CSE 401/M501 – Compilers

SSA
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Spring 2023

Administrivia

- Codegen assignment and related slides for today's class and tomorrow's sections posted now
 - Due a week from Thursday (for 401)
 - CSE M 501 compilers with extensions due a week later (end of last week of classes). No separate codegen submission.
 - Get System.out.println(17) from main working by this Friday night (no kidding!)
 - Easy enough to do by the deadline if you don't put it off
- Once codegen is done we'll do an overall evaluation of your compiler, all phases, and rerun a comprehensive set of tests. This final evaluation is the major part of the project grade. So you need to fix any remaining bugs, all the way back to the scanner!

Agenda

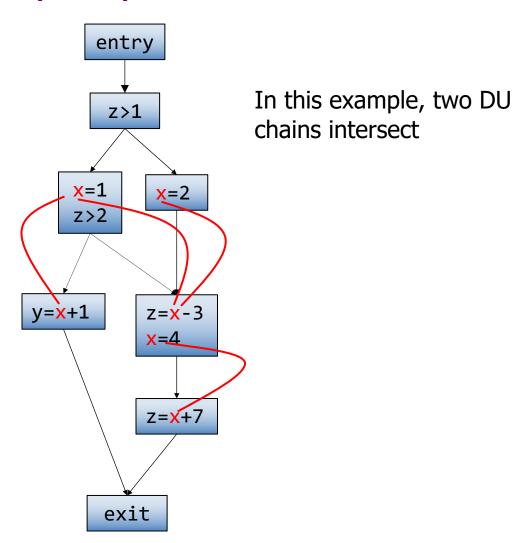
- Overview of SSA IR
 - Constructing SSA graphs
 - Sample of SSA-based optimizations
 - Converting back from SSA form

 Sources: Appel ch. 19, also an extended discussion in Cooper-Torczon sec. 9.3; Mike Ringenburg's CSE 401 slides

Def-Use (DU) Chains

- Common dataflow analysis problem: Find all sites where a variable is used, or find the definition site(s) of a variable used in an expression
- Traditional solution: def-use chains additional data structure on top of the dataflow graph
 - Link each statement defining a variable to all statements that use it
 - Link each use of a variable to its (single) definition

Def-Use (DU) Chains



DU-Chain Drawbacks

- Expensive: if a typical variable has N uses and M definitions, the total cost *per-variable* is O(N * M), i.e., O(n²)
 - Would be nice if cost were proportional to the size of the program
- Unrelated uses of the same variable are mixed together
 - Complicates analysis variable looks live across all uses even if unrelated

SSA: Static Single Assignment

- IR where each variable has only one definition in the program text
 - This is a single *static* definition, but that definition can be in a loop, function, or other code that is executed dynamically many times
- Makes many analyses (and related optimizations) more efficient
- Separates values from memory storage locations
- Complementary to CFG/DFG better for some things, but cannot do everything

SSA in Basic Blocks

Idea: for each original variable v_n create a new variable v_n at the n^{th} definition of the original v_n . Subsequent uses of v use v_n until the next definition point.

Original

$$a := x + y$$

$$b := a - 1$$

$$a := y + b$$

$$b := x * 4$$

$$a := a + b$$

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$$a_1 := x + y$$

$$b_1 := a_1 - 1$$

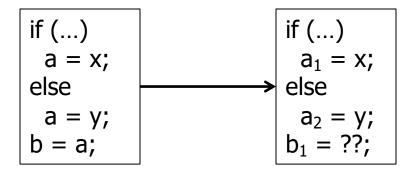
$$a_2 := y + b_1$$

$$b_2 := x * 4$$

$$a_3 := a_2 + b_2$$

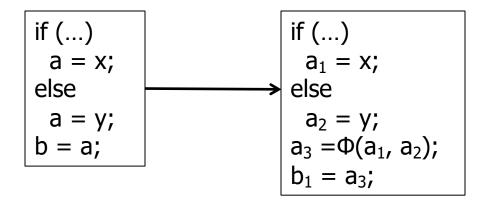
Merge Points

The issue is how to handle merge points



Merge Points

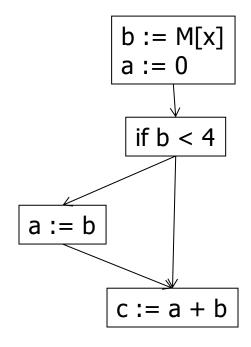
The issue is how to handle merge points



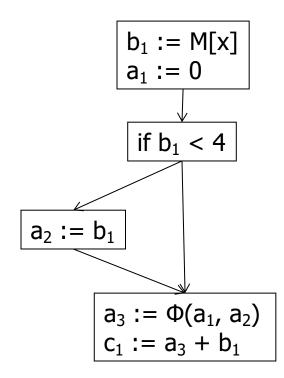
- Solution: introduce a Φ-function
 - $a_3 := \Phi(a_1, a_2)$
- Meaning: a_3 is assigned either a_1 or a_2 depending on which control path is used to reach the Φ -function

Another Example

Original



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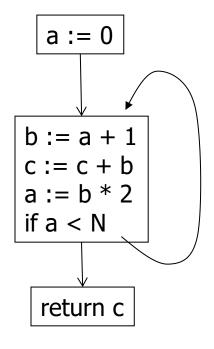


How Does Φ "Know" What to Pick?

