#### CSE 401/M501 – Compilers

LR Parsing Spring 2022

## Agenda

- LR Parsing
- Table-driven Parsers
- Parser States
- Shift-Reduce and Reduce-Reduce conflicts

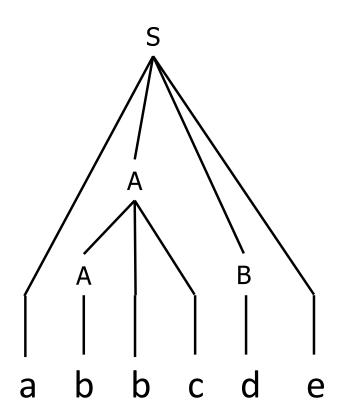
### **Bottom-Up Parsing**

- Idea: Read the input left to right
- Whenever we've matched the right hand side of a production, reduce it to the appropriate non-terminal and add that
   Opposite of "production" is "reduction"
- The upper edge of this partial parse tree is known as the *frontier*

### Example

- Grammar
  - S ::= aABe A ::= Abc | b B ::= d

Bottom-up Parse



# LR(1) Parsing

- We'll look at LR(1) parsers
  - Left to right scan, Rightmost derivation, 1 symbol
     lookahead
  - Almost all practical programming languages have an LR(1) grammar
  - LALR(1), SLR(1), etc. subsets of LR(1)
    - LALR(1) can parse most real languages, tables are more compact, and is used by YACC/Bison/CUP/etc.

## LR Parsing in Greek

- The bottom-up parser reconstructs a reverse rightmost derivation
- Given the rightmost derivation

 $S => \beta_1 => \beta_2 => \dots => \beta_{n-2} => \beta_{n-1} => \beta_n = w$ 

the parser will first discover  $\beta_{n-1} = \beta_n$ , then  $\beta_{n-2} = \beta_{n-1}$ , etc.

- Parsing terminates when
  - $-\beta_1$  reduced to *S* (start symbol, success), or
  - No match can be found (syntax error)

### How Do We Parse With This?

- Key: given what we've already seen and the next input symbol (the lookahead), decide what to do.
- Choices:
  - Shift: Advance 1 token further in the input
  - Reduce: Perform a reduction
- Can reduce  $A \Rightarrow \beta$  if both of these hold:
  - $-A ::= \beta$  is a valid production
  - $-A \Rightarrow \beta$  is a step in *this* rightmost derivation
- This is known as a *shift-reduce* parser

## **Sentential Forms**

- If S ⇒\* α, the string α is called a sentential form of the grammar. (Why the name? It's a sentence if α ∈ Σ\*; "sentential form" generalizes that to include nonterminals.)
- In the derivation  $S \Rightarrow \beta_1 \Rightarrow \beta_2 \Rightarrow ... \Rightarrow \beta_{n-2} \Rightarrow \beta_{n-1} \Rightarrow \beta_n = w$ each of the  $\beta_i$  are sentential forms (and  $\beta_n$  is a *sentence*)
- A sentential form in a rightmost derivation is called a right-sentential form (similarly for leftmost and leftsentential)

## Handles

- Informally, a substring of the tree frontier that matches the right side of a production *that is part of the rightmost derivation of the current input string* 
  - Even if  $A::=\beta$  is a production, it is a handle only if  $\beta$ matches the frontier at a point where  $A::=\beta$  was used in *this particular* derivation
  - $-\ \beta$  may appear in many other places in the frontier without being a handle for that particular production
- Bottom-up parsing is all about finding handles

## Handle Examples

• In the derivation

*S* => a*A*Be => a*A*de => a*A*bcde => abbcde

- abbcde is a right sentential form whose handle is
   A::=b at position 2
- aAbcde is a right sentential form whose handle is
   A::=Abc at position 4
  - Note: some books take the left end of the match as the position

## Handles – The Dragon Book Defn.

 Formally, a *handle* of a right-sentential form γ is a production A ::= β and a position in γ where β may be replaced by A to produce the *previous* right-sentential form in the rightmost derivation of γ

# Agenda

- LR Parsing Overview (last time)
  - Sentential forms:  $S \Rightarrow^* \alpha$
  - Handles/Frontier:  $S \Rightarrow_{rm}^{*} \alpha \underline{A} w \Rightarrow_{rm}^{*} \alpha \underline{\beta} w$
- Shift-Reduce Parsing
- Parser DFA Control
- Parser States
- Shift-Reduce and Reduce-Reduce conflicts

