CSE 401/M501 – Compilers

LR Parser Construction Hal Perkins Spring 2024

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Administrivia (1)

- HW1 sample solutions handed out after class today. Might be some use finishing up scanner project. Grades/feedback out soon.
- Scanners due Thursday, 11 pm how's it going?
 - Must read MiniJava overview as well as scanner assignment & reread again when you think you're "done"
 - Be sure to implement both kinds of comments
 - Be sure to look carefully at MiniJava grammar to discover tokens
 - Anything "quoted" in the MiniJava project grammar should be treated as a reserved word (token) in MiniJava, even if it's not that in full Java
 - Be sure you can handle comments at end of file, also files with and without newlines at the end (and with and without comments at the end!)
 - Scanner should continue after "invalid input character" errors
 - Be sure to terminate with correct System.exit code (0=ok, 1=errors)
 - Don't get "creative" with the specs compiler must work as required
 - Take advantage of JFlex regexp operations that go beyond basic regexps presented in class and on hw1 if they are useful
 - Don't implement the parser just yet plenty of time for that...
 - Reminder: you have a partner(!) be sure to take advantage
 - Discussion board/email: never "I have a question" or "I am confused"
 - Rather: "We are confused" or "We have a question" ☺

Administrivia (2)

- Upcoming attractions:
 - Today/Wednesday and in sections this week: LR parsing and LR parser construction
 - HW2 (written questions on grammars, LR parsing) out shortly, due next Thur.
 - Wednesday/Friday lectures: LR parsing conflicts, first/follow, abstract syntax trees and visitor pattern
 - Next part of the project, Parser + AST visitors, out early next week, due a week and a half later
 - More details in lectures and sections next week

New Administrivia (added Wed.)

- Written hw2 out now, due a week from Thursday. Covers LR parsing and parser construction.
 - We'll finish up most of the background today and in sections tomorrow, but will have a bit left to do on Friday
- Reminder: scanners due tomorrow night, 11pm. Try not to burn a late day on this one.

Agenda

- LR(0) state construction
- FIRST, FOLLOW, and nullable
- Variations: SLR, LR(1), LALR

LR State Machine

- Idea: Build a DFA that recognizes handles
 - Language generated by a CFG is generally not regular, but
 - Language of viable prefixes for a CFG is regular
 - So a DFA can be used to recognize handles
 - LR Parser reduces when DFA accepts a handle

Prefixes, Handles, &c (review)

- If S is the start symbol of a grammar G,
 - If *S* =>* α then α is a *sentential form* of *G*
 - γ is a *viable prefix* of *G* if there is some derivation S =>*_{rm} $\alpha Aw =>_{rm} \alpha \beta w$ and γ is a prefix of $\alpha \beta$
 - These are the strings that can appear on the LR parser stack
 - The occurrence of β in $\alpha\beta w$ is the right side of a handle of $\alpha\beta w$
- An *item* is a marked production (a . at some position in the right hand side)

- [A ::= . X Y] [A ::= X . Y] [A ::= X Y .]

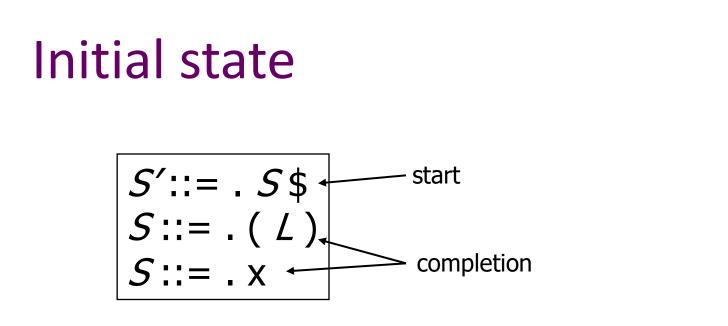
Building the LR(0) States

- Example grammar
 - S' ::= S \$ S ::= (L) S ::= x L ::= S L ::= L, S
 - We add a production S' with the original start symbol S followed by end of file (\$)
 - We accept if we reach the end of *S* in this production
 - Question: What language does this grammar generate?

