Lecture 18 (Fri 11/07/2008)

- Lab #2 Hardware Due Fri Nov 7 (TODAY) at 5pm
- Lab #3 Software Only Due Fri Nov 14 at 5pm
- Caches: Cache Organizations, Spatial Locality, Associativity

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How big is the cache?

For a byte-addressable machine with 16-bit addresses with a cache with the following characteristics:

- It is direct-mapped (as discussed last time)
- Each block holds one byte
- The cache index is the four least significant bits

Two questions:

How many blocks does the cache hold?

4-bit index -> 24 = 16 blocks

How many bits of storage are required to build the cache (e.g., for the data array, tags, etc.)?

tag size = 12 bits (16 bit address - 4 bit index) (12 tag bits + 1 valid bit + 8 data bits) x 16 blocks = 21 bits x 16 = 336 bits

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2

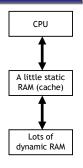
More cache organizations



- Today, we'll explore some alternate cache organizations.
 - How can we take advantage of spatial locality too?
 - How can we reduce the number of potential conflicts?
- We'll first motivate it with a brief discussion about cache performance.

Memory System Performance

- To examine the performance of a memory system, we need to focus on a couple of important factors.
 - How long does it take to send data from the cache to the CPU?
 - How long does it take to copy data from memory into the cache?
 - How often do we have to access main memory?
- There are names for all of these variables.
 - The hit time is how long it takes data to be sent from the cache to the processor. This is usually fast, on the order of 1-3 clock cycles.
 - The miss penalty is the time to copy data from main memory to the cache. This often requires dozens of clock cycles (at least).
 - The miss rate is the percentage of misses.



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Performance example

 Assume that 33% of the instructions in a program are data accesses. The cache hit ratio is 97% and the hit time is one cycle, but the miss penalty is 20 cycles.

AMAT = Hit time + (Miss rate x Miss penalty) =

How can we reduce miss rate?

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Average memory access time

• The average memory access time, or AMAT, can then be computed.

AMAT = Hit time + (Miss rate x Miss penalty)

This is just averaging the amount of time for cache hits and the amount of time for cache misses.

- How can we improve the average memory access time of a system?
 - Obviously, a lower AMAT is better.
 - Miss penalties are usually much greater than hit times, so the best way to lower AMAT is to reduce the miss penalty or the miss rate.
- However, AMAT should only be used as a general guideline. Remember that execution time is still the best performance metric.

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Performance example

 Assume data accesses only. The cache hit ratio is 97% and the hit time is one cycle, but the miss penalty is 20 cycles.

