# CSE 390Z: Mathematics for Computation Workshop

## QuickCheck: Number Theory Proof Solutions (due Monday, November 2)

Please submit a response to the following questions on Gradescope. We do not grade on accuracy, so please submit your best attempt. You may either typeset your responses or hand-write them. Note that hand-written solutions must be legible to be graded.

We have created **this template** if you choose to typeset with Latex. **This guide** has specific information about scanning and uploading pdf files to Gradescope.

## 0. Mod Madness

Prove that if $n \mid m$, where $n$ and $m$ are integers greater than $1$, and if $a \equiv b \pmod{m}$, where $a$ and $b$ are integers, then $a \equiv b \pmod{n}$. Write an English proof of the statement.

**Solution:**

Let integers $n > 1, m > 1$ be arbitrary and integers $a, b$ be arbitrary integers. Suppose $n \mid m$ and $a \equiv b \pmod{m}$. By definition of divides, we have $m = kn$ for some integer $k$. By definition of congruence, we have $m \mid a - b$. By definition of divides, this means that $a - b = mj$ for some integer $j$. Combining the two equations, we see that $a - b = (knj) = n(kj)$. Since $k, j$ are both integers, $kj$ is an integer. By definition of divides, we have $n \mid a - b$. By definition of congruence, we have $a \equiv b \pmod{n}$. Since $n, m, a, b$ were arbitrary, we have shown that for all integers $a, b, n, m$ with $n, m > 1$, if $n \mid m$ and $a \equiv b \pmod{m}$, then $a \equiv b \pmod{n}$.

## 1. Video Solution

Watch **this video** on the solution **after** making an initial attempt. Then, answer the following questions.

(a) What is one thing you took away from the video solution?

(b) What topic from the quick check or lecture would you most like to review in workshop?