Start of LR Parse

S'::= S\$
 S::= (L)
 S::= x
 L::= S
 L::= L, S

- Initially
 - Stack is empty
 - (except for start state number usually)
 - Input is the right hand side of S', i.e., S \$
 - Initial configuration is [S' ::= . S \$]
 - But, since position is just before S, we are also just before anything that can be derived from S



- A state is just a set of items
 - Start: an initial set of items
 - Completion (or closure): additional productions whose left-hand side nonterminal appears immediately following a dot in some item already in the state

0. S' ::= S

1. S ::= (L)

4. L ::= L, S

2. *S* ::= x

3. *L* ::= *S*

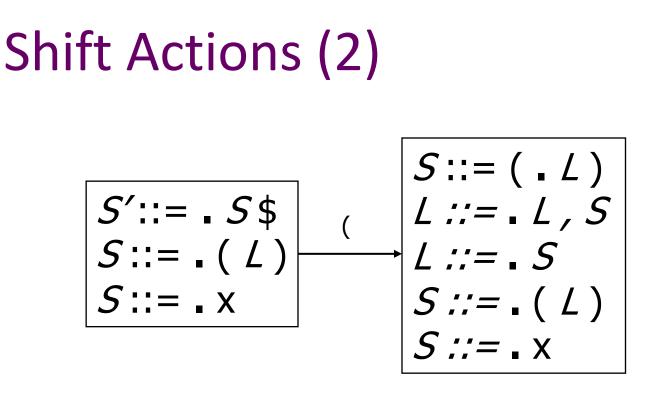
Shift Actions (1)

S'::= S\$
 S::= (L)
 S::= x
 L::= S
 L::= L, S

$$S'::= S$$

$$S::= (L) \xrightarrow{\times} S::= X$$

- To shift past the x, add a new state with appropriate item(s), including their closure
 - In this case, a single item; the closure adds nothing
 - This state will lead to a reduction since no further shift is possible



S'::= S\$
 S::= (L)
 S::= x
 L::= S
 L::= L, S

- If we shift past the (, we are at the beginning of L
- The closure adds all productions that start with L
 - and that requires adding all productions starting with S

Goto Actions

S'::= S\$
 S::= (L)
 S::= x
 L::= S
 L::= L, S

$$S'::= S$$

$$S::= (L)$$

$$S'::= S$$

• Once we reduce *S*, we'll pop the rhs from the stack exposing a previous state. Add a *goto* transition on *S* for this (i.e., if we back up into this state having reduced a rhs to *S*, then we need a goto transition on *S* to another state).

Basic Construction Operations

• Closure (S)

Adds all items implied by items already in S

- Goto (I, X)
 - I is a set of items
 - X is a grammar symbol (terminal or non-terminal)
 - Goto moves the dot past the symbol X in all appropriate items in set I

Closure Algorithm

• *Closure* (*S*) =

repeat

for any item $[A ::= \alpha \cdot B \beta]$ in *S* for all productions $B ::= \gamma$ add $[B ::= \cdot \gamma]$ to *S* until *S* does not change return *S*

• Classic example of a fixed-point algorithm

Goto Algorithm

• Goto (I, X) =

set *new* to the empty set for each item $[A ::= \alpha \cdot X \beta]$ in *I* add $[A ::= \alpha X \cdot \beta]$ to *new* return *Closure* (*new*)

• This may create a new state, or may return an existing one

LR(0) Construction

- First, augment the grammar with an extra start production S' ::= S \$
- Let T be the set of states
- Let *E* be the set of edges
- Initialize *T* to *Closure* ([*S*' ::= . *S* \$])
- Initialize *E* to empty