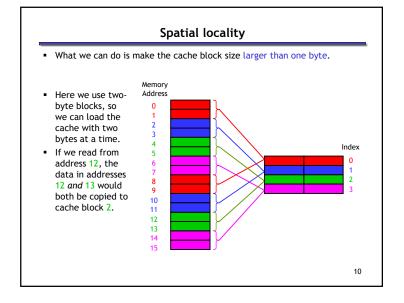
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AMAT = Hit time + (Miss rate x Miss penalty)
= 1 cycle + (3% x 20 cycles)
= 1.6 cycles
```

- If the cache was perfect and never missed, the AMAT would be one cycle. But even with just a 3% miss rate, the AMAT here increases 1.6 times!
- How can we reduce miss rate?

Spatial locality

- One-byte cache blocks don't take advantage of spatial locality, which
 predicts that an access to one address will be followed by an access to a
 nearby address.
- What can we do?

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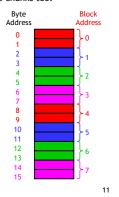


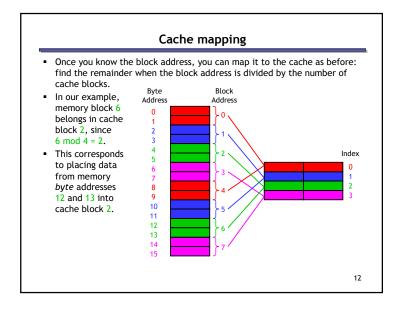
Block addresses

- Now how can we figure out where data should be placed in the cache?
- It's time for block addresses! If the cache block size is 2ⁿ bytes, we can
 conceptually split the main memory into 2ⁿ-byte chunks too.
- To determine the block address of a byte address *i*, you can do the integer division

 $i/2^n$

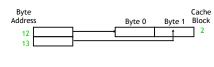
- Our example has two-byte cache blocks, so we can think of a 16-byte main memory as an "8-block" main memory instead.
- For instance, memory addresses 12 and 13 both correspond to block address 6, since
 12 / 2 = 6 and 13 / 2 = 6.





Data placement within a block

- When we access one byte of data in memory, we'll copy its entire block into the cache, to hopefully take advantage of spatial locality.
- In our example, if a program reads from byte address 12 we'll load all of memory block 6 (both addresses 12 and 13) into cache block 2.
- Note byte address 13 corresponds to the same memory block address! So a read from address 13 will also cause memory block 6 (addresses 12 and 13) to be loaded into cache block 2.
- To make things simpler, byte *i* of a memory block is always stored in byte *i* of the corresponding cache block.



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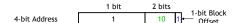
Address (4 bits) Tag Index (2 bits) Address (4 bits) Index Valid Tag Data O Mux 1 Hit Data

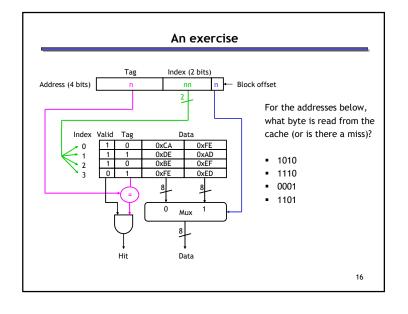
Locating data in the cache

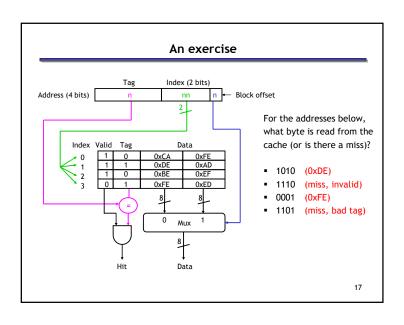
- Let's say we have a cache with 2^k blocks, each containing 2^n bytes.
- We can determine where a byte of data belongs in this cache by looking at its address in main memory.
 - -k bits of the address will select one of the 2^k cache blocks.
 - The lowest n bits are now a block offset that decides which of the 2^n bytes in the cache block will store the data.

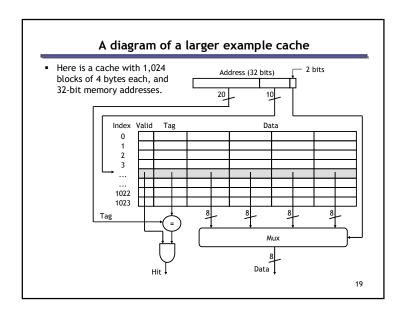


 Our example used a 2²-block cache with 2¹ bytes per block. Thus, memory address 13 (1101) would be stored in byte 1 of cache block 2.









Using arithmetic

 An equivalent way to find the right location within the cache is to use arithmetic again.

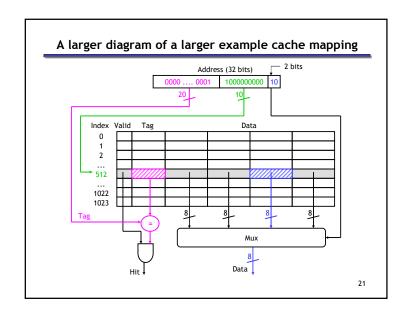
m-bit Address (m-k-n) bits k bits n-bit Block Offset

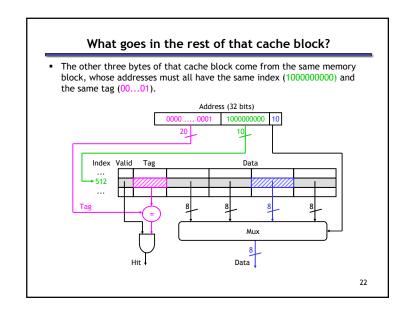
- We can find the index in two steps, as outlined earlier.
