QuickCheck: Relations Solutions

Please submit a response to the following questions on Gradescope. We do not grade on accuracy, so please submit your best attempt. You may either typeset your responses or hand-write them. Note that hand-written solutions must be legible to be graded.

We have created **this template** if you choose to typeset with Latex. **This guide** has specific information about scanning and uploading pdf files to Gradescope.

0. Relations

(a) Consider the relation $R \subseteq \mathbb{Z} \times \mathbb{Z}$ defined by $(a, b) \in R$ iff a < b. Determine if R is reflexive, symmetric, antisymmetric, and/or transitive. If a relation has a property, explain why. If not, state a counterexample.

Solution:

- Reflexive: No. For example, $(0,0) \notin R$.
- Symmetric: No. For example, $(0,1) \in R$ but $(1,0) \notin R$.
- Antisymmetric: Yes. Suppose (a, b) ∈ R and a ≠ b. Then a < b. Then by properties of less than, it is not possible for b < a. So (b, a) ∉ R.
- Transitive: Yes. Suppose $(a, b) \in R$ and $(b, c) \in R$. Then a < b and b < c. So a < c. So $(a, c) \in R$.

(b) Given an example of a relation that is neither symmetric nor antisymmetric.

Solution:

Consider the relation $R = \{(0,1), (1,0), (1,2)\}$. This is not symmetric, because $(1,2) \in R$ but $(2,1) \notin R$. This is also not antisymmetric, because $(0,1) \in R$ and $(1,0) \in R$.

1. Video Solution

Watch this solution video after making an initial attempt. Then, answer the following questions.

- (a) What is one thing you took away from the video solution?
- (b) What topic from the quick check or lecture would you most like to review in workshop?