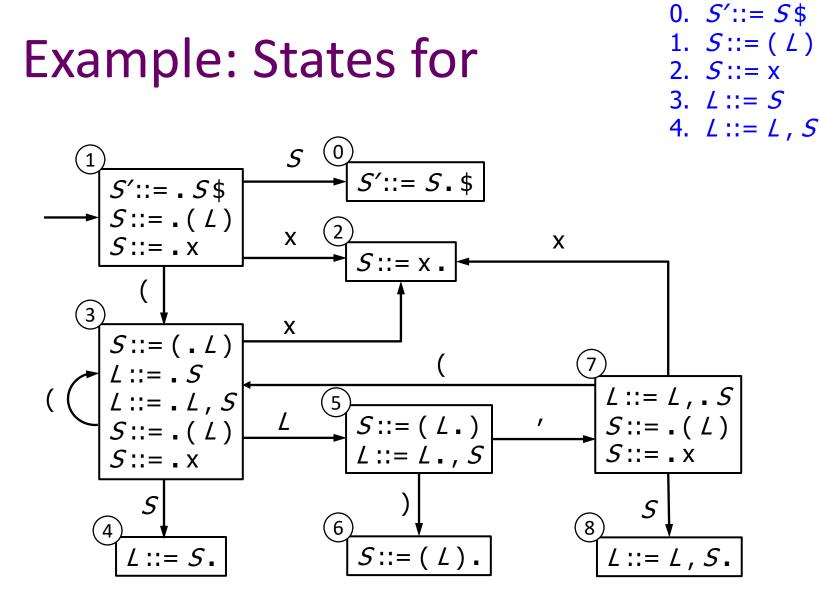
LR(0) Construction Algorithm

repeat for each state *I* in *T* for each item [$A ::= \alpha \cdot X \beta$] in *I* Let *new* be *Goto*(*I*, *X*) Add *new* to *T* if not present Add *I* \xrightarrow{X} *new* to *E* if not present until *E* and *T* do not change in this iteration

Footnote: For the marker \$, we don't compute goto(I, \$); instead, we make this an accept action.

Example: States for

S'::= S\$
 S::= (L)
 S::= x
 L::= S
 L::= L, S



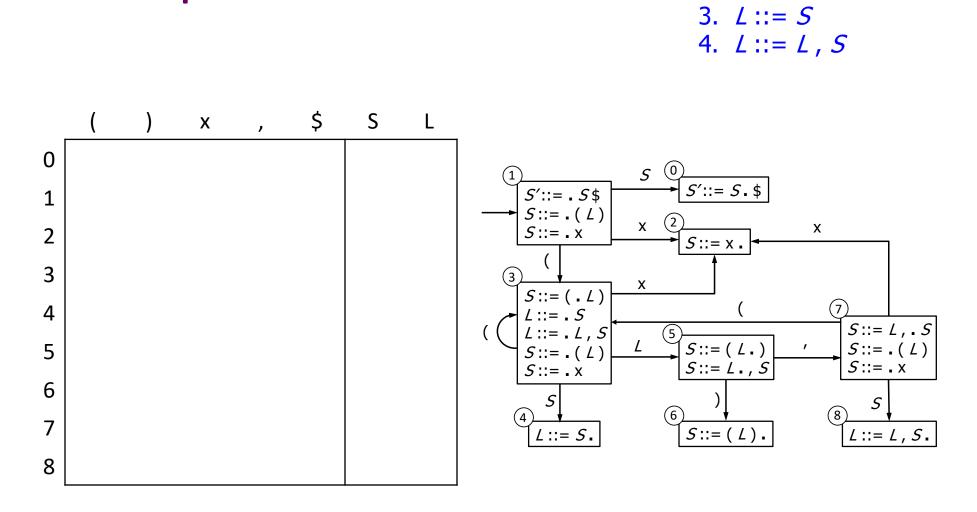
Building the Parse Tables (1)

- For each edge $I \xrightarrow{x} J$
 - if X is a terminal, put sj in column X, row I of the action table (shift to state j)
 - If X is a non-terminal, put gi in column X, row I of the goto table

Building the Parse Tables (2)

- For each state / containing an item
 [S' ::= S . \$], put accept in column \$ of row /
- Finally, for any state containing

 [A ::= γ .] put action rn (reduce) in every column of row I in the table, where n is the production number
 - i.e., when it reaches this state, the DFA has discovered that A ::= γ is a handle, so the parser should reduce γ to A



Example: Tables for

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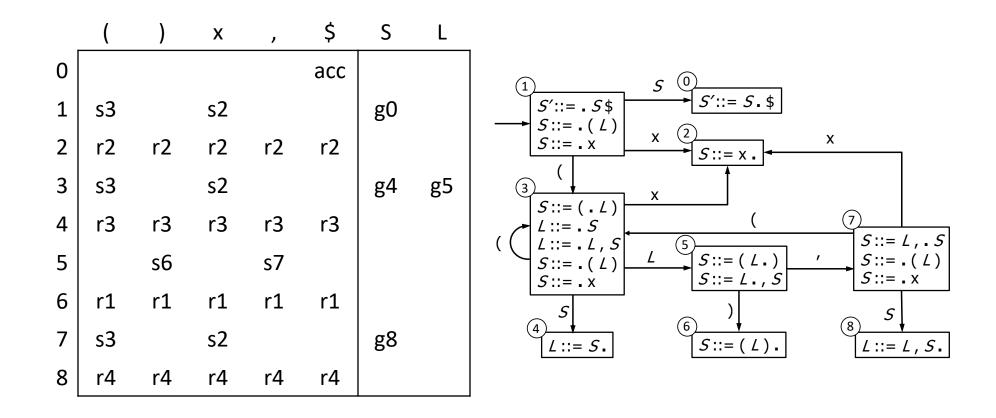
0. S' ::= S

