CSE 401/M501 – Compilers

LR Parsing Hal Perkins Autumn 2021

Administrivia

- HW1 due last night, but still have a late day or two if you need it (but try to save them)
- Project:
 - Scanner due Thursday night, but please shake down infrastructure well before then
 - DO NOT start on the parser yet just edit token classes in the .cup file (and any other small edits you need to get a clean build)
 - If you're still looking for a partner / need a project repo set up, send email to cse401-staff@cs
- HW2: LR parsing and grammars due in 2 weeks, but lectures aren't quite far enough along. Will post early next week.

Agenda

- LR Parsing
- Table-driven Parsers
- Parser States
- Shift-Reduce and Reduce-Reduce conflicts

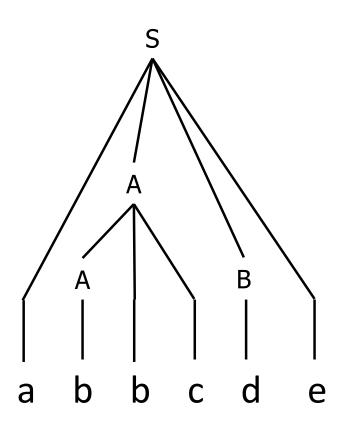
Bottom-Up Parsing

- Idea: Read the input left to right
- Whenever we've matched the right hand side of a production, reduce it to the appropriate non-terminal and add that non-terminal to the parse tree
- The upper edge of this partial parse tree is known as the *frontier*

Example

- Grammar
 - S ::= aABe A ::= Abc | b B ::= d

Bottom-up Parse



LR(1) Parsing

- We'll look at LR(1) parsers
 - Left to right scan, Rightmost derivation, 1 symbol lookahead
 - Almost all practical programming languages have an LR(1) grammar
 - LALR(1), SLR(1), etc. subsets of LR(1)
 - LALR(1) can parse most real languages, tables are more compact, and is used by YACC/Bison/CUP/etc.

LR Parsing in Greek

- The bottom-up parser reconstructs a reverse rightmost derivation
- Given the rightmost derivation $S =>\beta_1 =>\beta_2 =>... =>\beta_{n-2} =>\beta_n = w$ the parser will first discover $\beta_{n-1} =>\beta_n$, then $\beta_{n-2} =>\beta_{n-1}$, etc.
- Parsing terminates when
 - $-\beta_1$ reduced to *S* (start symbol, success), or
 - No match can be found (syntax error)

How Do We Parse with This?

- Key: given what we've already seen and the next input symbol (the lookahead), decide what to do.
- Choices:
 - Perform a reduction
 - Look ahead further
- Can reduce $A => \beta$ if both of these hold:
 - $A => \beta$ is a valid production
 - $-A =>\beta$ is a step in *this* rightmost derivation
- This is known as a *shift-reduce* parser

Sentential Forms

- If S =>* α, the string α is called a sentential form of the grammar
- In the derivation $S =>\beta_1 =>\beta_2 =>... =>\beta_{n-2} =>\beta_{n-1} =>\beta_n = w$ each of the β_i are sentential forms
- A sentential form in a rightmost derivation is called a right-sentential form (similarly for leftmost and leftsentential)

Handles

- Informally, a substring of the tree frontier that matches the right side of a production *that is part of the rightmost derivation of the current input string*
 - Even if $A::=\beta$ is a production, it is a handle only if β matches the frontier at a point where $A::=\beta$ was used in *this particular* derivation
 - $-\beta$ may appear in many other places in the frontier without being a handle for that particular production
- Bottom-up parsing is all about finding handles

Handle Examples

• In the derivation

S => a*A*Be => a*A*de => a*A*bcde => abbcde

- abbcde is a right sentential form whose handle is
 A::=b at position 2
- aAbcde is a right sentential form whose handle is
 A::=Abc at position 4
 - Note: some books take the left of the match as the position

Handles – The Dragon Book Defn.

