# **Dataflow Analysis + SSA**

CSE 401/M501 Sections

## Announcements

- 401 CodeGen hard deadline SATURDAY 11pm no matter what late days used before. Must commit/push/tag by Sat. 11pm, not later
- 401 report due next Monday 11pm (no late days); M501 project/report due as written on assignment
- HW4 due next Thursday, 11 pm



PeepholeA few InstructionsLocalIntraprocedural / GlobalInterproceduralInterprocedural

PeepholeA few InstructionsLocalA Basic BlockIntraprocedural / GlobalInterprocedural

PeepholeA few InstructionsLocalA Basic BlockIntraprocedural / GlobalA Function/MethodInterproceduralInterprocedural

PeepholeA few InstructionsLocalA Basic BlockIntraprocedural / GlobalA Function/MethodInterproceduralA Program

## **Overview of Dataflow Analysis**

- A framework for exposing properties about programs
- Operates using sets of "facts"



# **Overview of Dataflow Analysis**

- A framework for exposing properties about programs
- Operates using sets of "facts"
- Just the initial discovery phase
  - Changes can then be made to optimize based on the



# **Overview of Dataflow Analysis**

- Basic Framework of Set Definitions (for a Basic Block *b*):
  - IN(*b*): facts true on entry to *b*
  - OUT(b): facts true on exit from b
  - GEN(b): facts created (and not killed) in b
  - KILL(*b*): facts killed in *b*

## **Reaching Definitions** (*A Dataflow Problem*)

"What definitions of each variable might reach this point"

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-	Could be used for:	int x;
	<ul> <li>Constant Propagation</li> <li>Uninitialized Variables</li> </ul>	<pre>if (y &gt; 0) {     x = y; } else {     x = 0; }</pre>
	"x=y", "x=0"	<pre>System.out.println(x);</pre>

## **Reaching Definitions** (A Dataflow Problem)

"What definitions of each variable might reach this point"

```
Be careful: Does not involve the
value of the definition
- The dataflow problem
"Available Expressions"
is designed for that
still: "x=y", "x=0"
is till: "x=y", "x=0"
int x;
if (y > 0) {
x = y;
} else {
x = 0;
}
y = -1;
```

# **Equations for Reaching Definitions**

- IN(*b*): the definitions reaching upon entering block b
- OUT(*b*): the definitions reaching upon exiting block b
- GEN(b): the definitions assigned and not killed in block b
- KILL(*b*): the definitions of variables overwritten in block b

$$IN(b) = U_{p \in pred(b)}OUT(p)$$
$$OUT(b) = GEN(b) \cup (IN(b) - KILL(b))$$

# Problems 1(a) and 1(b)

Block	GEN	KILL	IN (1)	OUT (1)	IN (2)	OUT (2)
LO	L0					
L1	L1					
L2	L2					
L3	L3					
L4						
L5						

Block	GEN	KILL	IN (1)	OUT (1)	IN (2)	OUT (2)
LO	LØ					
L1	L1					
L2	L2					
L3	L3	LØ				
L4						
L5						

Block	GEN	KILL	IN (1)	OUT (1)	IN (2)	OUT (2)
LO	L0					
L1	L1		LØ			
L2	L2		L0, L1			
L3	L3	LØ	L0, L1, L2			
L4			L1, L2, L3			
L5			L1, L2, L3			

Block	GEN	KILL	IN (1)	OUT (1)	IN (2)	OUT (2)
LO	L0			LØ		
L1	L1		LØ	L0, L1		
L2	L2		L0, L1	L0, L1, L2		
L3	L3	LØ	L0, L1, L2	L1, L2, L3		
L4			L1, L2, L3	L1, L2, L3		
L5			L1, L2, L3	L1, L2, L3		

Block	GEN	KILL	IN (1)	OUT (1)	IN (2)	OUT (2)
LO	L0			LØ		LØ
L1	L1		LØ	L0, L1	L0, L1, L2, L3	L0, L1, L2, L3
L2	L2		L0, L1	L0, L1, L2	L0, L1, L2, L3	L0, L1, L2, L3
L3	L3	LØ	L0, L1, L2	L1, L2, L3	L0, L1, L2, L3	L1, L2, L3
L4			L1, L2, L3	L1, L2, L3	L1, L2, L3	L1, L2, L3
L5			L1, L2, L3	L1, L2, L3	L1, L2, L3	L1, L2, L3



Block	GEN	KILL	IN (1)	OUT (1)	IN (2)	OUT (2)
LO	L0			LØ		LØ
L1	L1		LØ	L0, L1	L0, L1, L2, L3	L0, L1, L2, L3
L2	L2		L0, L1	L0, L1, L2	L0, L1, L2, L3	L0, L1, L2, L3
L3	L3	LØ	L0, L1, L2	L1, L2, L3	L0, L1, L2, L3	L1, L2, L3
L4			L1, L2, L3	L1, L2, L3	L1, L2, L3	L1, L2, L3
L5			L1, L2, L3	L1, L2, L3	L1, L2, L3	L1, L2, L3