1. S ::= (L)

2. *S* ::= x

Example: Tables for

0. S'::= S\$
1. S ::= (L)
2. S ::= x
3. L ::= S
4. L ::= L, S



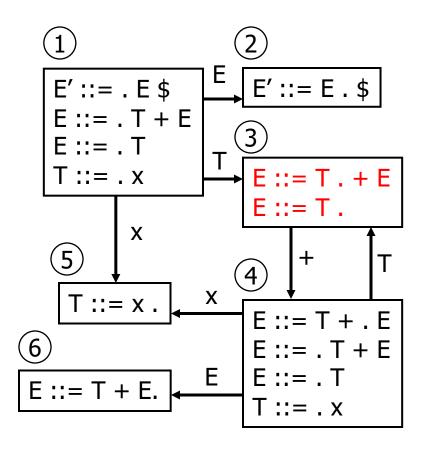
Where Do We Stand?

- We have built the LR(0) state machine and parser tables
 - No lookahead yet
 - Different variations of LR parsers add lookahead information, but basic idea of states, closures, and edges remains the same
- A grammar is LR(0) if its LR(0) state machine (equiv. parser tables) has no shift-reduce or reduce-reduce conflicts.

A Grammar that is not LR(0)

• Build the state machine and parse tables for a simple expression grammar

LR(0) Parser for 0. E'::= E \$ 1. E::= T + E 2. E::= T3. T::= x



	х	+	\$	Е	Т
1	s5			g2	g3
2			асс		
3	r2	s4,r2	r2		
4	s5			g6	g3
5	r3	r3	r3		
6	r1	r1	r1		

- State 3 is has two possible actions on +
 - shift 4, or reduce 2
- ∴ Grammar is not LR(0)

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How can we solve conflicts like this?

- Idea: look at the next symbol after the handle before deciding whether to reduce
- Easiest: SLR Simple LR. Reduce only if next input terminal symbol could follow resulting nonterminal
 - Suppose we've reached [A ::= β .] and the next input is x
 - Don't reduce unless Ax can appear in some sentential form
 - This is the *P idea*!
- More complex: LR and LALR. Store lookahead symbols in individual items to keep track of what can follow a *particular instance* of a reduction
 - LALR used by YACC/Bison/CUP; we won't examine in detail

SLR Parsers

- Idea: Use information about what can follow a nonterminal to decide if we should perform a reduction; don't reduce if the next input symbol can't ever follow the resulting non-terminal
- To decide, for each non-terminal A we need to know FOLLOW(A) – the set of terminal symbols that can follow A in some possible derivation
 - i.e., t is in FOLLOW(A) if there is some possible derivation that contains At
 - To compute this, we need to compute FIRST(γ) for strings γ that can follow A

Calculating FIRST(γ)

- Sounds easy... If γ = X Y Z, then FIRST(γ) is FIRST(X), right?
 - But what if we have the rule $X := \varepsilon$?
 - In that case, FIRST(γ) includes anything that can follow
 X, i.e. FOLLOW(X), which includes FIRST(Y) and, if Y
 can derive ε, FIRST(Z), and if Z can derive ε, ...
 - So computing FIRST and FOLLOW involves knowing
 FIRST and FOLLOW for other nonterminals, as well as which ones can derive ε

FIRST, FOLLOW, and nullable

- nullable(X) is true if X can derive the empty string
- Given a string γ of terminals and non-terminals, FIRST(γ) is the set of terminals that can begin strings derived from γ
 - For SLR we only need this for single terminal or non-terminal symbols, not arbitrary strings γ
- FOLLOW(X) is the set of terminals that can immediately follow X in some derivation
- All three of these are computed together
- Footnote: Textbook doesn't use a separate nullable(X) attribute, instead it indicates nullable by including ε in FIRST(X). Both will wind up with same results, but one or the other might be easier to follow, so to speak..