## Implementing Shift-Reduce Parsers

- Key Data structures
  - A stack holding the frontier of the tree
  - A string with the remaining input
- Also need to encode the rules that tell what action to take given (a) the state of the stack and (b) the lookahead symbol

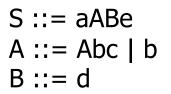
- Typically a table that encodes a finite automaton

### Shift-Reduce Parser Operations

- Shift push the next input symbol onto the stack
- Reduce if the top of the stack is the right side of a handle  $A::=\beta$ , pop the right side  $\beta$ and push the left side A
- Accept announce success
- *Error* syntax error discovered

Aside: Could handle be buried below top of stack? No – you could/should have done the reduction when it was @ top, before burial.

### Shift-Reduce Example



<u>Stack</u>	Input	Action		
\$	abbcde\$	shift		
\$a	bbcde\$	shift		
\$ab	bcde\$	reduce (A→b)	$\rightarrow$ a <u>b</u> bcde	h
\$aA	bcde\$	shift		Found:
\$aAb	cde\$	shift		reverse of a
\$aAbc	de\$	reduce (A→Abc)	→ a <u>Abc</u> de <sup>-</sup>	rightmost
\$aA	de\$	shift		derivation
\$aAd	e\$	reduce (B→d)	, ⇒ aA <u>d</u> e ⊂	Space = top
\$aAB	e\$	shift		of stack, underline
\$aABe	\$	reduce ( <i>S→aABe)</i>	$S \Rightarrow \underline{aABe}^{\prime}$	= handle
\$S	\$	accept		

### How Do We Automate This?

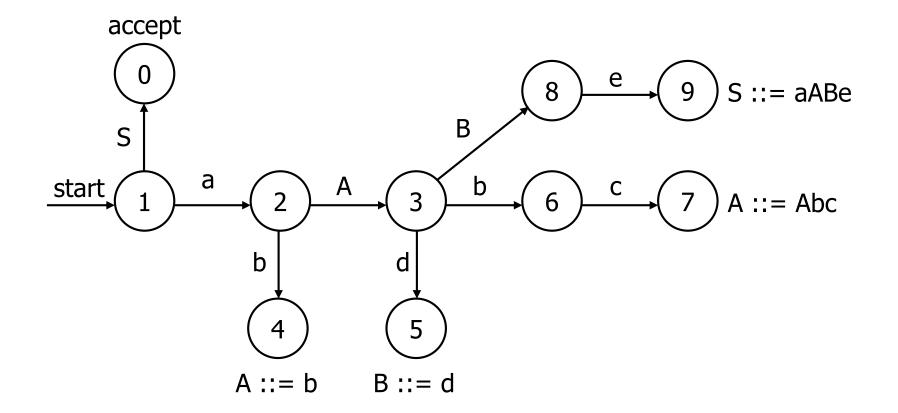
- Cannot use clairvoyance in a real parser (alas...)
- Defn. Viable prefix a prefix of a right-sentential form that can appear on the stack of the shift-reduce parser
  - Equivalent: a prefix of a right-sentential form that does not continue past the rightmost handle of that sentential form
  - In Greek:  $\gamma$  is a *viable prefix* of *G* if there is some derivation S =>\*<sub>rm</sub>  $\alpha Aw =>_{rm} \alpha \beta w$  and  $\gamma$  is a prefix of  $\alpha \beta$ .
  - The occurrence of  $\beta$  in  $\alpha\beta w$  is the right side of a handle of  $\alpha\beta w$

### How Do We Automate This?

- Fact: the set of viable prefixes of a CFG is a regular language(!)
- Idea: Construct a DFA to recognize viable prefixes given the stack and remaining input
  - Perform reductions when we recognize the rhs of handles

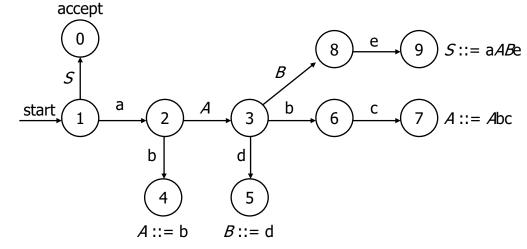
## DFA for prefixes of:

S ::= aABe A ::= Abc | b B ::= d



#### Trace

S ::= aABe A ::= Abc | b B ::= d



Stack	Input
\$	abbcde\$
\$a	bbcde\$
\$ab	bcde\$
\$aA	bcde\$
\$aAb	cde\$
\$aAbc	de\$
\$aA	de\$
\$aAd	e\$
\$aAB	e\$
\$aABe	\$
\$S	\$