 - Do integer division of the address by 2^n to find the block address.
 - Then mod the block address with 2^k to find the index.
- The block offset is just the memory address mod 2ⁿ.
- For example, we can find address 13 in a 4-block, 2-byte per block cache.
 - The block address is 13 / 2 = 6, so the index is then $6 \mod 4 = 2$.
 - The block offset would be 13 mod 2 = 1.

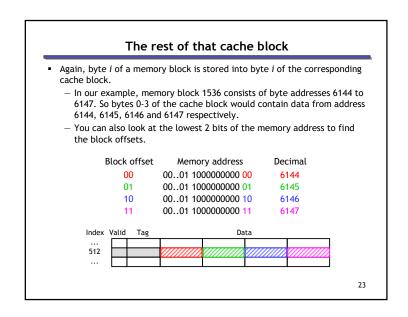
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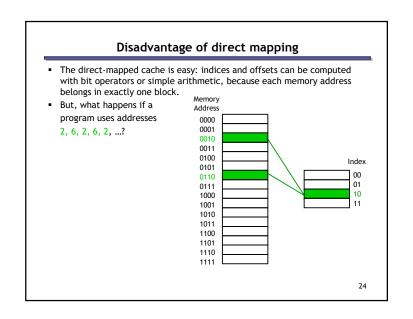
A larger example cache mapping

- Where would the byte from memory address 6146 be stored in this direct-mapped 2¹⁰-block cache with 2²-byte blocks?
- We can determine this with the binary force.
 - 6146 in binary is 00...01 1000 0000 00 10.
 - The lowest 2 bits, 10, mean this is the second byte in its block.
 - The next 10 bits, 1000000000, are the block number itself (512).
- Equivalently, you could use arithmetic instead.
 - The block offset is 6146 mod 4, which equals 2.
 - The block address is 6146/4 = 1536, so the index is 1536 mod 1024, or 512.

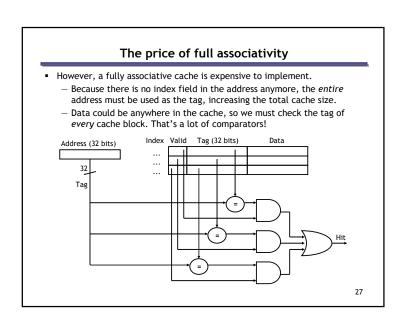








Disadvantage of direct mapping • The direct-mapped cache is easy: indices and offsets can be computed with bit operators or simple arithmetic, because each memory address belongs in exactly one block. Memory However, this isn't really Address flexible. If a program uses 0000 addresses 2, 6, 2, 6, 2, 0001 then each access will result 0010 in a cache miss and a load 0011 0100 into cache block 2. Index 0101 This cache has four blocks, 00 0110 but direct mapping might 01 0111 not let us use all of them. 10 1000 1001 This can result in more 1010 misses than we might like. 1011 1100 1101 1110 1111 25



A fully associative cache

- A fully associative cache permits data to be stored in any cache block, instead of forcing each memory address into one particular block.
 - When data is fetched from memory, it can be placed in any unused block of the cache.
 - This way we'll never have a conflict between two or more memory addresses which map to a single cache block.
- In the previous example, we might put memory address 2 in cache block 2, and address 6 in block 3. Then subsequent repeated accesses to 2 and 6 would all be hits instead of misses.
- If all the blocks are already in use, it's usually best to replace the least recently used one, assuming that if it hasn't used it in a while, it won't be needed again anytime soon.

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Set associativity

- An intermediate possibility is a set-associative cache.
 - The cache is divided into groups of blocks, called sets.
 - Each memory address maps to exactly one set in the cache, but data may be placed in any block within that set.
- If each set has 2^x blocks, the cache is an 2^x-way associative cache.
- Here are several possible organizations of an eight-block cache.

Locating a set associative block

- We can determine where a memory address belongs in an associative cache in a similar way as before.