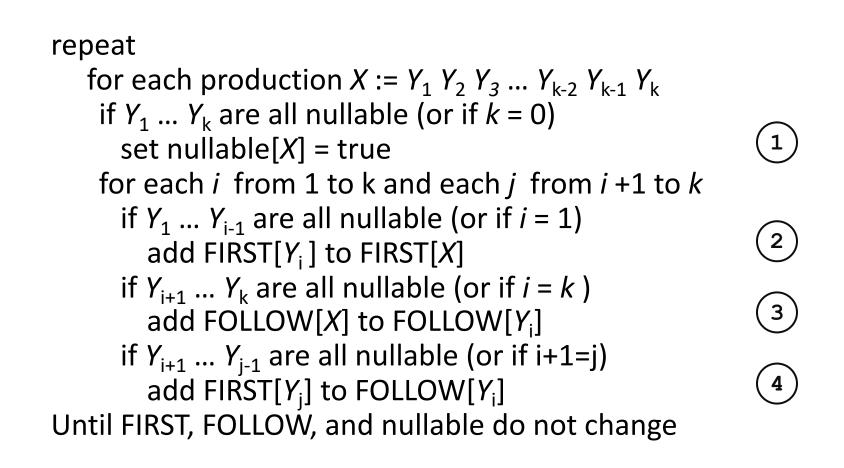
Computing FIRST, FOLLOW, and nullable (1)

Initialization

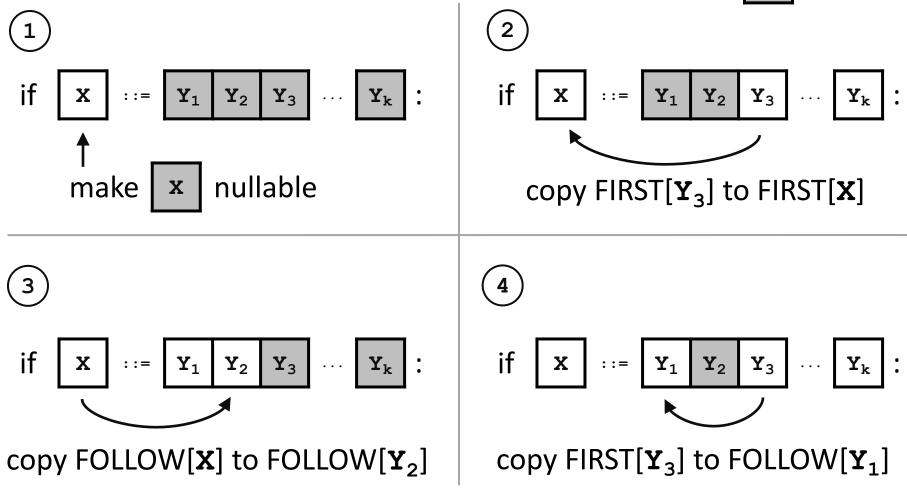
set FIRST and FOLLOW to be empty sets set nullable to false for all non-terminals set FIRST[a] to a for all terminal symbols a

- Repeatedly apply four simple observations to update these sets
 - Stop when there are no further changes
 - Another fixed-point algorithm

Computing FIRST, FOLLOW, and nullable (2)



Computing FIRST, FOLLOW, & nullable (3)



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Example (initial)

 Grammar 		nullable	FIRST	FOLLOW
<i>Z</i> ::= d				
<i>Z</i> ::= <i>X Y Z</i>	X	no		
Υ ::= ε				
<i>Y</i> ::= c				
<i>X</i> ::= <i>Y</i>	Y	no		
<i>X</i> ::= a				
	_			
	Z	no		
	I			

Example (final)

 Grammar 		nullable	FIRST	FOLLOW
Z ::= d Z ::= X Y Z	X	no yes	a, c	a, c, d
Y ::= ε Y ::= c X ::= Y X ::= a	Ŷ	no yes	C	a, c, d
	Ζ	no	a, c, d	

LR(0) Reduce Actions (review)

- In a LR(0) parser, if a state contains a reduction, it is unconditional regardless of the next input symbol
- Algorithm:
 - Initialize R to empty
 - for each state I in T

for each item [A ::= α .] in I

add (/, $A ::= \alpha$) to R

SLR Construction

- This is identical to LR(0) states, etc., except for the calculation of reduce actions
- Algorithm:

