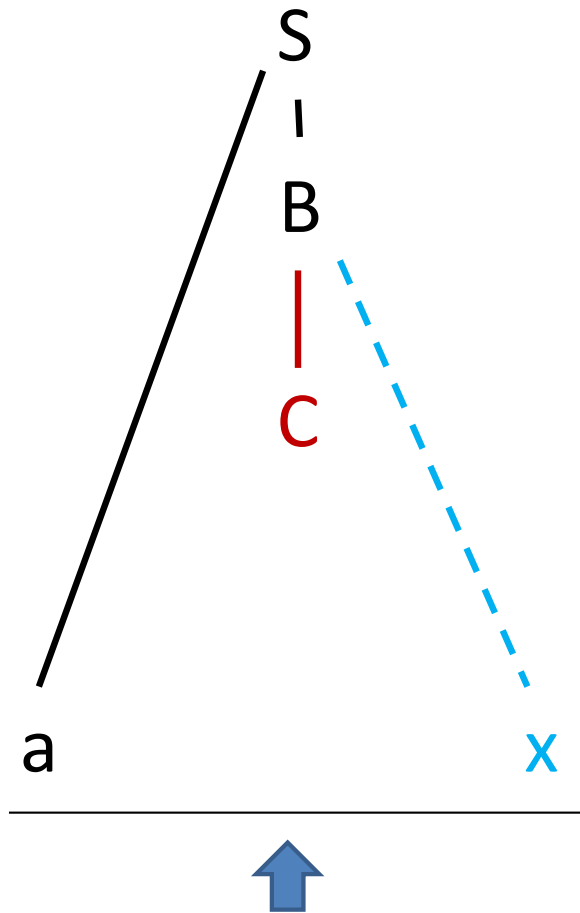
x

What's the issue?

0. $S ::= a B$
1. $B ::= C \mathbf{x} \mid y$
2. $C ::= \varepsilon \mid \mathbf{x}$

FIRST FOLLOW Conflict

Top down derivation of "ax"