 Formally, a *handle* of a right-sentential form γ is a production A ::= β and a position in γ where β may be replaced by A to produce the previous right-sentential form in the rightmost derivation of γ

Implementing Shift-Reduce Parsers

- Key Data structures
 - A stack holding the frontier of the tree
 - A string with the remaining input
- We also need something to encode the rules that tell us what action to take given the state of the stack and the lookahead symbol
 - Typically a table that encodes a finite automata

Shift-Reduce Parser Operations

- *Reduce* if the top of the stack is the right side of a handle A::=β, pop the right side β and push the left side A
- Shift push the next input symbol onto the stack
- *Accept* announce success
- *Error* syntax error discovered

Shift-Reduce Example

S ::= a*AB*e *A* ::= *A*bc | b *B* ::= d

<u>Stack</u>	Input	Action
\$	abbcde\$	shift
\$a	bbcde\$	shift
\$ab	bcde\$	reduce
\$aA	bcde\$	shift
\$aAb	cde\$	shift
\$aAbc	de\$	reduce
\$aA	de\$	shift
\$aAd	e\$	reduce
\$aAB	e\$	shift
\$aABe	\$	reduce
\$S	\$	accept

How Do We Automate This?

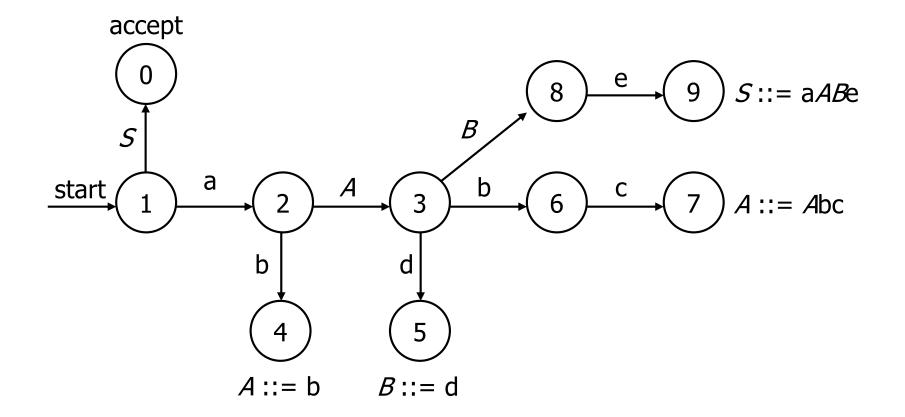
- Cannot use clairvoyance in a real parser (alas...)
- Defn. Viable prefix a prefix of a right-sentential form that can appear on the stack of the shift-reduce parser
 - Equivalent: a prefix of a right-sentential form that does not continue past the rightmost handle of that sentential form
 - In Greek: γ is a *viable prefix* of *G* if there is some derivation S =>*_{rm} $\alpha Aw =>_{rm} \alpha \beta w$ and γ is a prefix of $\alpha \beta$.
 - The occurrence of β in $\alpha\beta w$ is the right side of a handle of $\alpha\beta w$

How Do We Automate This?

- Fact: the set of viable prefixes of a CFG is a regular language(!)
- Idea: Construct a DFA to recognize viable prefixes given the stack and remaining input
 - Perform reductions when we recognize the rhs of handles

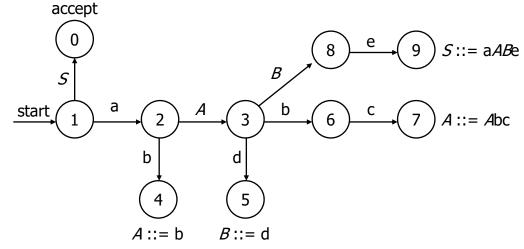
DFA for prefixes of

S :::= a*AB*e *A* ::= *A*bc | b *B* ::= d



Trace

S ::= a*AB*e *A* ::= *A*bc | b *B* ::= d



Stack	Input
\$	abbcde\$
\$a	bbcde\$
\$ab	bcde\$
\$aA	bcde\$
\$aAb	cde\$
\$aAbc	de\$
\$aA	de\$
\$aAd	e\$
\$aAB	e\$
\$aABe	\$
\$S	\$