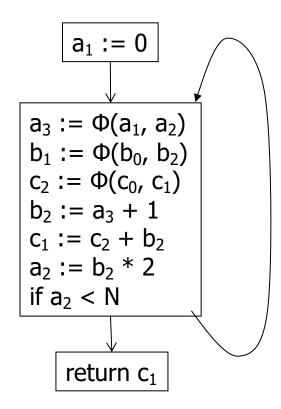
- It doesn't!
- Φ-functions don't actually exist at runtime
 - When we're done using the SSA IR, we translate back out of SSA form, removing all Φ-functions
 - Basically by adding code to copy all SSA x_i values to the single, non-SSA variable x
 - For analysis, all we typically need to know is the connection of uses to definitions – no need to "execute" anything
 - So Φ-functions are (only) compile-time bookkeeping

Example With a Loop

Original



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Notes:

Loop-back edges are also merge points, so require Φ-functions
Convention: a₀, b₀, c₀ are initial values of a, b, c on entry to initial block
b₁ is dead – can delete later
c is live on entry – either input parameter or uninitialized

What does SSA "buy" us?

No need for DU or UD chains – implicit in SSA

Compact representation

• SSA is "recent" (i.e., 80s)

Prevalent in real compilers for { } languages

Converting To SSA Form

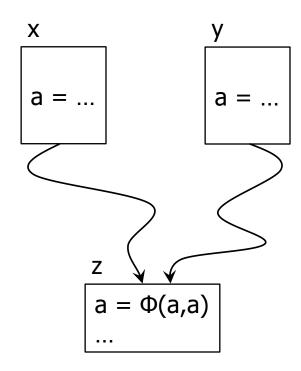
- Basic idea
 - First, add Φ-functions
 - Then, rename all definitions and uses of variables by adding subscripts

Inserting **Φ-Functions**

- Could simply add Φ-functions for every variable at every join point(!)
- Called "maximal SSA"
- But
 - Wastes way too much space and time
 - Not needed in many cases

Path-convergence criterion

- Insert a Φ-function for variable a at point z when:
 - There are blocks x and y,
 both containing definitions
 of a, and x ≠ y
 - There are nonempty paths
 from x to z and from y to z
 - These paths have no common nodes other than z

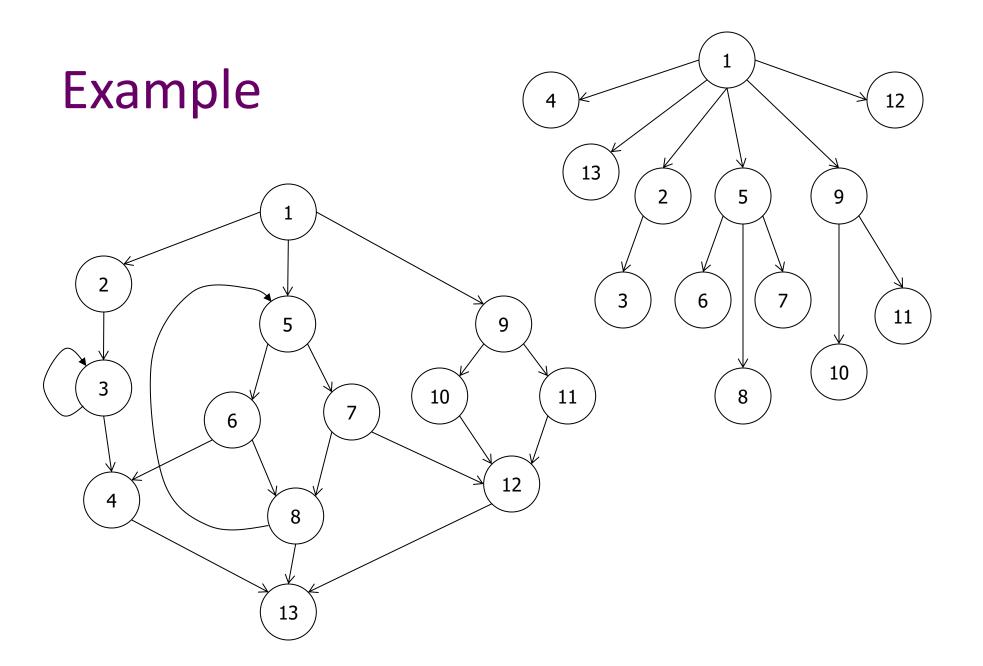


Details

- The start node of the flow graph is considered to define every variable (even if "undefined")
- Each Φ-function itself defines a variable, which may create the need for a new Φ-function
 - So we need to keep adding Φ-functions until things converge
- How can we do this efficiently?
 Use a new concept: dominance frontiers