### Observations

- Way too much backtracking
  - We want the parser to run in time proportional to the length of the input
- Where the heck did this DFA come from anyway?
  - From the underlying grammar
  - We'll defer construction details for now

# Avoiding DFA Rescanning

- Observation: no need to restart DFA after a shift.
   Stay in the same state and process next token.
- Observation: after a reduction, the contents of the stack are the same as before except for the new nonterminal on top

∴ Scanning the stack will take us through the same transitions as before until the last one

∴ If we record state numbers on the stack, we can back up directly to the appropriate state when we pop the right hand side of a production from the stack

### Stack

 Change the stack to contain alternation of states and symbols from the grammar

 $s_0 X_1 s_1 X_2 s_2 \dots X_n s_n$ 

- State  $s_0$  is the start state
- When we push a symbol on the stack, push the symbol plus the new FA state we reach
- When we reduce, popping the handle will reveal the state of the FA just prior to reading the handle
- Observation: in an actual parser, only the state numbers are needed, since they implicitly contain the symbol information, but for explanations / examples it can help to show both.

## Encoding the DFA in a Table

- A shift-reduce parser's DFA can be encoded in two tables
  - One row for each state
  - *action* table encodes what to do given the current state and the next input symbol
  - *goto* table encodes the transitions to take when we back up into a state after a reduction

# Actions (1)

- Given the current state and input symbol, the main possible actions are
  - si shift the input symbol and state i onto the stack (i.e., shift and move to state i)
  - rj reduce using grammar production j
    - The production tells us how many <symbol, state> pairs to pop off the stack (= length of RHS of production), and LHS nonterminal to push
    - Each production needs a unique number, i.e.,  $A ::= \alpha \mid \beta$  needs to be split into  $A ::= \alpha$  and  $A ::= \beta$

# Actions (2)

- Other possible *action* table entries
  - accept
  - blank no transition syntax error
    - A LR parser will detect an error as soon as possible on a left-to-right scan
    - A real compiler needs to produce an error message, recover, and continue parsing when this happens
      - (Often involves encoding error handling/recovery info in the action table)

### Goto

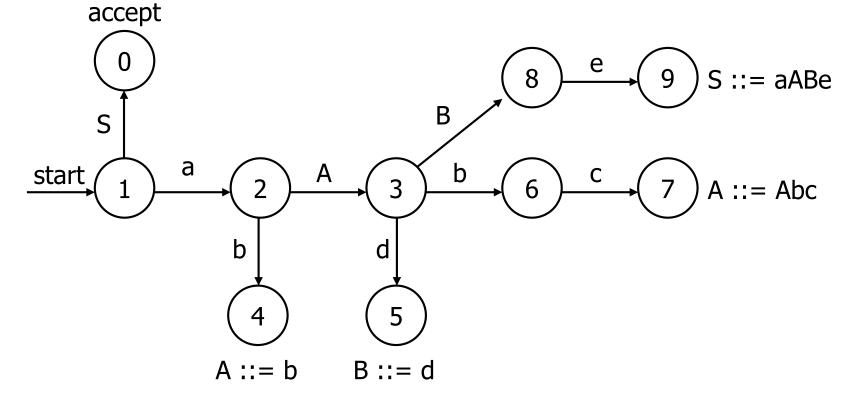
- When a reduction is performed using A ::= β, we pop |β| <symbol, state> pairs from the stack revealing a state *uncovered\_s* on the top of the stack
- Construction guarantees that β actually is on top of stack; parser needn't check this (tho to build AST, you may want to pull info from β's symbols)
- goto[*uncovered\_s*, A] is the new state to push on the stack when reducing production A ::= β (after popping handle β and pushing A)

## Aside: Extra Initial Production

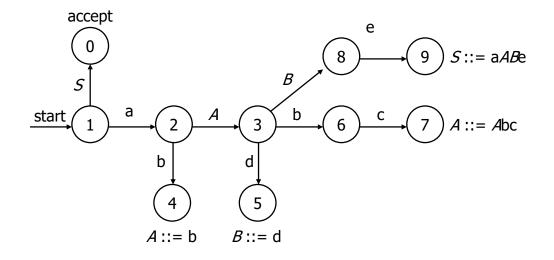
- When we construct the DFA we'll need to add a new production to handle end-of-file (i.e., end-of-input) correctly
- If S is the start state of the original grammar, add an initial production S' ::= S \$
  - \$ represents end-of-file (input)
  - Accept when we've reduced the input to S and there is no more input (i.e., lookahead is \$)

