Heap Problems

1. Ternary Heaps

Consider the following sequence of numbers:

\[5, 20, 10, 6, 7, 3, 1, 2\]

(a) Insert these numbers into a min-heap where each node has up to three children, instead of two.

(So, instead of inserting into a binary heap, we’re inserting into a ternary heap.)

Draw out the tree representation of your completed ternary heap.

(b) Draw out the array representation of the above tree. In your array representation, you should start at index 0 (not index 1).

(c) Given a node at index \(i\), write a formula to find the index of the parent.

(d) Given a node at index \(i\), write a formula to find the \(j\)-th child. Assume that \(0 \leq j < 3\).

2. Heaps – More Basics

(a) Insert the following sequence of numbers into a min heap:

\[10, 7, 15, 17, 12, 20, 6, 32\]

(b) Now, insert the same values into a max heap.

(c) Now, insert the same values into a min heap, but use Floyd’s buildHeap algorithm.

(d) Insert 1, 0, 1, 1, 0 into a min heap.

(e) Call removeMin on the min heap stored as the following array: \[2, 5, 7, 8, 10, 9\]

3. Sorting and Reversing (with Heaps)

(a) Suppose you have an array representation of a heap. Must the array be sorted?
(b) Suppose you have a sorted array (in increasing order). Must it be the array representation of a valid min-heap?

(c) You have an array representation of a min-heap. If you reverse the array, does it become an array representation of a max-heap?

(d) Describe the most efficient algorithm you can think of to convert the array representation of a min-heap into a max-heap. What is its running time?

4. Project Prep: Contains

You just finished implementing your heap of ints when your boss tells you to add a new method called contains. Your solution should not, in general, examine every element in the heap (do it recursively!)

(a) How efficient do you think you can make this method?

(b) Write code for contains. Remember that heapArray starts at index 0!

5. Challenge: Debugging Heaps of Problems

For this problem, we will consider a hypothetical hash table that uses linear probing and implements the IDictionary interface. Specifically, we will focus on analyzing and testing one potential implementation of the remove method.

(a) Come up with at least 4 different test cases to test this remove(…) method. For each test case, describe what the expected outcome is (assuming the method is implemented correctly).

Try and construct test cases that check if the remove(…) method is correctly using the key's hash code. (You may assume that you can construct custom key objects that let you customize the behavior of the equals(…) and hashCode( ) method.)

(b) Now, consider the following (buggy) implementation of the remove(…) method. List all the bugs you can find.

(c) Briefly describe how you would fix these bug(s).