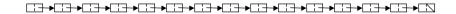


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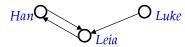
Chapter 9



Graphs

Graphs:

- A data structure useful for representing relationships between things
- A graph G is represented as G = (V, E)
 - V =a set of vertices (nodes)
 - E = a set of *edges* connecting vertices from V



 More general and arbitrary than trees (trees are a restricted type of graph)

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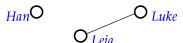
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Directed/Undirected Graphs

• In *directed* graphs, edges have a specific direction:



• In *undirected* graphs, they don't:



• Vertices u and v are adjacent if $(u,v) \in E$

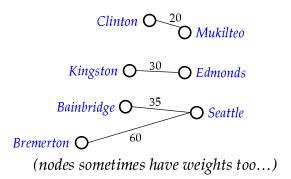
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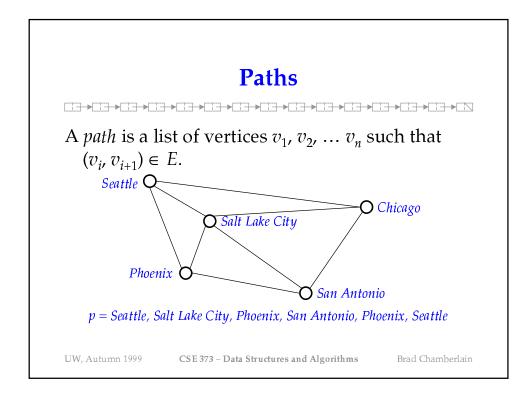
Weighted Graphs

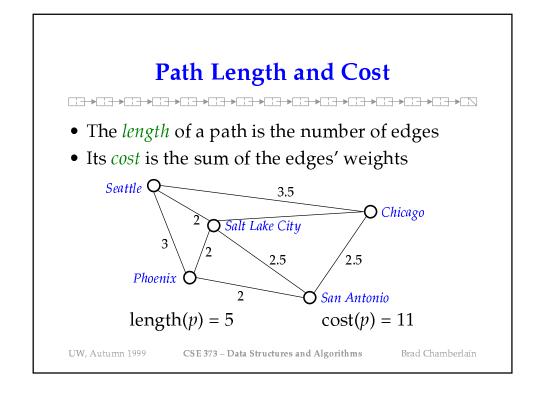
weighted graphs store a weight with each edge:



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Simple Paths and Cycles

A *simple path* repeats no vertices (except the first can also be the last):

- Seattle, Salt Lake City, Phoenix, San Antonio
- Seattle, Salt Lake City, San Antonio, Phoenix, Seattle

A *cycle* is a path that starts and ends at the same node

- Seattle, Salt Lake City, San Antonio, Phoenix, Seattle (For undirected graphs edges cannot appear twice)

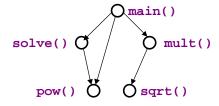
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Directed Acyclic Graphs

Directed Acyclic Graphs (DAGs) are directed graphs that contain no cycles



 $trees \subset DAGs \subset directed \ graphs$

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Connectivity



- Undirected graphs are *connected* if there is a path between any two vertices
- Directed graphs are *strongly connected* if there is a path between any two vertices
- It is *weakly connected* if it's connected when direction is ignored
- A *complete* graph is one that has an edge between every pair of vertices

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Graph Implementations

Adjacency Matrix: A $|V| \times |V|$ array in which:

- element (\mathbf{u}, \mathbf{v}) is 1 if there is an edge (u, v)
- it is 0 otherwise
- for weighted graphs, store weights rather than 1/0



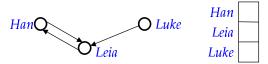
– space requirements?

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Graph Implementations

Adjacency Lists: A |V|-ary array in which each entry stores a list of all adjacent vertices



Space requirements?

How could we index into an adjacency list or matrix when nodes are named?

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Graph Applications

- Storing things that are graphs by nature (AI)
 - distances between cities
 - airline flights, travel options
 - relationships between people, things
 - distances between rooms in the game Clue
- Compilers
 - *callgraph* which functions call which other ones
 - dependence graphs which variables are defined and used at which statements

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