## Is it possible to replace the use of *a* in block L1 with the constant 0?

L1: b = a + 1

L0: a = 0

- L2: c = c + b
- L3: a = b \* 2 L4: if a < N goto L1
- L5: return c

Block	GEN	KILL	IN (1)	OUT (1)	IN (2)	OUT (2)
LO	L0			LØ		LØ
L1	L1		LØ	L0, L1	L0, L1, L2, L3	L0, L1, L2, L3
L2	L2		L0, L1	L0, L1, L2	L0, L1, L2, L3	L0, L1, L2, L3
L3	L3	LØ	L0, L1, L2	L1, L2, L3	L0, L1, L2, L3	L1, L2, L3
L4			L1, L2, L3	L1, L2, L3	L1, L2, L3	L1, L2, L3
L5			L1, L2, L3	L1, L2, L3	L1, L2, L3	L1, L2, L3

#### L0: a = 0

- L1: b = a + 1
- L2: c = c + b
- L3: a = b \* 2
- L4: if a < N goto L1
- L5: return c

Is it possible to replace the use of *a* in block L1 with the constant 0?

No. To determine this, we would look at the IN set for block L1 -- the fact that the IN set contains two definitions of 'a' (L0 and L3) means we cannot perform this constant propagation. In other words, more than one definition of 'a' is a reaching definition to block L1, and therefore performing constant propagation would only preserve one possible value of 'a' and the generated code would not be equivalent.

Block	GEN	KILL	IN (1)	OUT (1)	IN (2)	OUT (2)
LO	L0			LØ		LØ
L1	L1		LØ	L0, L1	L0, L1, L2, L3	L0, L1, L2, L3
L2	L2		L0, L1	L0, L1, L2	L0, L1, L2, L3	L0, L1, L2, L3
L3	L3	LØ	L0, L1, L2	L1, L2, L3	L0, L1, L2, L3	L1, L2, L3
L4			L1, L2, L3	L1, L2, L3	L1, L2, L3	L1, L2, L3
L5			L1, L2, L3	L1, L2, L3	L1, L2, L3	L1, L2, L3

## **Phi-Functions**

- A way to represent <u>multiple possible values</u> for a certain definition
  - Not a "real" instruction just a form of bookkeeping needed for SSA



## Where to place Phi-Functions?

- Wherever a variable has multiple possible definitions entering a block
  - Inefficient (and unnecessary!) to consider all possible phi-functions at the start of each block



### Example With a Loop



# Problem 2(a)



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0		
1		
2		
3		
4		
5		
6		



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0		
1		
2		
3		
4		
5		
6		



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0	1, 2, 3, 4, 5, 6	
1		
2		
3		
4		
5		
6		

A node **x** *dominates* a node **y** iff every path from the entry point of the control flow graph to **y** includes **x**.

A node **x** strictly dominates a node **y** iff **x** dominates **y** and  $x \neq y$ 

Need to go through 0 to get through 1, 2, 3, 4, 5, 6 and 0 cannot strictly dominate itself



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0	1, 2, 3, 4, 5, 6	0
1		
2		
3		
4		
5		
6		

A node **Y** is in the *dominance frontier* of node **X** iff **X** dominates an immediate predecessor of **Y** but **X** does not strictly dominate **Y**. A node **0** is in the *dominance frontier* of node **0** iff **0** dominates an immediate predecessor **(6)** of **0** but **0** does not strictly dominate 0

0 dominates 6, 6 is an immediate predecessor of 0, 0 does not strictly dominate 0



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0	1, 2, 3, 4, 5, 6	0
1		
2		
3		
4		
5		
6		



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0	1, 2, 3, 4, 5, 6	0
1	Ø	
2		
3		
4		
5		
6		

A node **x** dominates a node **y** iff every path from the entry point of the control flow graph to **y** includes **x**.

A node **x** strictly dominates a node **y** iff **x** dominates **y** and  $x \neq y$ 

1 does not dominate 6 because there is a path from 5 that doesn't include 1. 1 does not strictly dominate itself



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0	1, 2, 3, 4, 5, 6	0
1	Ø	1,6
2		
3		
4		
5		
6		

A node  $\mathbf{Y}$  is in the *dominance frontier* of node  $\mathbf{x}$  iff  $\mathbf{x}$  dominates an immediate predecessor of  $\mathbf{Y}$  but  $\mathbf{x}$  does not strictly dominate  $\mathbf{Y}$ .