Observations

- Way too much backtracking
 - We want the parser to run in time proportional to the length of the input
- Where the heck did this DFA come from anyway?
 - From the underlying grammar
 - We'll defer construction details for now

Avoiding DFA Rescanning

- Observation: no need to restart DFA after a shift. Stay in the same state and process next token.
- Observation: after a reduction, the contents of the stack are the same as before except for the new non-terminal on top

... Scanning the stack will take us through the same transitions as before until the last one

∴ If we record state numbers on the stack, we can back up directly to the appropriate state when we pop the right hand side of a production from the stack

Stack

- Change the stack to contain pairs of states and symbols from the grammar
 - $s_0 X_1 s_1 X_2 s_2 \dots X_n s_n$
 - State s_0 is the start state
 - When we push a symbol on the stack, push the symbol plus the new FA state we reach
 - When we reduce, popping the handle will reveal the state of the FA just prior to reading the handle
- Observation: in an actual parser, only the state numbers are needed, since they implicitly contain the symbol information, but for explanations / examples it can help to show both.

Encoding the DFA in a Table

- A shift-reduce parser's DFA can be encoded in two tables
 - One row for each state
 - *action* table encodes what to do given the current state and the next input symbol
 - *goto* table encodes the transitions to take when we back up into a state after a reduction

Actions (1)

- Given the current state and input symbol, the main possible actions are
 - si shift the input symbol and state i onto the stack (i.e., shift and move to state i)
 - rj reduce using grammar production j
 - The production number tells us how many <symbol, state> pairs to pop off the stack (= number of symbols on rhs of production)
 - Each production needs a unique number, i.e., A ::= α | β needs to be split into A ::= α and A ::= β

Actions (2)

- Other possible *action* table entries
 - accept
 - blank no transition syntax error
 - A LR parser will detect an error as soon as possible on a left-to-right scan
 - A real compiler needs to produce an error message, recover, and continue parsing when this happens
 - (Often involves encoding error handling/recovery info in the action table)

Goto

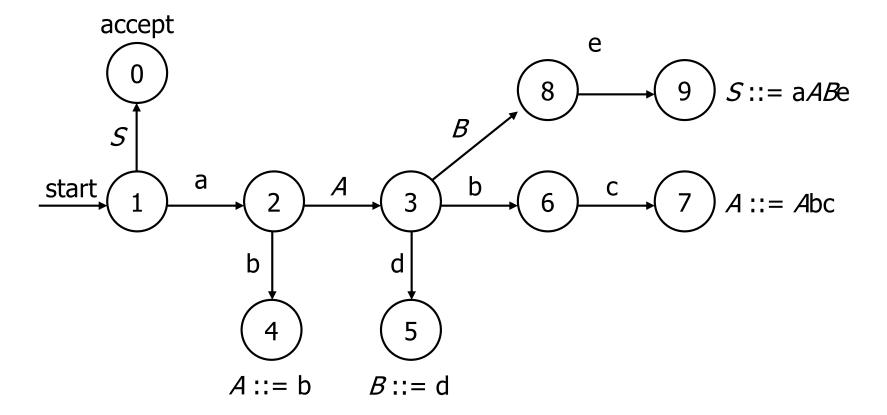
- When a reduction is performed using A ::= β, we pop |β| <symbol, state> pairs from the stack revealing a state *uncovered_s* on the top of the stack
- goto[*uncovered_s*, A] is the new state to push on the stack when reducing production A ::= β (after popping handle β and pushing A)

Aside: Extra Initial Production

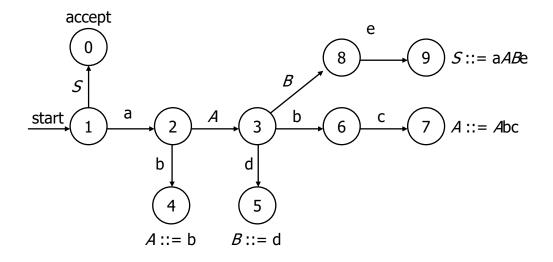
- When we construct the DFA we'll need to add a new production to handle end-of-file (i.e., end-of-input) correctly
- If S is the start state of the original grammar,
 add an initial production S' ::= S \$
 - \$ represents end-of-file (input)
 - Accept when we've reduced the input to S and there is no more input (i.e., lookahead is \$)