### Reminder: DFA for

S' ::= S \$
 S ::= aABe
 A ::= Abc
 A ::= b
 B ::= d



# LR Parse Table



Ctato		action						goto		
State	а	b	С	d	е	\$	Α	В	S	1
0						асс				2
1	s2								g0	4
2		s4					g3			
3		s6		s5				g8		
4	r3	r3	r3	r3	r3	r3				
5	r4	r4	r4	r4	r4	r4				
6			s7							
7	r2	r2	r2	r2	r2	r2				
8					s9					
9	r1	r1	r1	r1	r1	r1				

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0. S' ::= S \$
1. S ::= aABe
2. A ::= Abc
3. A ::= b
4. B ::= d

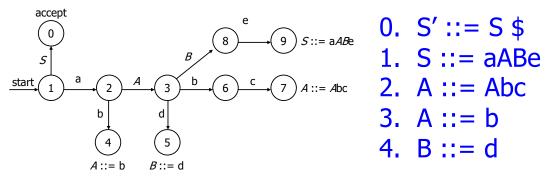
# LR Parsing Algorithm (1)

```
word = scanner.getToken();
while (true) {
    s = top of stack;
    if (action[s, word] = si) {
      push word; push i (state);
      word = scanner.getToken();
    } else if (action[s, word] = rj) {
      pop 2 * length of right side of
      production j (2^*|\beta|);
      uncovered_s = top of stack;
      push left side A of production j;
      push state goto[uncovered_s, A];
    }
```

```
} else if (action[s, word] = accept ) {
    return;
} else {
    // no entry in action table
    report syntax error;
    halt or attempt recovery;
}
```

```
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```

### Example



Stack	Input
\$1	abbcde\$
\$1a2	bbcde\$
\$1a2b4	bcde\$
\$1a2A3	bcde\$
\$1a2A3b6	cde\$
\$1a2A3b6c7	de\$
\$1a2A3	de\$
\$1a2A3d5	e\$
\$1a2A3B8	e\$
\$1a2A3B8e9	\$
\$1SO	\$

C		action						goto		
S	а	b	С	d	е	\$	А	В	S	
0						ас				
1	s2								g0	
2		s4					g3			
3		s6		s5				g8		
4	r3	r3	r3	r3	r3	r3				
5	r4	r4	r4	r4	r4	r4				
6			s7							
7	r2	r2	r2	r2	r2	r2				
8					s9					
9	r1	r1	r1	r1	r1	r1				

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# Agenda

- LR Parsing Overview (last Wed)
  - Sentential forms:  $S \Rightarrow^* \alpha$
  - Handles/Frontier:  $S \Rightarrow_{rm}^{*} \alpha \underline{A} w \Rightarrow_{rm}^{*} \alpha \underline{\beta} w$
- Shift-Reduce Parsing
- Parser DFA Control
   Viable prefixes
   (last Fri)
- Parser States
- Shift-Reduce and Reduce-Reduce conflicts

### **LR States**

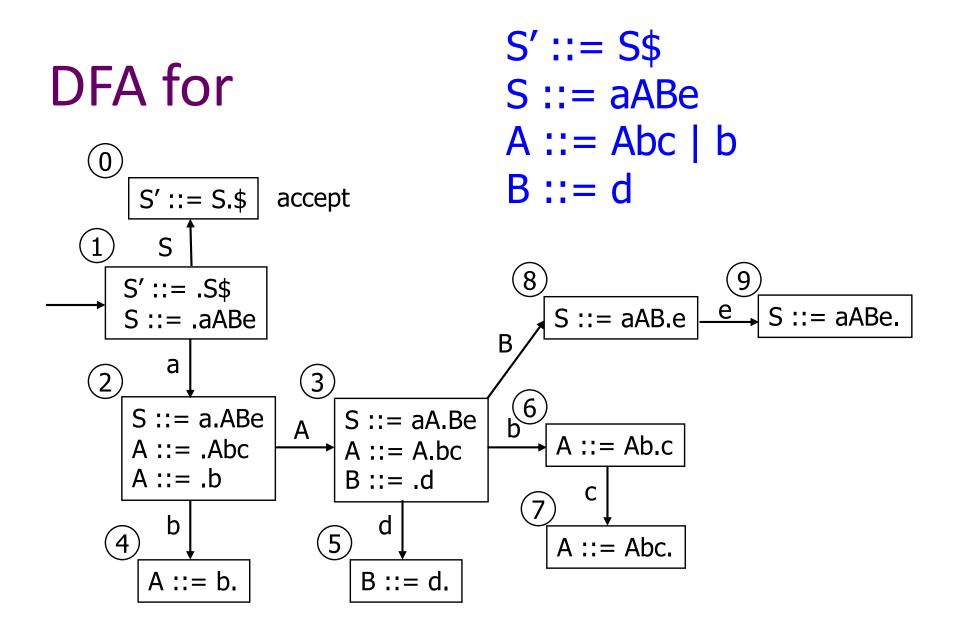
- Idea is that each state encodes
  - The set of all possible productions that we could be looking at, given the current state of the parse, and
  - Where we are in the right hand side of each of those productions

#### Items

- An *item* is a production with a dot in the right hand side
- Example: Items for production A ::= X Y

$$A ::= . X Y$$
  
 $A ::= X . Y$   
 $A ::= X Y .$ 

Idea: The dot represents a position in the production – partial match to rhs



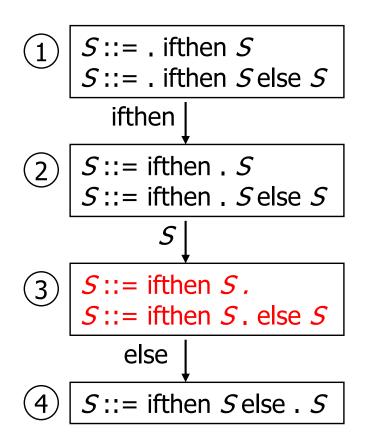
## Problems with Grammars

- Non-LR Grammars cause problems when constructing an LR parser (that's how you know it's not an LR grammar). Specifically:
  - Shift-reduce conflicts
