

# CSE 390Z: Mathematics for Computation Workshop

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## QuickCheck: Number Theory Proof Solutions

Please submit a response to the following questions on Gradescope. We do not grade on accuracy, so please submit your best attempt. You may either typeset your responses or hand-write them. Note that hand-written solutions must be legible to be graded.

We have created **this template** if you choose to typeset with Latex. **This guide** has specific information about scanning and uploading pdf files to Gradescope.

### 0. Mod Madness

Prove that if  $n \mid m$ , where  $n$  and  $m$  are integers greater than 1, and if  $a \equiv b \pmod{m}$ , where  $a$  and  $b$  are integers, then  $a \equiv b \pmod{n}$ . Write an English proof of the statement.

#### Solution:

Let integers  $n > 1, m > 1$  be arbitrary and integers  $a, b$  be arbitrary. Suppose  $n \mid m$  and  $a \equiv b \pmod{m}$ . By definition of divides, we have  $m = kn$  for some integer  $k$ . By definition of congruence, we have  $m \mid a - b$ . By definition of divides, this means that  $a - b = mj$  for some integer  $j$ . Combining the two equations, we see that  $a - b = (knj) = n(kj)$ . By definition of divides, we have  $n \mid a - b$ . By definition of congruence, we have  $a \equiv_n b$ . Since  $n, m, a, b$  were arbitrary, we have shown that if  $n \mid m$  and  $a \equiv b \pmod{m}$ , then  $a \equiv b \pmod{n}$ .

### 1. Video Solution

Watch **this video** on the solution **after** making an initial attempt. Then, answer the following questions.

- (a) What is one thing you took away from the video solution?
- (b) What topic from the quick check or lecture would you most like to review in workshop?