Caches – basic idea

- Small, fast memory
- Stores frequently-accessed *blocks* of memory.
- When it fills up, discard some blocks and replace them with others.
- Works well if we reuse data blocks
  - Examples:
    - Incrementing a variable
    - Loops
    - Function calls
Why do caches work

Locality principles

Temporal locality
- Location of memory reference is likely to be the same as another recent reference.
- Variables are reused in program
- Loops, function calls, etc.

Spacial locality
- Location of memory is likely to be near another recent reference
- Matrices, arrays
- Stack accesses
Cache performance example

- Problem (let’s assume single cycle CPU)
  - 500 MHz CPU cycle time = 2 ns
  - Instructions: arithmetic 50%, load/store 30%, branch 20%.
  - Cache: hit rate: 95%, miss penalty: 60 ns (or 30 cycles), hit time: 2 ns (or 1 cycle)

- MIPS CPI w/o cache for load/store:
  - $0.5 \times 1 + 0.2 \times 1 + 0.3 \times 30 = 9.7$

- MIPS CPI with cache for load/store:
  - $0.5 \times 1 + 0.2 \times 1 + 0.3 \times (0.95 \times 1 + 0.05 \times 30) = 1.435$
Caching Vocabulary

- **Miss Penalty** - time to fetch a block from a lower level cache or main memory

- **Block (Line) size** – Amount of data in each cache address (32-256 bytes)

- **Bank Size** - # of sets in the cache

- **Cache Size** –
  - Total Data contained = (bank size) x (associativity) x (block size)
  - Usually 4-64Kb for L1, 128-512 Kb L2
Cache types

- Direct-mapped
  - Memory location maps to single specific cache line (block)
  - What if two locations map to same line (block)?
    - Conflict, forces a miss

- Set-associative
  - Memory location maps to a set containing several blocks.
  - Each block still has tag and data, and sets can have 2,4,8,etc. blocks. Blocks/set = associativity
    - If two locations map to same set, one could be stored in first block of the set, and another in second block of the set.

- Fully-associative
  - Cache only has one set. All memory locations map to this set.
  - This one set has all the blocks, and a given location could be in any of these blocks
  - No conflict misses, but costly. Only used in very small caches.
More on Types

Direct mapped

Set associative

Fully associative

Block # 0 1 2 3 4 5 6 7

Set # 0 1 2 3

Tag

Data

Search

Tag

Data

Search

Tag

Data

Search
Direct-mapped cache example

- 4 KB cache, each block is 32 bytes
- How many blocks?
- How long is the index to select a block?
- How long is the offset (displacement) to select a byte in block?
- How many bits left over if we assume 32-bit address? These bits are tag bits
Direct-mapped cache example

- 4 KB cache, each block is 32 bytes
  - $4 \text{ KB} = 2^{12}$, $32 = 2^5$

- How many blocks?
  - $2^{12}\text{ bytes} / 2^5\text{ bytes in block} = 2^7 = 128\text{ blocks}$

- How long is the index to select a block?
  - $\log_2{128} = 7\text{ bits}$

- How long is the offset (displacement) to select a byte in block?
  - 5 bits

- How many bits left over if we assume 32-bit address? These bits are tag bits
  - $32 - 7 - 5 = 20\text{ bits}$
Direct Mapped 4-word Block

- Address and cache:

![Diagram of a direct mapped cache with a 4-word block.](image)
4-way Associative 1-word block
Cache Misses: The Three Cs

- **Compulsory:**
  - Very first access of a block (Cold-Start Misses)

- **Capacity:**
  - Cache is too small to hold all blocks in the working set. Some are discarded to be retrieved later

- **Conflict:** (only in Direct or Set Assoc.)
  - More than $n$ blocks map to a set in an $n$-way set associative cache.
Cache size

- 4 KB visible size

Let’s look at total space and overhead:

- Each block contains:
  - 1 valid bit
  - 20-bit tag
  - 32 bytes of data = 256 bits
  - Total block (line) size: 1+20+256 = 277 bits

- Total cache size in hardware, including overhead storage:
  - 277 bits * 128 blocks = 35456 bits = 4432 bytes = 4.32 Kb
  - Overhead: 0.32 Kb (336 bytes) for valid bits and tags
Cache access examples…

- Consider a direct-mapped cache with 8 blocks and 2-byte block. Total size = 8 * 2 = 16 bytes
- Address: 1 bit for offset/displacement, 3 bits for index, rest for tag
- Consider a stream of reads to these bytes:
  - These are byte addresses:
    - A@3, B@13, C@1, D@0, E@5, F@1, G@4, H@32, I@33, J@1
  - Corresponding block addresses ((byteaddr/2)%8):
    - 1, 6, 0, 0, 2, 0, 2, 0 (16%8), 0, 0.
  - Tags: 2 for 32, 33, 0 for all others ((byteaddr/2)/8).
- Let’s look at what this looks like. How many misses?
- What if we increase associativity to 2? Will have 4 sets, 2 blocks in each set, still 2 bytes in each block. Total size still 16 bytes. How does behavior change?...

(get notes from someone for the drawings)