  - Reduce-reduce conflicts
- I.e., arrive at a situation where two (or more) conflicting actions called-for.

### Shift-Reduce Conflicts

- Situation: both a shift and a reduce are possible at a given point in the parse (equivalently: in a particular state of the DFA)
- Classic example: if-else statement
   S ::= ifthen S | ifthen S else S

#### Parser States for



*S* ::= ifthen *S S* ::= ifthen *S* else *S*

- State 3 has a shiftreduce conflict
  - Can shift past else into state 4 (s4)
  - Can reduce (r1)

S ::= ifthen S

(Note: other S ::= . ifthen items not included in states 2,4 to save space)

## Solving Shift-Reduce Conflicts

- Option 1: Fix the grammar
  - Done in Java reference grammar, others
- Option 2: Use a parser tool with a "longest match" rule – i.e., if there is a conflict, choose to shift instead of reduce
  - Does exactly what we want for if-else case
  - Guideline: a few shift-reduce conflicts are fine, but be sure they do what you want (and that this behavior is guaranteed by the tool specification)

### Reduce-Reduce Conflicts

- Situation: two different reductions are possible in a given state
- Contrived example

### Parser States for

1. S ::= A2. S ::= B3. A ::= x4. B ::= x

$$\begin{array}{c} 1 \\ S ::= .A \\ S ::= .B \\ A ::= .x \\ B ::= .x \\ \end{array}$$

$$\begin{array}{c} x \\ A ::= x \\ B ::= x \\ \end{array}$$

• State 2 has a reducereduce conflict (r3, r4)

# Handling Reduce-Reduce Conflicts

- These normally indicate a serious problem with the grammar.
- Fixes
  - Use a different kind of parser generator that takes lookahead information into account when constructing the states

- 1. S ::= Aa2. S ::= Bb3. A ::= x4. B ::= x
- Most practical tools (Yacc, Bison, CUP, et al) do this
- Fix the grammar

## Another Reduce-Reduce Conflict

 Suppose the grammar tries to separate arithmetic and boolean expressions

> expr ::= aexp | bexp aexp ::= aexp \* aident | aident bexp ::= bexp && bident | bident aident ::= id bident ::= id

• This will create a reduce-reduce conflict (try it and see)

# **Covering Grammars**

- A solution is to merge *aident* and *bident* into a single non-terminal (or use *id* in place of *aident* and *bident* everywhere they appear)
- This is a *covering grammar* 
  - Will generate some programs that are not generated by the original grammar
  - Use the type checker or other static semantic analysis to weed out illegal programs later

### **Coming Attractions**

- Constructing LR tables
  - We'll present a simple version (SLR(0)) in lecture, then talk about extending it to LR(1) and then a little bit about how this relates to LALR(1) used in most parser generators
- LL parsers and recursive descent
- Continue reading ch. 3