0. $S ::= a B$

1. $B ::= C x \mid y$

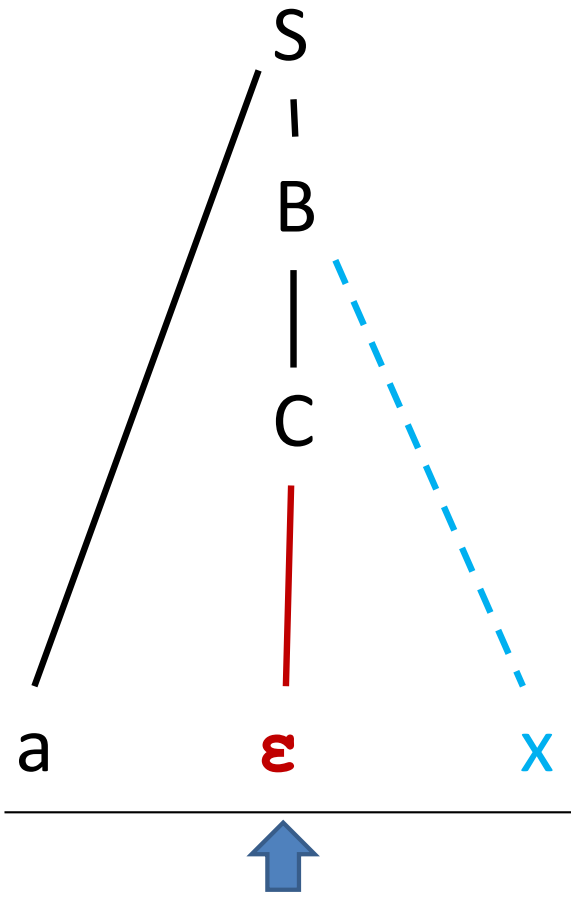
2. $C ::= \epsilon \mid \mathbf{x}$

Lookahead Remaining

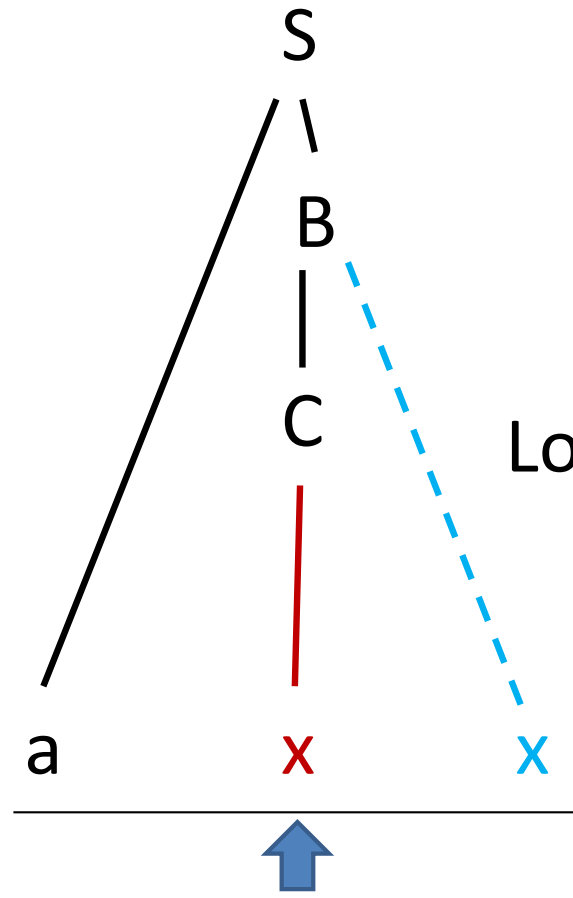
x

Top down derivation of "ax"

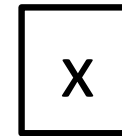
- 0. $S ::= a B$
- 1. $B ::= C x \mid y$
- 2. $C ::= \epsilon \mid x$



OR



Lookahead Remaining



Applying the Fix: Substitute the Common Prefix,

1

0. $S ::= a B$

1. $B ::= x \mid xx \mid y$

~~2. $C ::= \epsilon \mid x$~~

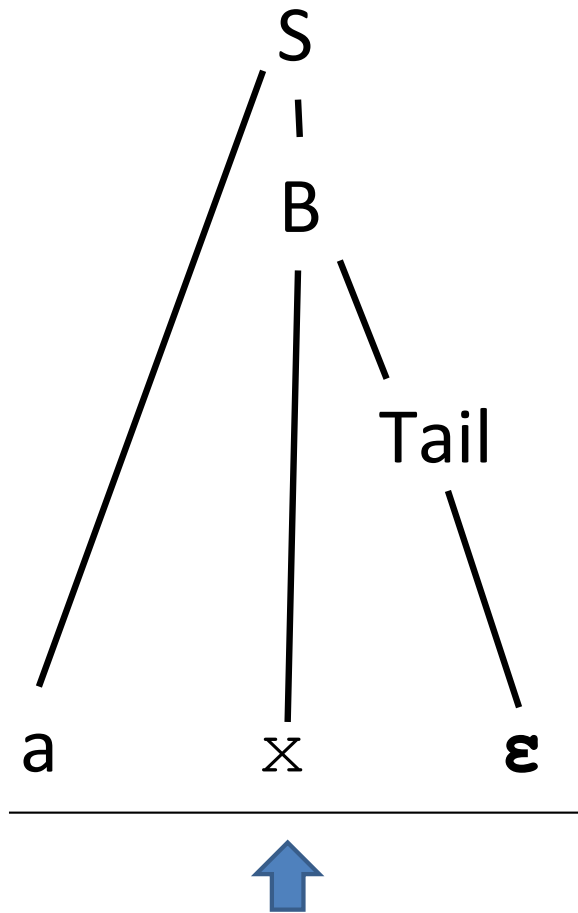
2

0. $S ::= a B$

1. $B ::= x Tail \mid y$

2. $Tail ::= x \mid \epsilon$

Top down derivation of "ax"



0. $S ::= a B$

1. $B ::= x Tail \mid y$

2. $Tail ::= x \mid \epsilon$

Lookahead Remaining

x