Reminder: DFA for

S' ::= S\$
 S ::= aABe
 A ::= Abc
 A ::= b
 B ::= d



LR Parse Table



State	action						goto		
State	а	b	С	d	е	\$	А	В	S
0						асс			
1	s2								g0
2		s4					g3		
3		s6		s5				g8	
4	r3	r3	r3	r3	r3	r3			
5	r4	r4	r4	r4	r4	r4			
6			s7						
7	r2	r2	r2	r2	r2	r2			
8					s9				
9	r1	r1	r1	r1	r1	r1			

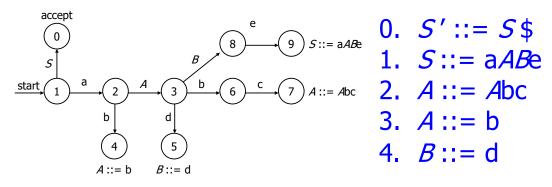
S'::= S\$
 S::= aABe
 A ::= Abc
 A ::= b
 B ::= d

LR Parsing Algorithm (1)

```
word = scanner.getToken();
while (true) {
    s = top of stack;
    if (action[s, word] = si) {
      push word; push i (state);
      word = scanner.getToken();
    } else if (action[s, word] = rj) {
      pop 2 * length of right side of
     production j (2^*|\beta|);
      uncovered s = top of stack;
      push left side A of production j ;
      push state goto[uncovered s, A];
```

```
} else if (action[s, word] = accept ) {
    return;
} else {
    // no entry in action table
    report syntax error;
    halt or attempt recovery;
}
```

Example



Stack	Input
\$1	abbcde\$
\$1a2	bbcde\$
\$1a2b4	bcde\$
\$1a2A3	bcde\$
\$1a2A3b6	cde\$
\$1a2A3b6c7	de\$
\$1a2A3	de\$
\$1a2A3d5	e\$
\$1a2A3B8	e\$
\$1a2A3B8e9	\$
\$1SO	\$

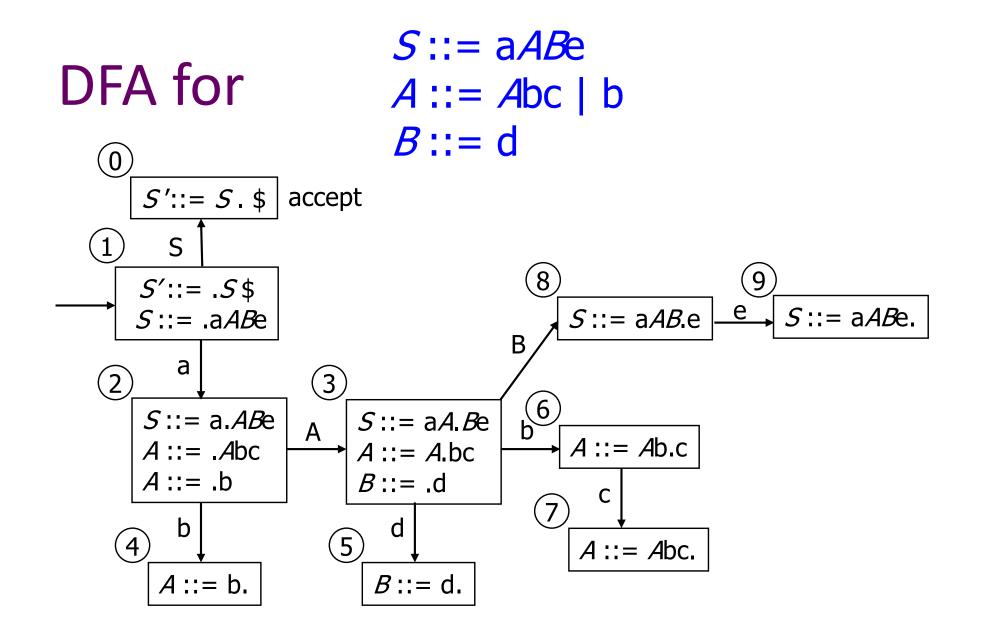
-										
	S	action						goto		
		а	b	С	d	е	\$	А	В	S
	0						ас			
	1	s2								g0
	2		s4					g3		
	3		s6		s5				g8	
	4	r3	r3	r3	r3	r3	r3			
	5	r4	r4	r4	r4	r4	r4			
	6			s7						
	7	r2	r2	r2	r2	r2	r2			
	8					s9				
	9	r1	r1	r1	r1	r1	r1			