Dominators

- Definition: a block x dominates a block y iff every path from the entry of the control-flow graph to y includes x
- So, by definition, x dominates x
- We can associate a Dom(inator) set with each
 CFG node x set of all blocks dominated by x
 | Dom(x) | ≥ 1
- Properties:
 - Transitive: if a dom b and b dom c, then a dom c
 - There are no cycles, thus can represent the dominator relationship as a tree



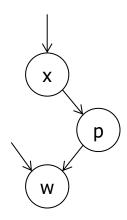
Dominators and SSA

- One property of SSA is that definitions dominate uses; more specifically:
 - If $x := Φ(...,x_i,...)$ is in block b, then the definition of x_i dominates the ith predecessor of b
 - If x is used in a non-Φ statement in block b, then the definition of x dominates block b

Dominance Frontier (1)

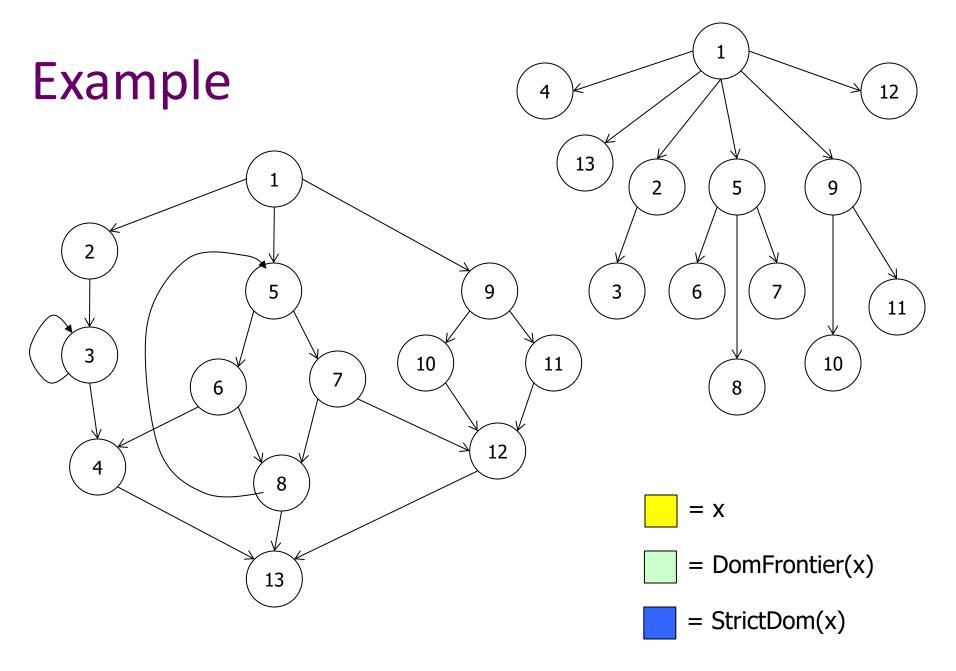
- To get a practical algorithm for placing Φfunctions, we need to avoid looking at all combinations of nodes leading from x to y
- Instead, use the dominator tree in the flow graph

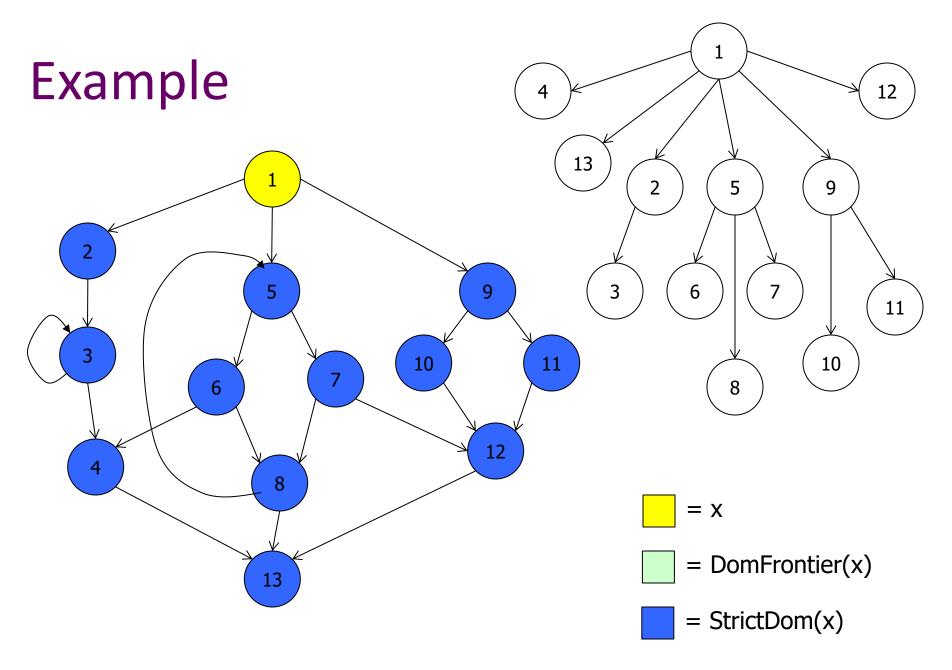
Dominance Frontier (2)