- If a cache has 2^s sets and each block has 2ⁿ bytes, the memory address can be partitioned as follows.

Address (m bits) Tag Index Block offset

 Our arithmetic computations now compute a set index, to select a set within the cache instead of an individual block.

Block Offset = Memory Address mod 2^n

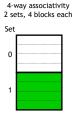
Block Address = Memory Address / 2ⁿ Set Index = Block Address mod 2^s

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Block replacement

- Any empty block in the correct set may be used for storing data.
- If there are no empty blocks, the cache controller will attempt to replace the least recently used block, just like before.
- For highly associative caches, it's expensive to keep track of what's really the least recently used block, so some approximations are used. We won't get into the details.

2-way associativity 4 sets, 2 blocks each Set 0 1 2



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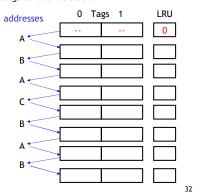
Example placement in set-associative caches

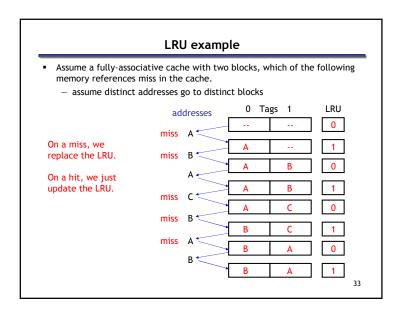
- Where would data from memory byte address 6195 be placed, assuming the eight-block cache designs below, with 16 bytes per block?
- 6195 in binary is 00...0110000 011 0011.
- Each block has 16 bytes, so the lowest 4 bits are the block offset.
- For the 1-way cache, the next three bits (011) are the set index.
 For the 2-way cache, the next two bits (11) are the set index.
 For the 4-way cache, the next one bit (1) is the set index.
- The data may go in *any* block, shown in green, within the correct set.

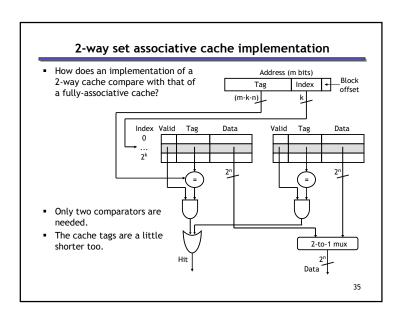
1-way associativity 8 sets, 1 block each Set Set Set O 1 2 3 3 4 5 5 6 7 7

LRU example

- Assume a fully-associative cache with two blocks, which of the following memory references miss in the cache.
 - assume distinct addresses go to distinct blocks







Set associative caches are a general idea By now you may have noticed the 1-way set associative cache is the same as a direct-mapped cache. • Similarly, if a cache has 2^k blocks, a 2^k-way set associative cache would be the same as a fully-associative cache. 8-way 1-way 2-way 8 sets. 4 sets. 2 sets. 1 set, 2 blocks each 4 blocks each 8 blocks 1 block each fully associative direct mapped 34

Summary

- Larger block sizes can take advantage of spatial locality by loading data from not just one address, but also nearby addresses, into the cache.
- Associative caches assign each memory address to a particular set within the cache, but not to any specific block within that set.
 - Set sizes range from 1 (direct-mapped) to 2^k (fully associative).
 - Larger sets and higher associativity lead to fewer cache conflicts and lower miss rates, but they also increase the hardware cost.
 - In practice, 2-way through 16-way set-associative caches strike a good balance between lower miss rates and higher costs.
- Next, we'll talk more about measuring cache performance, and also discuss the issue of writing data to a cache.