X = 1, Y = 6, 1 dominates 1, 1 is an immediate predecessor of 6, 1 does not strictly dominate 6

X = 1, Y = 1, 1 dominates 1, 1 is an immediate predecessor of 1, 1 does not strictly dominate 1



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0	1, 2, 3, 4, 5, 6	0
1	ø	1,6
2		
3		
4		
5		
6		



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0	1, 2, 3, 4, 5, 6	0
1	Ø	1,6
2	3, 4, 5	
3		
4		
5		
6		

A node **x** *dominates* a node **y** iff every path from the entry point of the control flow graph to **y** includes **x**.

A node **x** strictly dominates a node **y** iff **x** dominates **y** and  $x \neq y$ 

Need to go through 2 to get through 3, 4, 5 and 2 cannot strictly dominate itself



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0	1, 2, 3, 4, 5, 6	0
1	Ø	1,6
2	3, 4, 5	6
3		
4		
5		
6		

A node **Y** is in the *dominance frontier* of node **x** iff **x** dominates an immediate predecessor of **Y** but **x** does not strictly dominate **Y**.

X = 2, Y = 6, 2 dominates 5, 5 is an immediate predecessor of 6, 2 does not strictly dominate 6



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0	1, 2, 3, 4, 5, 6	0
1	Ø	1,6
2	3, 4, 5	6
3	Ø	5
4		
5		
6		

3 does not strictly dominate 5 (path through 4) and therefore does not strictly dominate anything else

3 dominates 3, 3 is an immediate predecessor of 5, 3 does not strictly dominate 5



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0	1, 2, 3, 4, 5, 6	0
1	Ø	1,6
2	3, 4, 5	6
3	Ø	5
4	Ø	5
5		
6		

Same as previous slide but with 4 instead of 3



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0	1, 2, 3, 4, 5, 6	0
1	ø	1,6
2	3, 4, 5	6
3	ø	5
4	ø	5
5	Ø	6
6		

5 does not strictly dominate 6 (path through 1) and therefore does not strictly dominate anything else

5 dominates 5, 5 is an immediate predecessor of 6, 5 does not strictly dominate 6



NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0	1, 2, 3, 4, 5, 6	0
1	Ø	1,6
2	3, 4, 5	6
3	ø	5
4	ø	5
5	Ø	6
6	Ø	0

6 does not strictly dominate 0 (path through 0) and therefore does not strictly dominate anything else

6 dominates 6, 6 is an immediate predecessor of 0, 6 does not strictly dominate 0

# Problem 2(b)

# **Converting to SSA**



Compute the dominance frontier of each node





Determine which variables need merging in each node



Assign numbers to definitions and add phi functions



### Step 1: Dominance Frontiers

NODE	STRICTLY DOMINATES	DOMINANCE FRONTIER
0	1, 2, 3, 4, 5, 6	0
1	ø	1, 6
2	3, 4, 5	6
3	ø	5
4	ø	5
5	ø	6
6	ø	0

# **Converting to SSA**



Compute the dominance frontier of each node





Determine which variables need merging in each node



We will compute using the dominance frontiers



Assign numbers to definitions and add phi functions



### **Step 2**: Determine Necessary Merges

**ITERATION 1**: Each node in the dominance frontier of node X will merge any definitions created in node X.





### **Step 2**: Determine Necessary Merges

**ITERATION 2**: Each merge will create a new definition, which may need merging again.





### **Step 2**: Determine Necessary Merges

**ITERATION 3**: Each merge will create a new definition, which may need merging again.



# **Converting to SSA**



Compute the dominance frontier of each node





Determine which variables need merging in each node





Assign numbers to definitions and add phi functions



Place phi functions first, then increment subscripts

Merges go first, and each successive definition of a variable should increment its index by 1.



Note: these subscripts determined after doing the rest of the CFG!

Merges go first, and each successive definition of a variable should increment its index by 1.



*Note: must merge its own (later) definition because of the back-edge!* 

Merges go first, and each successive definition of a variable should increment its index by 1.

Nothing to merge

Merges go first, and each successive definition of a variable should increment its index by 1.



Nothing to merge

Merges go first, and each successive definition of a variable should increment its index by 1.

$$\mathbf{B_4} \quad \mathbf{d} = \mathbf{b} + 1 \qquad \qquad \mathbf{B_4} \quad \mathbf{d}_4 = \mathbf{b}_2 + 1$$

Nothing to merge

Merges go first, and each successive definition of a variable should increment its index by 1.

$$\mathbf{B}_{5} \ \boxed{\mathbf{c} = \mathbf{d} >> 4} \qquad \qquad \mathbf{B}_{5} \ \boxed{\mathbf{B}_{5}} \ \boxed{\mathbf{B}_{5}$$

Merges go first, and each successive definition of a variable should increment its index by 1.