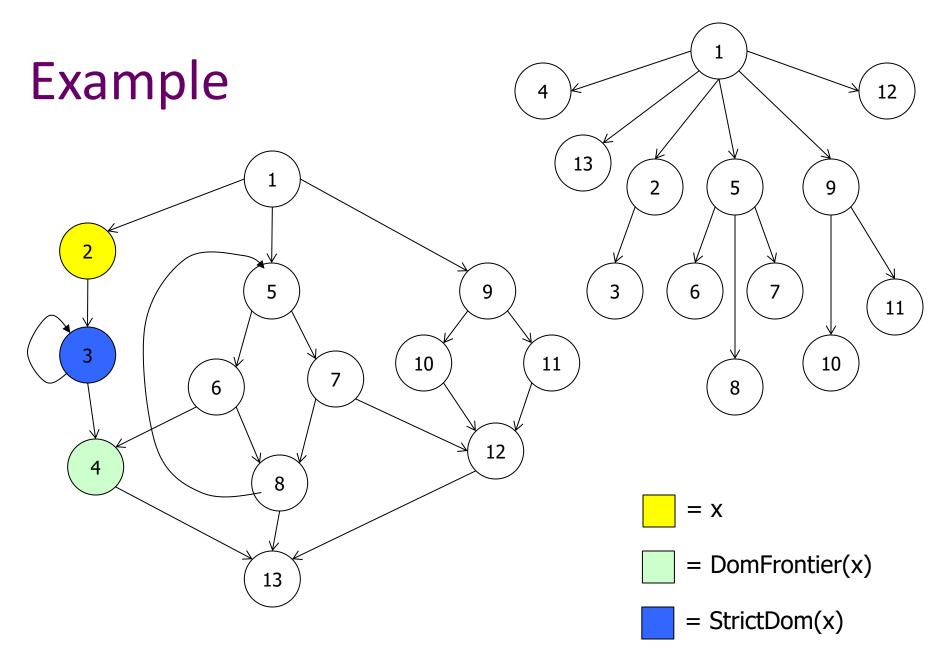


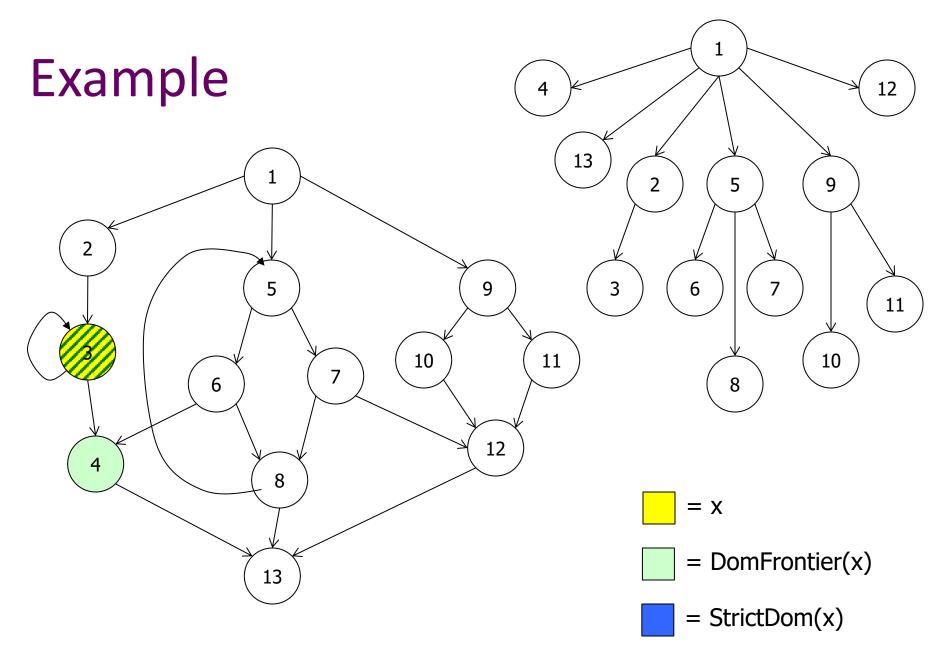
Definitions

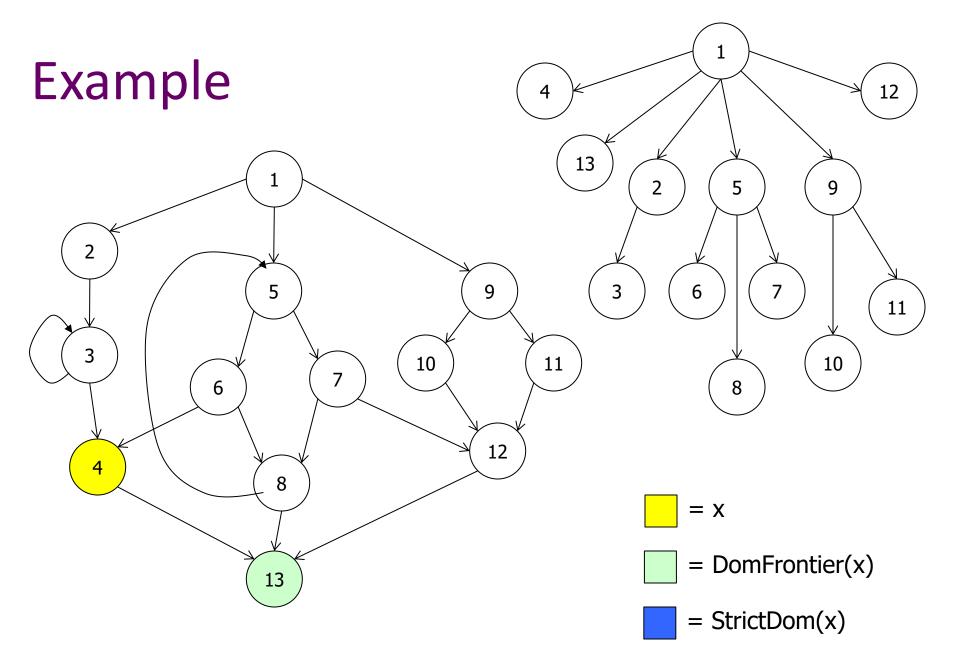
- x strictly dominates y if x dominates y and $x \neq y$
- The dominance frontier of a node x is the set of all nodes w such that x dominates a predecessor p of w, but x does not strictly dominate w
 - ∴ if x and w are different, then x does not dominate w there is some other path to w that does not go through x
 - But x can be in *it's own* dominance frontier! That can happen if there is a back edge to x from some node that x dominates (i.e., x is the head of a loop)
- Essentially, the dominance frontier is the border between dominated and undominated nodes