Initialize R to empty

for each state I in T

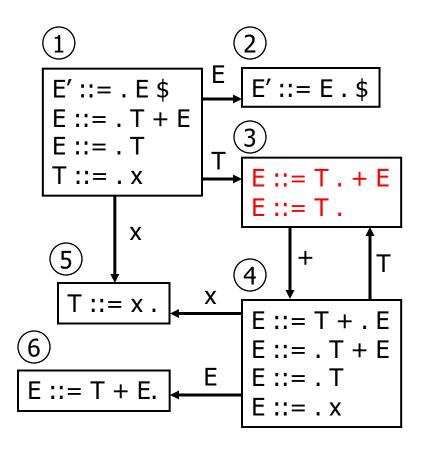
```
for each item [A ::= \alpha .] in I
```

for each terminal a in FOLLOW(A) so new!

add (*I*, a, $A ::= \alpha$) to R

– i.e., reduce α to A in state / only on lookahead a

SLR Parser for



```
    E' ::= E $
    E ::= T + E
    E ::= T
    T ::= x
```

	х	+	\$	Е	Т
1	s5			g2	g3
2			acc		
3	r2	s4, <mark>r2</mark>	r2		
4	s5			g6	g3
5	r3	r3	r3		
6	r1	r1	r1		

Ghost yellow = reductions omitted in SLR parser because next terminal is not in FOLLOW(non-terminal)

On To LR(1)

- Many practical grammars are SLR
- LR(1) is more powerful yet
- Similar construction, but notion of an item is more complex, incorporating lookahead information
 - So lookahead information is associated with specific items rather than using FOLLOW for the non-terminal, which ignores the context where that non-terminal appears in the derivation

LR(1) Items

- An LR(1) item [$A ::= \alpha \cdot \beta$, a] is
 - A grammar production (A ::= $\alpha\beta$)
 - A right hand side position (the dot)
 - A lookahead symbol (a)
- Idea: This item indicates that α is the top of the stack and the next input is derivable from $\beta a.$
- Full construction: see the book(s)

LR(1) Tradeoffs

- LR(1)
 - Pro: extremely precise; largest set of grammars
 - Con: potentially *very* large parse tables with many states

LALR(1)

- Variation of LR(1), but merge any two states that differ only in lookahead
 - Example: these two would be merged

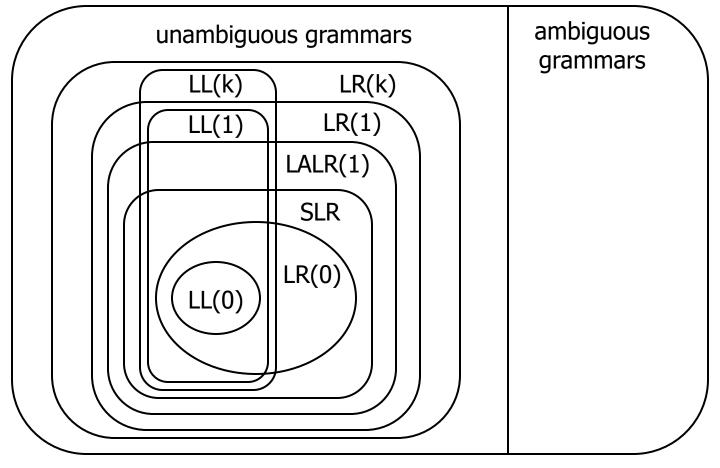
to produce

[A ::= x . y , ab]

LALR(1) vs LR(1)

- LALR(1) tables can have many fewer states than LR(1)
 - Somewhat surprising result: will actually have same number of states as SLR parsers, even though LALR(1) is more powerful because of the more fine-grained lookahead info in the states
 - After the merge step, LALR(1) acts like SLR parser with "smarter" FOLLOW sets (can be specific to particular handles)
- LALR(1) may have reduce conflicts where LR(1) would not (but in practice this doesn't happen often)
- Most practical bottom-up parser tools are LALR(1) (e.g., yacc, bison, CUP, ...)

Language Hierarchies



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Coming Attractions

Lecture

- ASTs and Visitor pattern
- LL(k) Parsing Top-Down
- Recursive Descent Parsers

What you can do if you want a parser in a hurry
 Sections next week

- AST construction what do do while you parse!
- Visitor Pattern details how to traverse ASTs for further processing (type checking, code gen, ...)