LR States

- Idea is that each state encodes
 - The set of all possible productions that we could be looking at, given the current state of the parse, and
 - Where we are in the right hand side of each of those productions

Items

- An *item* is a production with a dot in the right hand side
- Example: Items for production A ::= X Y
 - A ::= . X YA ::= X . YA ::= X Y.
- Idea: The dot represents a position in the production



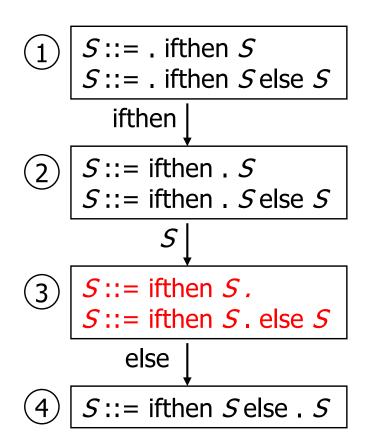
Problems with Grammars

- Grammars can cause problems when constructing a LR parser
 - Shift-reduce conflicts
 - Reduce-reduce conflicts

Shift-Reduce Conflicts

- Situation: both a shift and a reduce are possible at a given point in the parse (equivalently: in a particular state of the DFA)
- Classic example: if-else statement
 S ::= ifthen S | ifthen S else S

Parser States for



S ::= ifthen *S S* ::= ifthen *S* else *S*

- State 3 has a shiftreduce conflict
 - Can shift past else into state 4 (s4)
 - Can reduce (r1)

S ::= ifthen S

(Note: other S ::= . ifthen items not included in states 2-4 to save space)

Solving Shift-Reduce Conflicts

- Fix the grammar
 - Done in Java reference grammar, others
- Use a parse tool with a "longest match" rule i.e., if there is a conflict, choose to shift instead of reduce
 - Does exactly what we want for if-else case
 - Guideline: a few shift-reduce conflicts are fine, but be sure they do what you want (and that this behavior is guaranteed by the tool specification)

Reduce-Reduce Conflicts

- Situation: two different reductions are possible in a given state
- Contrived example

Parser States for

1. S ::= A2. S ::= B3. A ::= x4. B ::= x

(1)
$$S ::= .A$$

 $S ::= .B$
 $A ::= .x$
 $B ::= .x$
(2) X
 $A ::= x.$
 $B ::= x.$

• State 2 has a reducereduce conflict (r3, r4)

Handling Reduce-Reduce Conflicts

- These normally indicate a serious problem with the grammar.
- Fixes
 - Use a different kind of parser generator that takes lookahead information into account when constructing the states
 - Most practical tools (Yacc, Bison, CUP, et al) do this
 - Fix the grammar

Another Reduce-Reduce Conflict

• Suppose the grammar tries to separate arithmetic and boolean expressions

expr ::= aexp | bexp aexp ::= aexp * aident | aident bexp ::= bexp && bident | bident aident ::= id bident ::= id

• This will create a reduce-reduce conflict

Covering Grammars

- A solution is to merge *aident* and *bident* into a single non-terminal (or use *id* in place of *aident* and *bident* everywhere they appear)
- This is a *covering grammar*
 - Will generate some programs that are not generated by the original grammar
 - Use the type checker or other static semantic analysis to weed out illegal programs later

Coming Attractions

- Constructing LR tables
 - We'll present a simple version (SLR(0)) in lecture, then talk about extending it to LR(1) and then a little bit about how this relates to LALR(1) used in most parser generators
- LL parsers and recursive descent
- Continue reading ch. 3