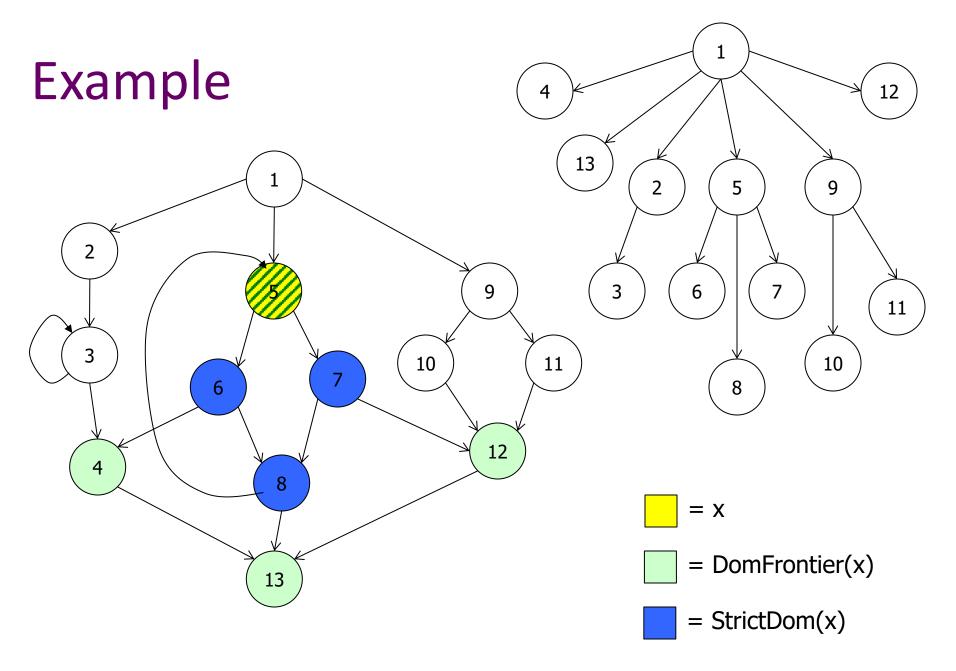


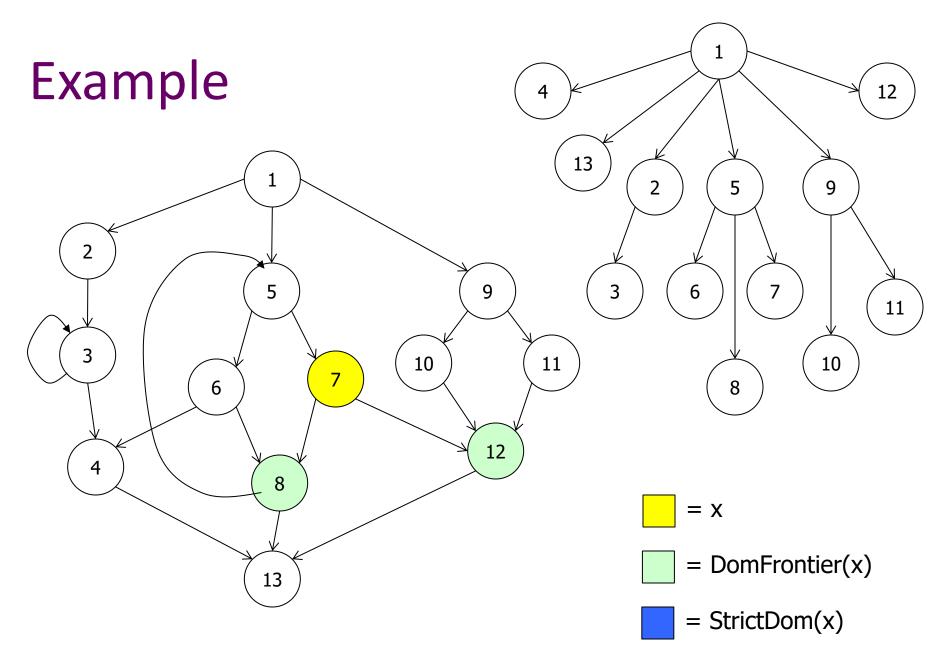


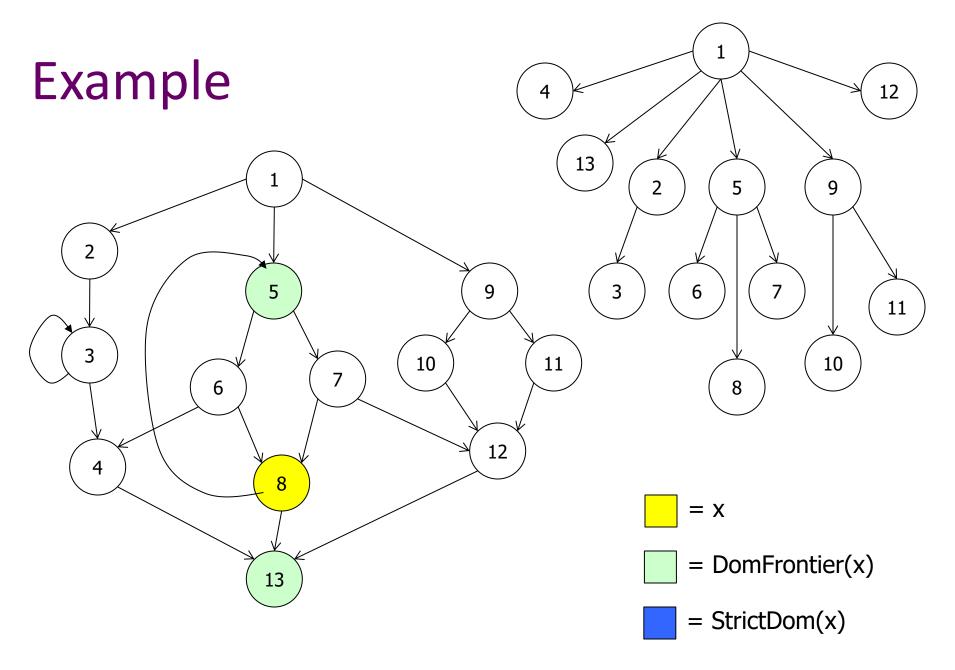


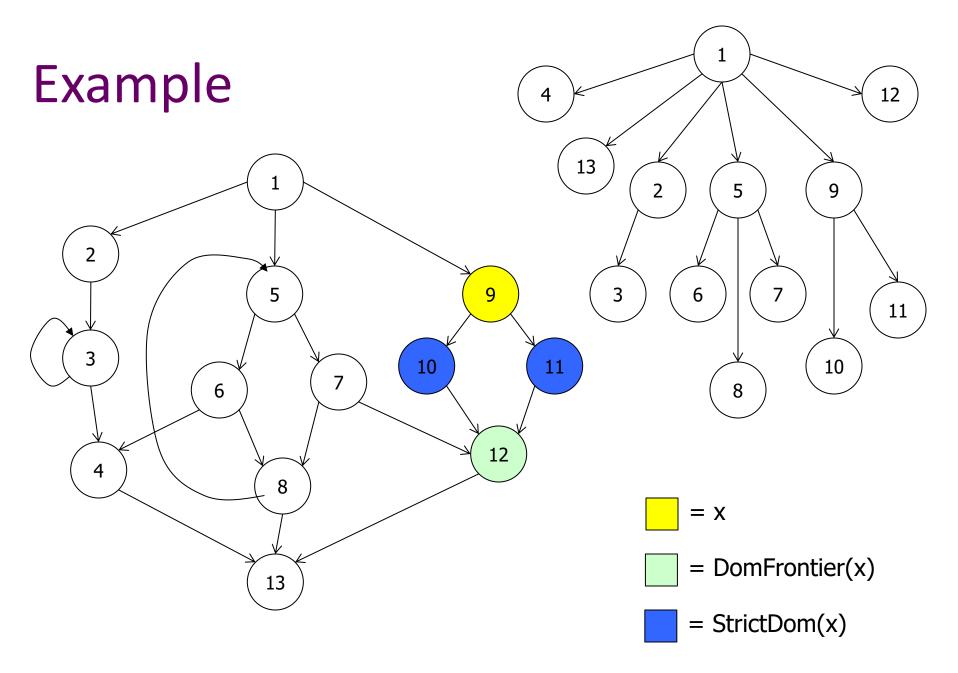


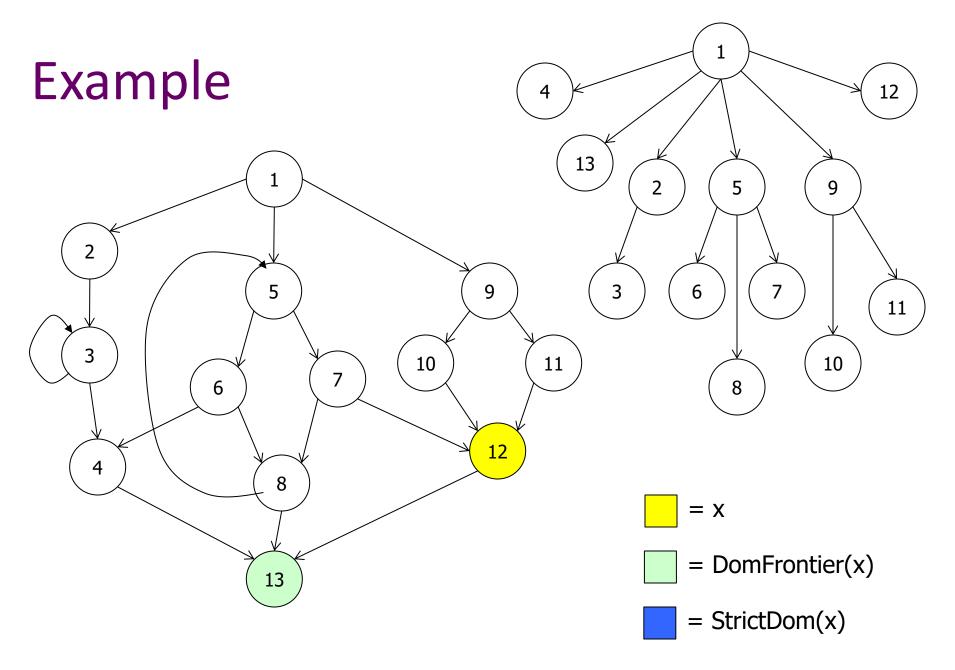


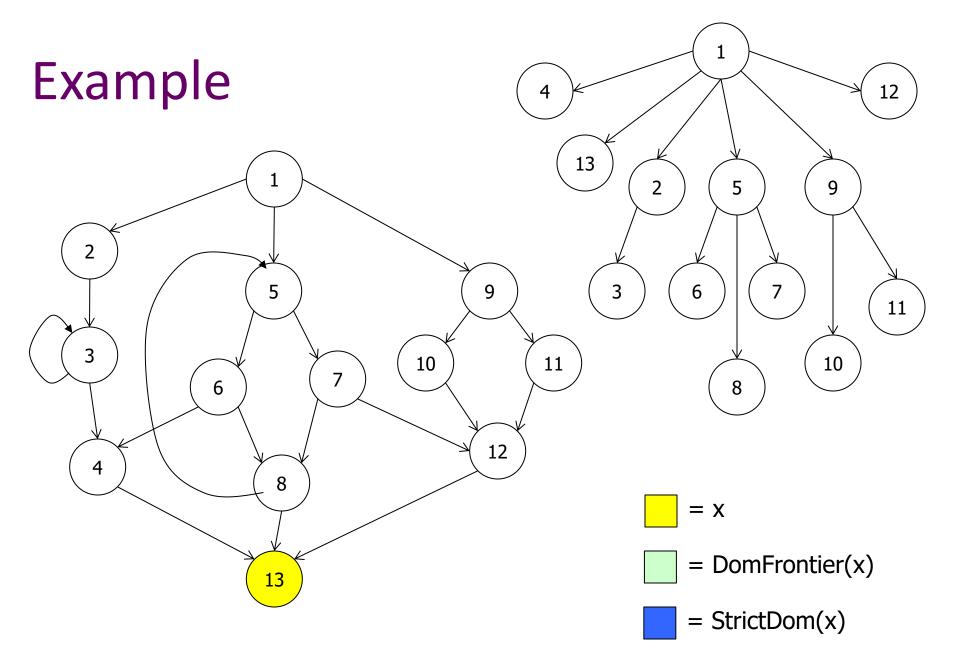




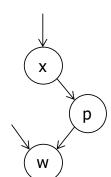








Dominance Frontier Criterion for Placing Φ-Functions



- If a node x contains the definition of variable a, then every node in the dominance frontier of x needs a Φ-function for a
 - Idea: Everything dominated by x will see x's definition of a. The dominance frontier represents the first nodes we could have reached via an alternative path, which will have an alternate reaching definition of a (recall the convention that the entry node defines all variables with version $0 a_0$)
 - Why is this right for loops? Hint: strict dominance...
 - Since the Φ-function itself is a definition, this placement rule needs to be iterated until it reaches a fixed-point
- Theorem: this algorithm places exactly the same set of Φ-functions as the path convergence criterion (above)

Placing Φ-Functions: Details

- See the book for the full construction, but the basic steps are:
 - 1. Compute the dominance frontiers for each node in the flowgraph
 - 2. Insert just enough Φ-functions to satisfy the criterion. Use a worklist algorithm to avoid reexamining nodes unnecessarily
 - 3. Walk the dominator tree and rename the different definitions of each variable a to be a_1 , a_2 , a_3 , ...

SSA Optimizations

- Why go to the trouble of translating to SSA?
- The advantage of SSA is that it makes many optimizations and analyses simpler and more efficient
 - We'll give a couple of examples
- But first, what do we know? (i.e., what information is stored in the compiler SSA graph data structures?)

SSA Data Structures

For each ...

- Statement: links to containing block, next and previous statements, variables defined, variables used
- Variable: link to its (single) definition and (possibly multiple) use sites
- Block: List of contained statements, ordered list of predecessor(s) & successor(s) blocks

Dead-Code Elimination

- A variable is live ⇔ its list of uses is not empty(!)
 - That's it! Nothing further to compute
- Algorithm to delete dead code:

while there is some variable v with no uses

if the statement that defines v has no other side effects, then delete it and remove this statement from list of uses for its operand variables - which may cause those variables to become dead

Simple Constant Propagation

- If c is a constant in v := c, any use of v can be replaced by c
 - So update every use of v to use constant c
- If the c_i 's in $v := \Phi(c_1, c_2, ..., c_n)$ are all the same constant c, we can replace this with v := c
- Incorporate copy propagation, constant folding, and others in the same worklist algorithm

Simple Constant Propagation

```
W := list of all statements in SSA program
while W is not empty
  remove some statement S from W
  if S is v:=\Phi(c, c, ..., c), replace S with v:=c
  if S is v := c
    delete S from the program
    for each statement T that uses v
      substitute c for v in T
      add T to W
```

Converting Back from SSA

- Unfortunately, real machines do not include a Ф instruction
- So after analysis, optimization, and transformation, need to convert back to a "Φ-less" form for execution
 - (Also sometimes needed for different kinds of analysis or transformation. A production optimizer might convert the IR into and out of SSA form multiple times)

Translating Φ-functions

- The meaning of $x := \Phi(x_1, x_2, ..., x_n)$ is "set $x = x_1$ if arriving on predecessor block edge 1, set $x = x_2$ if arriving on edge 2, etc."
- So, for each i, insert x = x_i at the end of predecessor block i
- Rely on copy propagation and coalescing in register allocation to eliminate redundant copy instructions

SSA Wrapup

- More details needed to fully and efficiently implement SSA, but these are the main ideas
 - See recent compiler books (but not the Dragon book!)
- Allows efficient implementation of many optimizations
- SSA is used in most modern optimizing compilers (Ilvm is based on it) and has been retrofitted into many older ones (gcc is a major example)
- Not a silver bullet some optimizations still need non-SSA forms – but very effective for many